

UNCLASSIFIED

AD NUMBER

**AD859287**

NEW LIMITATION CHANGE

TO

**Approved for public release, distribution  
unlimited**

FROM

**Distribution authorized to U.S. Gov't.  
agencies and their contractors;  
Administrative/Operational Use; APR 1969.  
Other requests shall be referred to Naval  
Air Systems Command, Washington, DC.**

AUTHORITY

**USNASC ltr, 26 Oct 1971**

THIS PAGE IS UNCLASSIFIED

Report No. MSD-P69-144



Contract No. 00019-68-C-0247

AD 859287

# COLLOCATION FLUTTER ANALYSIS STUDY

This document is subject to special export controls and transmittal to foreign governments or foreign nationals may be made only with prior approval of the Naval Air Systems Command (AIR-~~550214~~).

6022

PLK/25 7/366

## VOLUME III.

AICs - COMPUTER PROGRAM TO CALCULATE UNSTEADY AERODYNAMIC INFLUENCE COEFFICIENTS FOR SUBSONIC, TRANSONIC AND SUPERSONIC FLIGHT

APRIL 1969



SEP 25 1969

MISSILE SYSTEMS DIVISION

**HUGHES**

HUGHES AIRCRAFT COMPANY

COFA

COLLOCATION FLUTTER ANALYSIS STUDY

VOLUME III

AICs - COMPUTER PROGRAM TO CALCULATE  
UNSTEADY AERODYNAMIC INFLUENCE COEFFICIENTS FOR  
SUBSONIC, TRANSONIC, AND SUPERSONIC FLIGHT

Prepared by Dynamics & Environments Section Personnel  
Hughes Aircraft Company, Missile Systems Division  
Contract No.00019-68-C-0247

APRIL 1969

This document is subject to special export controls and transmittal  
to foreign governments or foreign nationals may be made only with  
prior approval of the Naval Air Systems Command (AT&T)

TABLE OF CONTENTS

<u>Part</u>		<u>Page</u>
	TABLE OF CONTENTS	ii
	ABSTRACT	iii
I	INTRODUCTION	1
II	NOMENCLATURE	3
III	DISCUSSION OF THE DERIVATION OF AERODYNAMIC INFLUENCE COEFFICIENTS	5
IV	SUBSONIC PROGRAM	
	A. TECHNICAL DISCUSSION OF THE SUBSONIC KERNEL FUNCTION METHOD	27
	B. SUBSONIC AIC COMPUTER PROGRAM DESCRIPTION	36
	1. PROCESSING REQUIREMENTS	40
	2. INPUT INSTRUCTIONS	41
	3. SAMPLE PROBLEMS	48
	4. PROGRAM LISTING	88
	5. FLOW CHARTS	126
V	TRANSONIC PROGRAM	
	A. TECHNICAL DISCUSSION OF THE TRANSONIC BOX METHOD	206
	B. TRANSONIC AIC COMPUTER PROGRAM DESCRIPTION	210
	1. PROCESSING REQUIREMENTS	215
	2. INPUT INSTRUCTIONS	216
	3. SAMPLE PROBLEMS	224
	4. PROGRAM LISTING	251
	5. FLOW CHARTS	290
VI	SUPersonic PROGRAM	
	A. TECHNICAL DISCUSSION OF THE SUPersonic BOX METHOD	374
	B. SUPersonic AIC COMPUTER PROGRAM DESCRIPTION	381
	1. PROCESSING REQUIREMENTS	387
	2. INPUT INSTRUCTIONS	388
	3. SAMPLE PROBLEMS	394
	4. PROGRAM LISTING	421
	5. FLOW CHARTS	459
VII	REFERENCES	520

## ABSTRACT

Subsonic Kernel function, transonic box, and supersonic box methods for computing unsteady aerodynamics are applied to the problem of interaction of a general trapezoidal wing with a downstream rectangular control surface lying in the wake of the wing. The unsteady aerodynamic forces are related to a set of collocation stations through a series of matrix transformations, interpolations, and differentiations. The resulting matrix is a set of aerodynamic influence coefficients (AICs) that are directly applicable to flutter analysis.

The transformation of the unsteady aerodynamics into AICs is presented as a separate discussion; followed by discussions for the developments of analytical techniques for each flight regime. The analytical developments and a discussion of the basic single-planar-surface are presented, followed by the complete two-surface solutions for the general aerodynamic forces. Each of the three numerical methods is developed by detailing the complete set of equations necessary to compute airloads on the configurations considered. A computer program to determine the AIC matrix for each flight regime is presented with a complete discussion of usage and logical flow. Also included are program listings, flow charts and sample input and output problems.

## PART I - INTRODUCTION

The requirements for determination of flutter margins of safety for the lifting surfaces of advanced guided missiles have precipitated a need for accurate methods of analysis of unsteady aerodynamic loading in the high subsonic, transonic, and supersonic flight regimes. These methods must not only account for the high degree of chordwise and spanwise deformation of the surfaces, but also include the interference effects between tandem lifting surfaces. Recent developments in lifting surface theory in the three Mach number regimes have permitted extensions (Refs. 2 and 3) to determine airloads on typical missile wings with downstream control surfaces. These extensions account for the interaction and wake effects as well as for the three-dimensionality of the flow for a trapezoidal wing planform and a coplanar rectangular control surface placed at an arbitrary distance downstream of the unswept trailing edge of the wing. An underlying assumption in these methods is that the missile body diameter is large enough compared to the spans of the surfaces that the body surface acts as a reflection plane for disturbances at the line of its intersection with the lifting surfaces.

The present study extends the methods of Ref. 3 to obtain aerodynamic influence coefficients (AIC's) that relate the forces on the surfaces at a discrete set of points (control or collocation points) to the transverse deflections of the same set of points. Subsonic kernel function, transonic box, and supersonic box methods for computing the oscillatory AIC's are applied to the interference problem of a general trapezoidal wing with a downstream rectangular control surface lying in the wake of the wing. Highly efficient numerical methods for computation by the kernel function and Mach box techniques have been employed, along with the techniques for the newly developed transonic box method, to obtain AIC's which account for all interference effects within the framework of linearized theory.

Discussion of the derivation of the AIC's is given in Part III for the three Mach number regimes. The analytical basis of the theories are outlined in Appendices to Part III. Each of the three numerical methods is discussed and the basic equations necessary to compute airloads on the configurations considered are summarized.

The three computer programs are presented in Parts IV, V, and VI, for the subsonic, sonic, and supersonic cases, respectively. In addition to a technical outline of the methods employed, each Part is a manual containing a complete discussion of usage and logical flow accompanied by program listings, flow charts and sample input and output. Each Part also presents results computed by operation of the program for typical planforms.

PART II - NOMENCLATURE

a	Free-stream acoustic velocity
$a_{n,m}$	Coefficients of Kernel function pressure series
b	L cal semi-chord
$b_r$	Reference semi-chord
$c_h$	Element of dimensionless AIC matrix
$c_p$	Pressure coefficient
$D_{n,m}$	Element of Kernel function matrix
G	Supersonic source influence function
h	AIC control point displacement.
K	Kernel function
k	Local reduced frequency $\sim \frac{\omega b}{U}$
$k_r$	Reference reduced frequency $\sim \frac{\omega b_r}{U}$
M	Mach number
p	Complex amplitude of pressure
S	Planform area
s	Semi-span
U	Free-stream fluid velocity
$U_k$	Chebyshev polynomial

$[W]$	Substantial derivative matrix
w	Complex amplitude of downwash
X,Y,Z	Cartesian coordinate system
$\beta^2$	$1-M^2$ for $M < 1$ ; $M^2-1$ for $M > 1$
$\Delta$	Box length
$\xi, \eta, \zeta$	Cartesian coordinate system variables
$\tilde{\xi}, \tilde{\eta}$	Special coordinates for collocation and integration points
$\phi$	Complex amplitude of velocity potential
$\psi$	Transonic doublet influence function
$\rho$	Atmospheric density
$\omega$	Angular frequency of harmonic oscillation $\sim$ rad/sec
AR	Aspect ratio $\sim 2s^2/S$

### PART III

#### DISCUSSION OF THE DERIVATION OF AERODYNAMIC INFLUENCE COEFFICIENTS

#### DERIVATION OF SUBSONIC AERODYNAMIC INFLUENCE COEFFICIENTS

The subsonic kernel function procedure was developed by Watkins, Woolston and Cunningham,<sup>1</sup> extended to a wing-tail combination by Moore and Park,<sup>2</sup> and refined by Andrew.<sup>3</sup> The present study extends the method of Ref. 3 to obtain aerodynamic influence coefficients (AICs). Oscillatory AICs have been defined in Ref. 4 to relate control point forces to control point deflections through the matrix equation.

$$\{F\} = \rho \omega^2 b_r^2 s [C_h] \{h\} \quad (3.1)$$

The derivation of the AICs requires a review of the technique of Refs. 1 - 3. (NOTE: These references are outlined in Part IV, Section A). The starting point is an assumed series for the lifting pressure distribution. It is chosen in the form<sup>3</sup>

$$C_p(\xi, \eta) = \frac{\sqrt{s^2 - \eta^2}}{b(\eta)} \sum_{n=0}^N \sum_{m=0}^M a_{nm} P_m(\eta) f_n(\xi) \quad (3.2)$$

where the chordwise pressure functions are

$$f_0(\xi) = \sqrt{(1 - \xi^2) / (1 + \xi^2)} \quad (3.3a)$$

$$f_n(\xi) = \sqrt{1 - \xi^2} U_{n-1}(\xi), \quad 1 \leq n \quad (3.3b)$$

the spanwise pressure functions are

$$P_0(\eta) = 1.0 \quad (3.4a)$$

$$P_m(\eta) = \eta^2 U_{m-1}(\eta), \quad i \leq m \quad (3.4b)$$

and the Chebyshev polynomial recurrence relation is

$$U_k(x) = 2x U_{k-1}(x) - U_{k-2}(x) \quad (3.5)$$

when  $U_0(x) = 1.0$  and  $U_1(x) = 2x$ . The numerical procedures of Refs. 1 - 3 lead to a matrix formulation of the aerodynamic lifting surface integral equation as an equation between the control point down-washes and the amplitudes of the assumed pressure modes

$$\{w/U\} = [D_{nm}] \{a_{nm}\} \quad (3.6)$$

The solution of Eq. 3.6 by least-squares methods is given by Ref. 3 which we write in the form

$$\{a_{nm}\} = [A_{M<1}] \{w/U\} \quad (3.7)$$

In order to find the AICs it is necessary to define a grid of control points. We find it convenient to divide the surface into NS strips and to locate the control points on the centerline of each strip. We further choose NC control points on each strip located at the same fractional chord location on each strip. A typical distribution of control points is shown in Figure 3.1 for a wing-tail combination.

The downwashes required in Eq. 3.7 are obtained by a substantial differentiation of the AIC control point deflections

$$\{w/U\} = [W] \{h\} \quad (3.8)$$

Since the downwashes required in Ref. 3 are at an optimum set of points different from the AIC control points, the matrix  $[W]$  is seen to be an interpolation as well as a substantial differentiation matrix.

TYPICAL DISTRIBUTION OF CONTROL POINTS

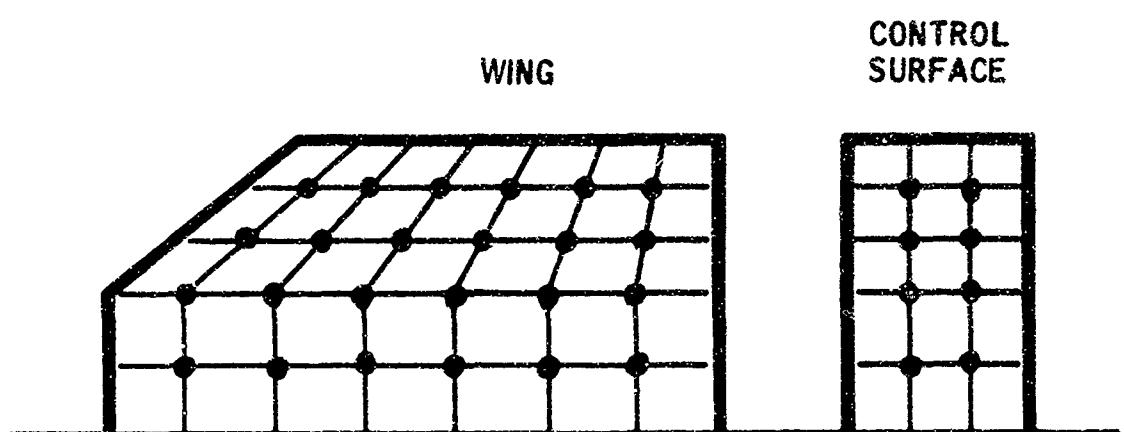


Figure 3.1

From the pressure nodes and their amplitudes the forces may be found by an integration procedure. The NC forces on each strip may be found by integration of the pressure on the strip in the region of each of the NC forces to obtain equivalent concentrated forces. This leads to a relationship between the forces and the pressure mode amplitudes

$$\{F\} = qs^2 [B] \{a_{nm}\} \quad (3.9)$$

We designate the matrix  $[B]$  as the integration matrix.

Combining Eqs. 3.7, 3.8 and 3.9, and identifying the result with Eq. 3.1 leads to the subsonic oscillatory AICs.

$$[C_h] = (s/2k_r^2) [B] [A_{M<1}] [W] \quad (3.10)$$

Ref. 3 provides  $[A_{M<1}]$ ; the extension to obtain AICs requires the development of the matrices  $[W]$  and  $[B]$ . These are discussed next.

#### THE SUBSTANTIAL DIFFERENTIATION MATRIX $[W]$

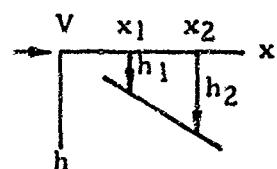
The substantial differentiation matrix is derived by surface fitting techniques. For maximum accuracy we fit the surface "in-the-small," i.e., locally. Rather than use a surface fit per se, we shall fit curves in the chordwise direction and then fit similar curves spanwise along lines of constant chord fraction. A higher order polynomial is not well behaved between points, so we choose to connect a series of parabolas. A number of options exists as the number of points is increased so it is well to develop the equations systematically.

With two control points the curve, of course, is a straight line. Its equation may be written in matrix form.

$$h(x) = [1 \ x] \begin{bmatrix} 1 & x_1 \\ 1 & x_2 \end{bmatrix}^{-1} \begin{Bmatrix} h_1 \\ h_2 \end{Bmatrix} \quad (3.11)$$

With three control points the parabola is given by

$$h(x) = \begin{bmatrix} 1 & x_1 & x_1^2 \\ 1 & x_2 & x_2^2 \\ 1 & x_3 & x_3^2 \end{bmatrix}^{-1} \begin{Bmatrix} h_1 \\ h_2 \\ h_3 \end{Bmatrix} \quad (3.12)$$



In the case of four points we fit two parabolas that are tangent half-way between the second and third points. For  $x < x_{2-3} = (x_2 + x_3)/2$  we write

$$h(x) = a_0 + a_1 x + a_2 x^2 \quad (3.13)$$

and for  $x > x_{2-3}$

$$h(x) = b_0 + b_1 x + b_2 x^2 \quad (3.14)$$

At  $x = x_{2-3}$  the deflections and slopes must be equal.

$$a_0 + a_1 x_{2-3} + a_2 x_{2-3}^2 = b_0 + b_1 x_{2-3} + b_2 x_{2-3}^2 \quad (3.15)$$

$$a_1 + 2a_2 x_{2-3} = b_1 + 2b_2 x_{2-3} \quad (3.16)$$

The unknown coefficients are determined by the solution of the matrix equation

$$\left[ \begin{array}{cccccc} 1 & x_1 & x_1^2 & 0 & 0 & 0 \\ 1 & x_2 & x_2^2 & 0 & 0 & 0 \\ 1 & x_{2-3} & x_{2-3}^2 & -1 & -x_{2-3} & -x_{2-3}^2 \\ 0 & 1 & 2x_{2-3} & 0 & -1 & -2x_{2-3} \\ 0 & 0 & 0 & 0 & x_3 & x_3^2 \\ 0 & 0 & 0 & 0 & x_4 & x_4^2 \end{array} \right] \left\{ \begin{array}{c} a_0 \\ a_1 \\ a_2 \\ b_0 \\ b_1 \\ b_2 \end{array} \right\} = \left[ \begin{array}{cccc} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{array} \right] \left\{ \begin{array}{c} h_1 \\ h_2 \\ h_3 \\ h_4 \end{array} \right\}$$
(3.17)

Solving for the coefficients leads to the equations for the curve.

$$h(x) = \left[ 1 \ x \ x^2 \ 0 \ 0 \ 0 \right] \left\{ \begin{array}{c} a_0 \\ a_1 \\ a_2 \\ b_0 \\ b_1 \\ b_2 \end{array} \right\} \text{ for } x \leq x_{2-3} \quad (3.18a)$$

$$= \left[ 0 \ 0 \ 0 \ 1 \ x \ x^2 \right] \left\{ \begin{array}{c} a_0 \\ a_1 \\ a_2 \\ b_0 \\ b_1 \\ b_2 \end{array} \right\} \text{ for } x \geq x_{2-3} \quad (3.18b)$$

The case of five points leads to the general pattern. We use two parabolas at the ends as in the four point case and one intermediate parabola that goes through one point and is tangent to the other parabolas.

For  $x < x_{2-3} - (x_2 + x_3)/2$

$$h(x) = a_0 + a_1 x + a_2 x^2 \quad (3.19)$$

$$h'(x) = a_1 + 2a_2 x \quad (3.20)$$

For  $x_{2-3} < x < x_{3-4} = (x_3 + x_4)/2$

$$h(x) = b_0 + b_1 x + b_2 x^2 \quad (3.21)$$

$$h'(x) = b_1 + 2b_2 x \quad (3.22)$$

Finally, for  $x > x_{3-4}$

$$h(x) = c_0 + c_1 x + c_2 x^2 \quad (3.23)$$

$$h'(x) = c_1 + 2c_2 x \quad (3.24)$$

The nine coefficients are found from the solution of

$$\left[ \begin{array}{ccccccc} 1 & x_1 & x_1^2 & 0 & 0 & 0 & 0 \\ 1 & x_2 & x_2^2 & 0 & 0 & 0 & 0 \\ 1 & x_{2-3} & x_{2-3}^2 & -1 & -x_{2-3} & -x_{2-3}^2 & 0 \\ 0 & 1 & 2x_{2-3} & 0 & -1 & -2x_{2-3} & 0 \\ 0 & 0 & 0 & 1 & x_3 & x_3^2 & 0 \\ 0 & 0 & 0 & 1 & x_{3-4} & x_{3-4}^2 & -1 \\ 0 & 0 & 0 & 0 & 1 & 2x_{3-4} & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & x_4 \\ 0 & 0 & 0 & 0 & 0 & 1 & x_5 \end{array} \right] \left\{ \begin{array}{l} a_0 \\ a_1 \\ a_2 \\ b_0 \\ b_1 \\ b_2 \\ c_0 \\ c_1 \\ c_2 \end{array} \right\} = \left[ \begin{array}{l} 1 \ 0 \ 0 \ 0 \ 0 \\ 0 \ 1 \ 0 \ 0 \ 0 \\ 0 \ 0 \ 0 \ 0 \ 0 \\ 0 \ 0 \ 0 \ 0 \ 0 \\ 0 \ 0 \ 1 \ 0 \ 0 \\ 0 \ 0 \ 0 \ 0 \ 0 \\ 0 \ 0 \ 0 \ 0 \ 0 \\ 0 \ 0 \ 0 \ 1 \ 0 \\ 0 \ 0 \ 0 \ 0 \ 1 \end{array} \right] \left\{ \begin{array}{l} h_1 \\ h_2 \\ h_3 \\ h_4 \\ h_5 \\ \vdots \end{array} \right\} \quad (3.25)$$

The general pattern is indicated by the partitioning. The equations for six or more points may be written by inspection. The equation for the curve may be written in the form

$$\left\{ \begin{array}{l} h(x < x_{2-3}) \\ h(x_{2-3} \leq x \leq x_{3-4}) \\ h(x \geq x_{3-4}) \end{array} \right\} = \begin{bmatrix} 1 & x & x^2 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & x & x^2 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & x & x^2 \end{bmatrix} \left\{ \begin{array}{l} a_0 \\ a_1 \\ a_2 \\ b_1 \\ b_2 \\ b_3 \\ c_0 \\ c_1 \\ c_2 \end{array} \right\} \quad (3.26)$$

The curves that are obtained from this procedure resemble the deflection curve of a beam over multiple deflected supports. If only one support is deflected the curve damps out as the distance from the deflected support is increased. Some examples of the surface fits are shown in Figures 3.2 - 3.4.

The foregoing procedure may be summarized formally by rewriting Eq. 3.25 as

$$[T(x_a)] \{a_n\} = [B(x_a)] \{h_a\} \quad (3.27)$$

and Eq. 3.26 as

$$\{h(x)\} = [C(x)] \{a_n\} \quad (3.28)$$

The deflection at an arbitrary location is found in terms of the AIC control point deflections by combining Eqs. 3.27 and 3.28.

TYPICAL (W) MATRIX DEFLECTION PATTERN  
FOR A UNIT DISPLACEMENT AT A

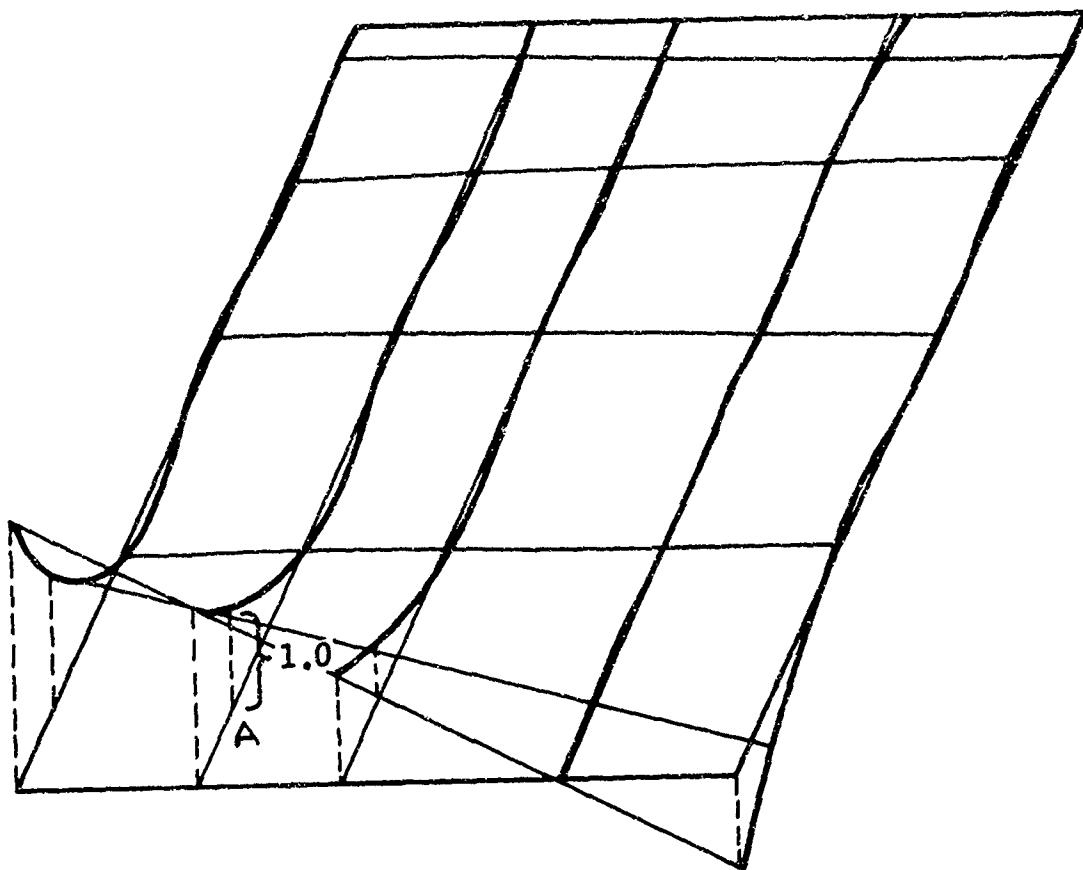


Figure 3.2

TYPICAL (W) MATRIX DEFLECTION PATTERN  
FOR A UNIT DISPLACEMENT AT B

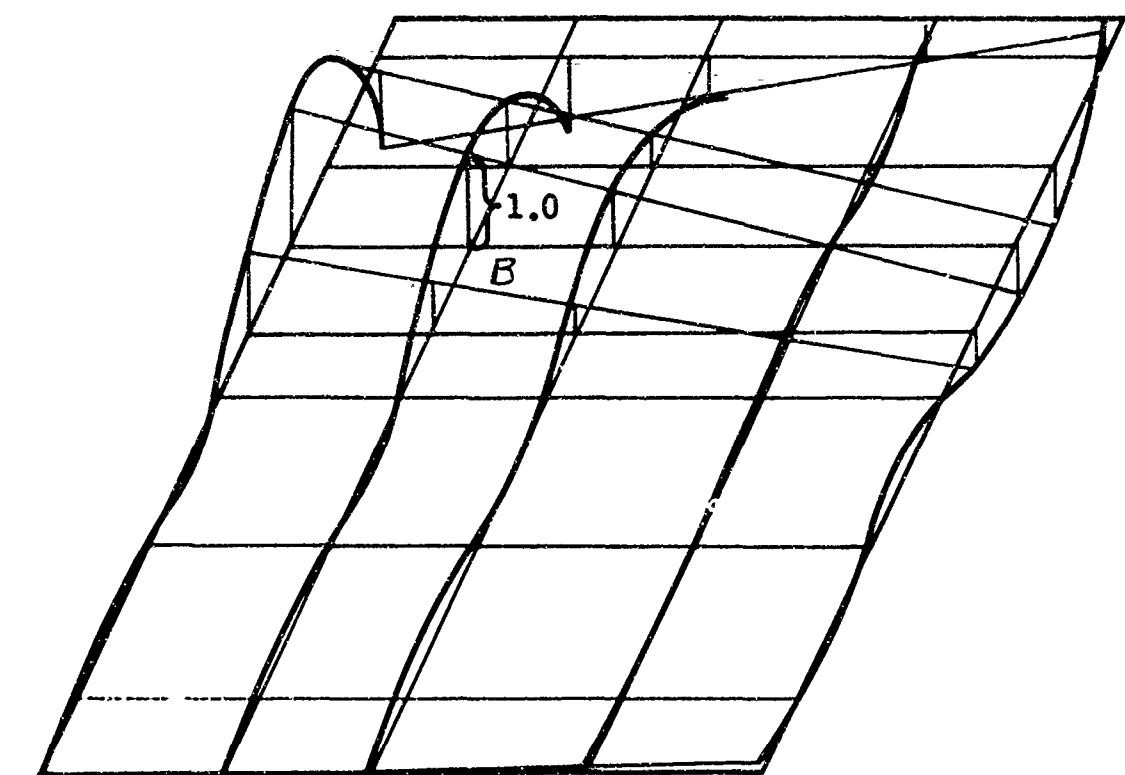


Figure 3.3

TYPICAL (W) MATRIX DEFLECTION PATTERN

FOR A UNIT DISPLACEMENT AT C

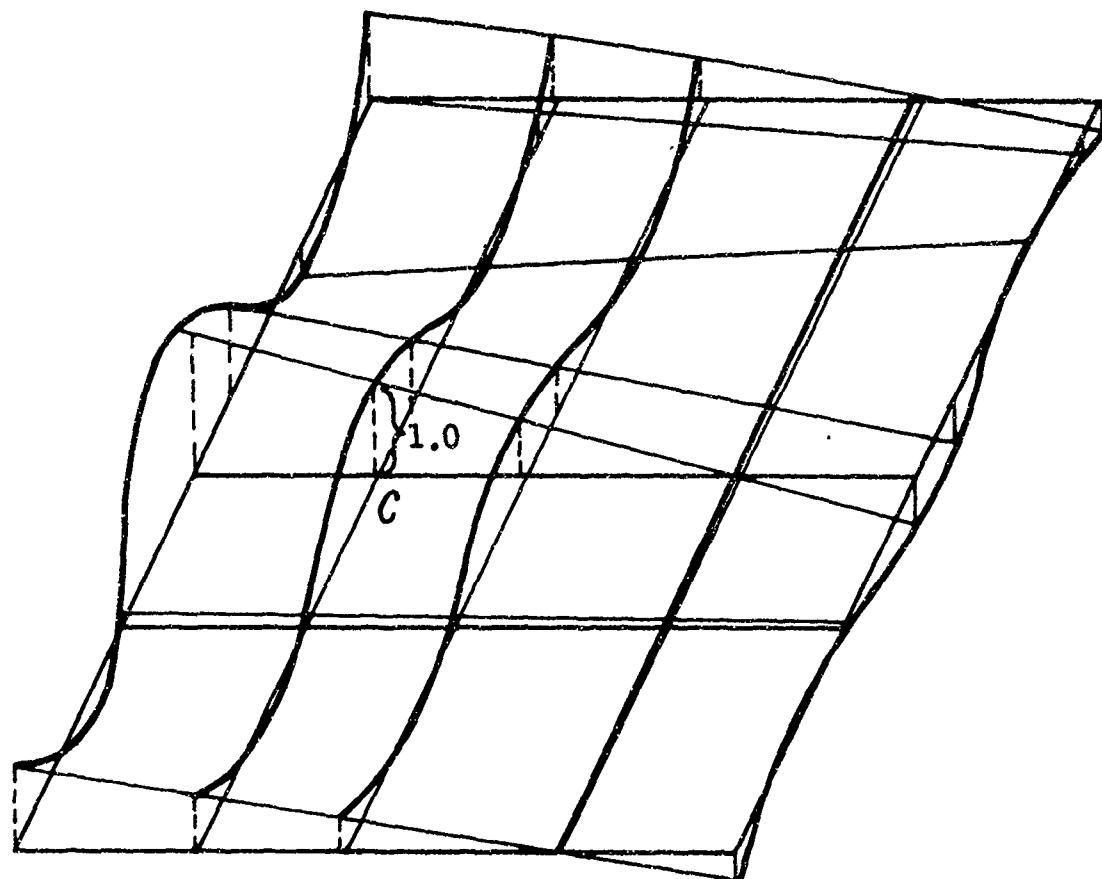


Figure 3.4

$$\{h(x)\} = [C(x)] [T(x_a)]^{-1} [B(x_a)] \{h_a\} \quad (3.29)$$

The downwash is the substantial derivative of Eq. 3.29.

$$\left\{ \frac{w(x)}{U} \right\} = \frac{\partial}{\partial x} \{h(x)\} + i \frac{\omega}{U} \{h(x)\} \quad (3.30a)$$

$$= \frac{\partial}{\partial x} \{h(x)\} + i \frac{k_r}{b_r} \{h(x)\} \quad (3.30b)$$

The derivative of Eq. 3.29 is

$$\frac{\partial}{\partial x} \{h(x)\} = [C'(x)] [T(x_a)]^{-1} [B(x_a)] \{h_a\} \quad (3.31)$$

where  $[C'(x)]$  is the matrix of derivatives of  $C(x)$ .

We next consider the interpolation in the spanwise direction. We have already defined  $\{h_a\}$  as the set of AIC control point deflections. Since the collocation points in the lifting surface theory have different chordwise and spanwise locations, we introduce the matrix  $\{h_b\}$  of deflections on the AIC strip centerline at the fractional chord locations of the lifting surface theory collocation points. Interpolation among the  $\{h_b\}$  on all of the strips then leads to the lifting surface theory collocation point deflections  $\{h_c\}$ . The substantial derivative matrix is then defined by

$$[W] \{h_a\} = \frac{\partial}{\partial x} \{h_c\} + i \frac{k_r}{b_r} \{h_c\} \quad (3.32)$$

The chordwise interpolation leads to

$$\{h_b\} = [C(x_b)] [T(x_a)]^{-1} [B(x_a)] \{h_a\} \quad (3.33)$$

and

$$\frac{\partial}{\partial x} \{h_b\} = [C'(x_b)] [T(x_a)]^{-1} [B(x_a)] \{h_a\} \quad (3.34)$$

Then the spanwise interpolation leads to

$$\{h_c\} = [C(y_c)] [T(y_a)]^{-1} [B(y_a)] \{h_b\} \quad (3.35)$$

and

$$\frac{\partial}{\partial x} \{h_c\} = [C(y_c)] [T(y_a)]^{-1} [B(y_a)] \frac{\partial}{\partial x} \{h_b\} \quad (3.36)$$

The required matrix  $[W] = [W_R] + i[W_I]$  is found by combining Eqs. 3.32 - 3.36. The real and imaginary parts appear formally as

$$[W_R] = [C(y_c)] [T(y_a)]^{-1} [B(y_a)] [C'(x_b)] [T(x_a)]^{-1} [B(x_a)] \quad (3.37)$$

and

$$[W_I] = (k_r/b_r) [C(y_c)] [T(y_a)]^{-1} [B(y_a)] [C(x_b)] [T(x_a)]^{-1} [B(x_a)] \quad (3.38)$$

The formalism may be illustrated simply by considering two strips with 4 AIC points and 4 aerodynamic collocation points as shown in Figure 3.5.

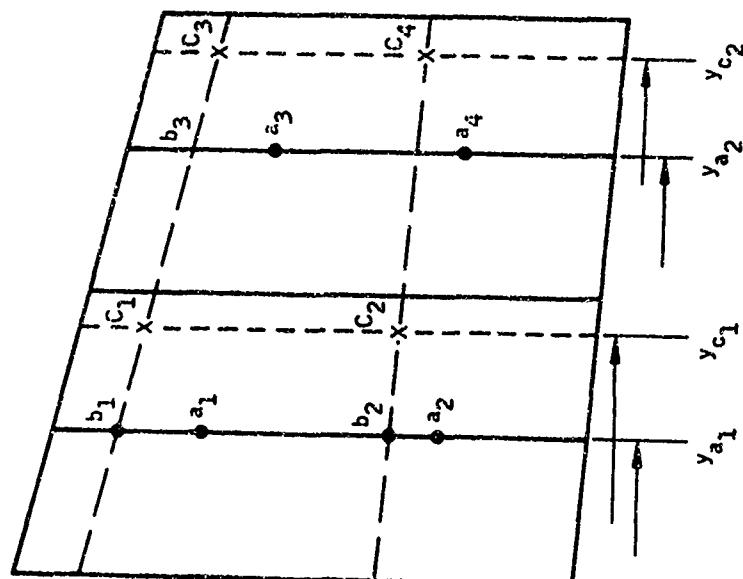


Figure 3.5

On the two strips

$$\begin{bmatrix} h_{b_1} \\ h_{b_2} \end{bmatrix} = \begin{bmatrix} 1 & x_{b_1} \\ 1 & x_{b_2} \end{bmatrix} \begin{bmatrix} 1 & x_{a_1} \\ 1 & x_{a_2} \end{bmatrix}^{-1} \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} h_{a_1} \\ h_{a_2} \end{bmatrix}$$

$$= [X_{12}] \begin{bmatrix} h_{a_1} \\ h_{a_2} \end{bmatrix}$$

$$\begin{bmatrix} h_{b_3} \\ h_{b_4} \end{bmatrix} = \begin{bmatrix} 1 & x_{b_3} \\ 1 & x_{b_4} \end{bmatrix} \begin{bmatrix} 1 & x_{a_3} \\ 1 & x_{a_4} \end{bmatrix}^{-1} \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} h_{a_3} \\ h_{a_4} \end{bmatrix}$$

$$= [X_{34}] \begin{bmatrix} h_{a_3} \\ h_{a_4} \end{bmatrix}$$

The slopes on the two strips are

$$\frac{\partial}{\partial x} \begin{bmatrix} h_{b_1} \\ h_{b_2} \end{bmatrix} = \begin{bmatrix} 0 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & x_{a_1} \\ 1 & x_{a_2} \end{bmatrix}^{-1} \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} h_{a_1} \\ h_{a_2} \end{bmatrix}$$

$$\frac{\partial}{\partial x} \begin{bmatrix} h_{b_3} \\ h_{b_4} \end{bmatrix} = \begin{bmatrix} 0 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & x_{a_3} \\ 1 & x_{a_4} \end{bmatrix}^{-1} \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} h_{a_3} \\ h_{a_4} \end{bmatrix}$$

Combining the deflections yields a partitioned form

$$\begin{Bmatrix} h_{b_1} \\ h_{b_2} \\ h_{b_3} \\ h_{b_4} \end{Bmatrix} = \begin{bmatrix} X_{12} & | & 0 \\ \hline & | & | \\ 0 & | & X_{34} \end{bmatrix} \begin{Bmatrix} h_{a_1} \\ h_{a_2} \\ h_{a_3} \\ h_{a_4} \end{Bmatrix}$$

The spanwise interpolation on the two spanwise lines gives

$$\begin{Bmatrix} h_{c_1} \\ h_{c_3} \end{Bmatrix} = \begin{bmatrix} 1 & y_{c_1} \\ 1 & y_{c_2} \end{bmatrix} \begin{bmatrix} 1 & y_{a_1} \\ 1 & y_{a_2} \end{bmatrix}^{-1} \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \begin{Bmatrix} h_{b_1} \\ h_{b_3} \end{Bmatrix}$$

$$= [Y_{13}] \begin{Bmatrix} h_{b_1} \\ h_{b_3} \end{Bmatrix}$$

on the forward line and

$$\begin{Bmatrix} h_{c_2} \\ h_{c_4} \end{Bmatrix} = [Y_{13}] \begin{Bmatrix} h_{b_2} \\ h_{b_4} \end{Bmatrix}$$

on the aft line. Combining the deflections leads to another partitioned form but also requires a row rearrangement matrix to order the  $\{h_b\}$  properly

$$\begin{aligned} \begin{Bmatrix} h_{c_1} \\ h_{c_2} \\ h_{c_3} \\ h_{c_4} \end{Bmatrix} &= \begin{bmatrix} Y_{13} & & 0 \\ & \ddots & \\ & & Y_{13} \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{Bmatrix} h_{b_1} \\ h_{b_2} \\ h_{b_3} \\ h_{b_4} \end{Bmatrix} \\ &= [Y] [R] \begin{Bmatrix} h_{b_1} \\ h_{b_2} \\ h_{b_3} \\ h_{b_4} \end{Bmatrix} \end{aligned}$$

The same procedure is used for the slopes. We note that Eqs. 3.37 and 3.38 must be generalized to include the row rearrangement matrix, and the formal equations for the real and imaginary parts of the substantial differentiation matrix become

$$[w_R] = [C(y_c)] [T(y_a)]^{-1} [B(y_a)] [R] [C'(x_b)] [T(x_a)]^{-1} [B(x_a)]$$

and

$$[w_I] = (k_r/b_r) [C(y_c)] [T(y_a)]^{-1} [B(y_a)] [R] [C(x_b)] [T(x_a)]^{-1} [B(x_a)]$$

where the format of each factor is illustrated in the above example.

#### THE INTEGRATION MATRIX [B]

The integration matrix converts the pressure distribution on each strip into an equivalent system of concentrated forces at the AIC control points by integrating the pressure spanwise and chordwise in the region of each AIC control point.

The integration of the pressure coefficient, Eq. 3.2 in the region of the AIC point leads to the force

$$F_n = q \iint c_p(\xi, \eta) d\xi d\eta \quad (3.39)$$

Letting  $\eta = \cos \phi$  and  $\xi = \cos \theta$  in Eqs. 3.2 and 3.7 we obtain

$$F_n = q s^2 \sum_m \sum_n a_{nm} \int_{\theta_f}^{\theta_a} \int_{\phi_i}^{\phi_o} \sin^2 \phi \sin \theta P_m(\eta) f_n(\xi) d\phi d\theta \quad (3.39A)$$

where  $\theta_f$  and  $\theta_a$  denote the chordwise angular measure of the forward and aft locations, respectively, of the pressure region, and  $\phi_i$  and  $\phi_o$  denote the spanwise angular measure of the inboard and outboard end, respectively, of the strip. If we define the spanwise integral

$$I_m(\eta_i, \eta_o) = \int_{\phi_i}^{\phi_o} \sin^2 \phi P_m(\eta) d\phi \quad (3.39B)$$

and the chordwise integral

$$J_n(\tilde{\xi}_f, \tilde{\xi}_a) = \int_{\theta_f}^{\theta_a} \sin \theta f_n(\xi) d\theta \quad (3.39C)$$

then the force from the nm mode is

$$F_{n,m} = q s^2 a_{nm} I_m J_n \quad (3.39D)$$

and in matrix form

$$F_n = q s^2 \begin{bmatrix} I_m & J_n \end{bmatrix} \begin{Bmatrix} a_{nm} \end{Bmatrix} \quad (3.39E)$$

so that the integration matrix  $[B]$  is given by

$$[B] = [I_m(\eta_i, \eta_o) J_n(\tilde{\xi}_f, \tilde{\xi}_a)] \quad (3.39F)$$

The integrals are easily evaluated. Consider first the spanwise integration. In terms of the spanwise angular coordinate  $\phi$  we note

$$P_0(n) = 1.0 \quad (3.40)$$

$$\begin{aligned} P_m(n) &= n^2 U_{m-1}(n) \\ &= \cos^2 \phi \sin m\phi / \sin \phi, \quad 1 \leq m \end{aligned} \quad (3.40A)$$

Then

$$\begin{aligned} I_0(n_i, n_o) &= \int_{\phi_i}^{\phi_o} \sin^2 \phi \, d\phi \\ &= \frac{1}{2} (\cos^{-1} n_o - \cos^{-1} n_i - n_o \sqrt{1 - n_o^2} + n_i \sqrt{1 - n_i^2}) \end{aligned} \quad (3.40B)$$

For  $m \geq 1$

$$I_m = \int_{\phi_i}^{\phi_o} \sin \phi \cos^2 \phi \sin m\phi \, d\phi \quad (3.40C)$$

from which

$$\begin{aligned} I_1 &= \int_{\phi_i}^{\phi_o} \sin^2 \phi \cos^2 \phi \, d\phi \\ &= \frac{1}{6} \left[ n_o (1 - n_o^2)^{3/2} - n_i (1 - n_i^2)^{3/2} + I_0 \right] \end{aligned} \quad (3.40C)$$

and for  $m \geq 1, \neq 3$ ,

$$\begin{aligned} I_m &\approx \frac{1}{m} \left\{ \frac{1}{m-1} [\sin(m-1)\phi_o - \sin(m-1)\phi_i] \right. \\ &\quad - \frac{1}{m+1} [\sin(m+1)\phi_o - \sin(m+1)\phi_i] \\ &\quad \left. + \frac{1}{m-3} [\sin(m-3)\phi_o - \sin(m-3)\phi_i] \right. \\ &\quad \left. - \frac{1}{m+3} [\sin(m+3)\phi_o - \sin(m+3)\phi_i] \right\} \end{aligned} \quad (3.40D)$$

$$\text{NOTE: } \sin n\phi = 2 \cos \phi \sin(n-1)\phi - \sin(n-2)\phi \quad (3.40E)$$

$$\text{so that } \sin n\phi_o = 2 n_o \sin(n-1)\phi_o - \sin(n-2)\phi_o$$

$$\text{and } \sin n\phi_i = 2 n_i \sin(n-1)\phi_i - \sin(n-2)\phi_i$$

Finally,

$$\begin{aligned} I_3 &= 3I_1 - \frac{2}{3} \left[ n_o (1 - \frac{n_o^2}{n_o^2})^{5/2} - n_i (1 - \frac{n_i^2}{n_i^2})^{5/2} \right] \\ &\quad - \left\{ \frac{1}{4} \cos^{-1} n_o - \frac{1}{4} \cos^{-1} n_i - \frac{1}{4} \left( n_o \sqrt{1 - \frac{n_o^2}{n_o^2}} - n_i \sqrt{1 - \frac{n_i^2}{n_i^2}} \right) \right. \\ &\quad \left. - \frac{1}{6} \left[ n_o (1 - \frac{n_o^2}{n_o^2})^{3/2} - n_i (1 - \frac{n_i^2}{n_i^2})^{3/2} \right] \right\} \end{aligned} \quad (3.40D)$$

Consider next the chordwise integral. In terms of the chordwise angular coordinate  $\phi$  we note

$$f_o(\tilde{\xi}) = \frac{1 - \cos \phi}{\sin \phi} \quad (3.41)$$

$$f_n(\tilde{\xi}) = \sin n\phi, n \geq 1 \quad (3.42)$$

$$\begin{aligned} J_o(\tilde{\xi}_f, \tilde{\xi}_a) &= \int_{\phi_f}^{\phi_a} (1 - \cos \phi) d\phi \\ &= \cos^{-1} \tilde{\xi}_a - \cos^{-1} \tilde{\xi}_f - \sqrt{1 - \tilde{\xi}_a^2} + \sqrt{1 - \tilde{\xi}_f^2} \end{aligned} \quad (3.43)$$

For  $n > 1$

$$J_n = \frac{1}{2(n-1)} \left[ \sin(n-1)\phi_a - \sin(n-1)\phi_f \right] \quad (3.44)$$

$$- \frac{1}{2(n+1)} \left[ \sin(n+1)\phi_a - \sin(n+1)\phi_f \right]$$

and for  $n = 1$

$$J_1 = \frac{1}{2} \left[ \cos^{-1} \tilde{\xi}_a - \cos^{-1} \tilde{\xi}_f - \tilde{\xi}_a \sqrt{1 - \tilde{\xi}_a^2} + \tilde{\xi}_f \sqrt{1 - \tilde{\xi}_f^2} \right] \quad (3.45)$$

To illustrate the format of  $[B]$  consider the  $s^{\text{th}}$  strip

$$\begin{bmatrix} B_s \end{bmatrix} = \begin{bmatrix} I_m(n_s) J_n(\tilde{\xi}_1) \\ I_m(n_s) J_n(\tilde{\xi}_2) \\ I_m(n_s) J_n(\tilde{\xi}_{NC}) \end{bmatrix} \quad (3.46)$$

where  $n_s$  denotes the midpoint of the  $s^{\text{th}}$  strip, and  $\tilde{\xi}_1, \tilde{\xi}_2, \dots, \tilde{\xi}_{NC}$  denote the first through NC chordwise forces on the strip. Generalizing to NS strips and illustrating the dependence on  $n$  and  $m$  we have

$$\begin{bmatrix} B \end{bmatrix} = \begin{bmatrix} I_0(n_1) J_0(\tilde{\xi}_1) & I_1(n_1) J_1(\tilde{\xi}_1) & \dots & I_{NS}(n_1) J_{NS}(\tilde{\xi}_1) \\ I_0(n_1) J_0(\tilde{\xi}_2) & I_1(n_1) J_1(\tilde{\xi}_2) & & \\ I_0(n_1) J_0(\tilde{\xi}_{NC}) & I_1(n_1) J_1(\tilde{\xi}_{NC}) & & \\ I_0(n_2) J_0(\tilde{\xi}_1) & I_1(n_2) J_1(\tilde{\xi}_1) & & \\ I_0(n_2) J_0(\tilde{\xi}_{NC}) & I_1(n_2) J_1(\tilde{\xi}_{NC}) & & \\ I_0(n_{NS}) J_0(\tilde{\xi}_1) & I_1(n_{NS}) J_1(\tilde{\xi}_1) & & \\ I_0(n_{NS}) J_0(\tilde{\xi}_{NC}) & I_1(n_{NS}) J_1(\tilde{\xi}_{NC}) & I_{NS}(n_{NS}) J_{NS}(\tilde{\xi}_{NC}) & \end{bmatrix} \quad (3.47)$$

## DERIVATION OF SONIC AND SUPERSONIC AERODYNAMIC INFLUENCE COEFFICIENTS

The supersonic Mach box method was developed by Zartarian and Hsu<sup>4</sup> and extended to intersecting planar lifting surfaces by Moore and Andrew<sup>5</sup>. The sonic box method was developed by Rodemich and Andrew<sup>6</sup>. A further extension to the wing-tail combination was made by Moore and Park<sup>2</sup> and refined by Andrew<sup>3</sup>. (NOTE: These references are outlined in Part I, Section A for the sonic case, and in Part VI, Section A for the supersonic case.

The box methods lead to the velocity potentials whose streamwise substantial derivative gives the pressure coefficient. The solution for the velocity potentials may be written [cf. Eq. (?)]

$$\{\phi\} = \left[ A_{M \geq 1} \right] \{w/V\} \quad (3.48)$$

The pressure coefficients are given by

$$\{C_p\} = (2/a M) \left[ W_a \right] \{\phi\} \quad (3.49)$$

where  $[W_a]$  is the substantial derivative evaluated at the box centers. Since the boxes are all small the aerodynamic force on the boxes are approximately given by the product of the box pressure and its area. The forces on a strip (assumed to be narrow) are regarded as acting at the strip centerline and at the chordwise centerline of each spanwise line of boxes, and are found by summing spanwise the contribution of each box to the strip.

$$\{F_a\} = q [A] \{C_p\} \quad (3.50)$$

The elements of the diagonal area matrix  $[A]$  consist of the appropriate box area or fractions thereof lying on the strip from each spanwise line of boxes.

The box forces are converted into AIC control point forces by the static equivalence of the box forces in the region of each control point, i.e., the control points are assumed to be connected by a series of simple beams, hinged at each control point, so that the AIC control point forces are the reactions to the box forces distributed along the series of beams. This leads to approximate generalized forces since this method of representing the chordwise deflections is not consistent with that used in the  $[W]$  matrix. However, it leads to a more physically meaningful distribution of AIC forces, and the resulting approximation to the generalized forces in an arbitrary vibration mode is sufficiently accurate. Denoting the statically equivalent transformation matrix by  $[T]$  we have the AIC forces

$$\{F\} = [T] \{F_a\} \quad (3.51a)$$

$$= q [T] [A] \{c_p\} \quad (3.51b)$$

If the foregoing equations are combined, including Eq. 3.8, the AIC control forces are related to the control point deflections through

$$\{F\} = (2q/a_M) [T] [A] [W_a] [A_M \geq 1] [W] \{h\} \quad (3.52)$$

and leads to the AIC's by comparison with Eq. 3.1.

$$[c_h] = (1/a_M k_r^2 s) [T] [A] [W_a] [A_M \geq 1] [W] \quad (3.53)$$

PART IV - SECTION A

TECHNICAL DISCUSSION OF THE SUBSONIC  
KERNEL FUNCTION METHOD

INTRODUCTION

In defining aerodynamic influence coefficients, the aerodynamic loads are first derived by the well documented "Kernel function" method, and the resulting loads are then converted to aerodynamic influence coefficients. The procedure followed uses results from any of the pertinent papers, and extends the analysis to cover the problem of tandem surfaces.

The first published numerical procedure for solving the subsonic pressure distribution problem for isolated planar lifting surfaces undergoing simple harmonic motion was developed at NASA's Langley Research Center by Watkins, Runyan, and Woolston (Reference 1). Hsu (Reference 7) significantly advanced the logical development of the method when he established an optimum set of collocation and integration points. Rodemich (Reference 8), and later Landahl (Reference 9), have presented expressions for the kernel that are very much simpler than those previously used, and they take less time to evaluate. A further advance was made by Rodden and Revell (Reference 10), who described the matching of the boundary conditions with the least squared error. Rowe (Reference 11) has shown that to obtain sufficiently accurate results using Hsu's procedure, an extremely large number of collocation points must be used and when this is done, using the spanwise pressure function that Hsu and Watkins used, the downwash matrix becomes ill-conditioned. Rowe overcame this problem by using a Fourier series for the spanwise pressure function.

The present method uses Hsu's set of collocation points, Rodemich's expression for the kernel, Rodden and Revell's idea for matching the boundary conditions, and, like Rowe does, it uses an orthogonal set of functions for the spanwise pressure function. However, the present method utilizes these developments in a way that has not been previously published. The techniques employed result in speeds and accuracy not previously attained.

## TANDEM SURFACE VIBRATION IN SUBSONIC FLOW

The method presented herein was developed for application to a missile with a very low aspect ratio, trapezoidal wing and a downstream rectangular control surface lying in the wake of the wing. The diameter of the body of the missile is considered large enough to act as a reflection plane for acoustic signals that emanate from points on the lifting surfaces.

The problem to be considered is that of determining the air loads on the wing and control surface which are induced by a simple harmonic motion. The surrounding fluid is assumed to be compressible, inviscid isentropic, and irrotational. The perturbation potential is used, and the problem is further linearized by applying boundary conditions at the mean ( $z = 0$ ) surface. Thickness effects are ignored. With these hypothesis, it is well known that an integral relation exists between the pressure discontinuity over the surface  $z = 0$  and the downwash over the same plane. If the downwash and pressure difference are representable in the form

$$\begin{aligned} W_1(x, y, 0, t) &= W(x, y)e^{i\omega t} \\ \Delta P_1(x, y, 0, t) &= \Delta P(x, y)e^{i\omega t} \end{aligned} \quad (4.1)$$

The integral relation becomes

$$\frac{W(x, y)}{U} = -\frac{1}{8\pi} \iint \frac{\Delta P(\xi, \eta)}{\frac{1}{2}\rho U^2} K\left(\frac{\omega}{U}, M, x - \xi, y - \eta\right) d\xi d\eta \quad (4.2)$$

The integral extends over the plane  $z = 0$ , but the integrand is zero except over the wing and control surface. The kernel function  $K$  is strongly singular and integration in a spanwise direction requires the use of the finite part concept. This is indicated by the cross on the integration sign. Equation (4.2) then represents the integral equation of the system wherein, given  $W(x, y)$  over the wing and control surface,  $\Delta P$  must then be determined.

The function  $K(k, M, x-\xi, y-\eta)$  is represented here in the form

$$K\left(\frac{\omega}{U}, M, x-\xi, y-\eta\right) = e^{-i \frac{\omega}{U} (x-\xi)} \frac{K_1}{(y-\eta)^2} \quad (4.3)$$

where

$$K_1 = -k_1 K_1(k_1) - \frac{(x-\xi)}{R} e^{-i k_1 u_1} \quad (4.4)$$

$$+ i k_1 \int_0^1 \frac{w e^{-k_1 w}}{\sqrt{1-w^2}} dw + i k_1 \int_0^{u_1} \frac{u e^{-i k_1 u}}{\sqrt{1+u^2}} du$$

and  $R = \sqrt{(x-\xi)^2 + \beta^2 r_1^2}$

$$r_1 = |y-\eta|$$

$$k_1 = \frac{\omega r_1}{U}$$

$$u_1 = \frac{MR - (x-\xi)}{\beta^2 r_1}$$

$M$  = Mach number

$$\beta^2 = 1 - M^2$$

$K_1(k_1)$  is the modified Bessel function of the second kind of order one and argument  $k_1$ .

This form for the kernel function has been used in References 8 and 9. While it is not identical to that of Reference 1, it may be obtained directly from that equation by substitution of the integral representation of the modified Bessel and Struve functions. The second order singularity in the spanwise variable in Equation (4.3) requires the use of the "finite part" technique of Hadamard.

## PRESSURE DISTRIBUTION

As in many earlier studies, the pressure distribution is approximated as the sum of a series of functions which have the proper behavior as inferred from steady state and two-dimensional solutions. This behavior includes a Kutta condition at the trailing edge, a square root singularity at the leading edge, and a half ordered zero at the top for each surface. The pressure distribution on each surface is then approximated in the form

$$\frac{1}{2} \frac{\Delta p(\xi, \eta)}{\rho U^2} = \frac{\sqrt{s^2 - \eta^2}}{b(\eta)} \sum_{n=0}^N \sum_{m=0}^M a_{nm} P_m(\bar{\eta}) f_n(\tilde{\xi}) \quad (4.5)$$

where

$$f_0(\tilde{\xi}) = \sqrt{\frac{1 - \tilde{\xi}}{1 + \tilde{\xi}}} \quad f_n(\tilde{\xi}) = \sqrt{1 - \tilde{\xi}^2} U_{n-1}(\tilde{\xi}); 1 \leq n$$

$$P_0(\bar{\eta}) = 1.0 \quad P_m(\bar{\eta}) = \bar{\eta}^2 U_{m-1}(\bar{\eta}); 1 \leq m$$

$$U_0(x) = 1.0$$

$$U_1(x) = 2x \quad (4.6)$$

$$U_k(x) = 2xU_{k-1}(x) - U_{k-2}(x); 2 \leq k$$

$$\tilde{\xi} = \frac{\xi - \bar{\xi}}{b(\bar{\eta})} \quad \text{and} \quad \bar{\xi} = \frac{1}{2}(\xi_{l.e.} + \xi_{t.e.})$$

$$\bar{\eta} = \frac{\eta}{s}$$

The functions  $U_n$  are Chebyshev Polynomials and are introduced for purposes of convenience.

For a trapezoidal wing, the lines  $\xi = \text{constant}$  and  $\eta = \text{constant}$  are not orthogonal. This transformation maps each surface into a square in its  $(\xi, \eta)$  plane.

The fundamental integral Equation (4.2) is inverted by substituting Equation (4.5) into Equation (4.1), and determining the coefficient  $a_{nm}$  so that Equation (4.2) is equilibrated at a designated set of collocation points. This equilibrium is represented schematically in the form

$$\begin{Bmatrix} \begin{Bmatrix} W^W \\ U \end{Bmatrix} \\ \begin{Bmatrix} W^C \\ U \end{Bmatrix} \end{Bmatrix} = \begin{bmatrix} D_{nm}^{WW} & D_{nm}^{WC} \\ D_{nw}^{CW} & D_{nm}^{CC} \end{bmatrix} \begin{Bmatrix} \begin{Bmatrix} a_{nm}^W \\ a_{nm}^C \end{Bmatrix} \end{Bmatrix} \quad (4.7)$$

The left hand side of Equation (4.7) represents the prescribed downwash at the chosen set of collocation points.  $D_{nm}$   $a_{nm}$  is the effect on downwash of the corresponding term in the pressure series expansion. The superscripts W and C designate wing and control surface, respectively. The left superscript on the D's indicate the surface on which the collocation point is located, the right superscript, the surface over which the integral is taken. Then  $D_{nm}(x, y)$  is given by

$$D_{nm}(x, y) = -\frac{s^2}{8\pi} \int_{-1}^1 \sqrt{1 - \eta^2} P_m(\eta) \int_{-1}^1 f_n(\xi) \frac{K_1(x - \xi, y - \eta)}{(y - \eta)^2} d\xi d\eta \quad (4.8)$$

The integrals involved in Equation (4.8) are evaluated by following the methods of Hsu. In this procedure, the Gauss-Mehler quadrature is used, and the collocation points are selected by a method which is analogous to using the Gauss-Mehler quadrature on the inverse problem.

In brief, this technique is concerned with a numerical evaluation of an integral in the form

$$\int_a^b W(x) f(x) dx \approx \sum_{j=1}^n H_j f(x_j)$$

Where  $W(x)$  is a given weighting function,  $f(x)$  an arbitrary function, and  $H_j$  are weighting numbers. The first choice of points  $x_j$  is taken to be that corresponding to which the approximate integration would be exact for a polynomial of degree less than or equal to  $2n - 1$ . The integration points and weighting numbers are listed in Kopel (Reference 12) page 283. They are; for

$$\begin{aligned}
 W(x) &= (1-x)^\alpha (1+x)^\beta & (\alpha, \beta) &= \pm \frac{1}{2} \\
 && (a, b) &= (-1, +1) \\
 \alpha = \beta = \frac{1}{2} & \quad x_j = \cos \left( \frac{\pi j}{n+1} \right), \quad H_j = \frac{\pi(1-x_j^2)}{n+1} \\
 \alpha = \beta = -\frac{1}{2} & \quad x_j = \cos \left( \frac{(2j-1)\pi}{2n} \right), \quad H_j = \frac{\pi}{n} \\
 \alpha = -\beta = \frac{1}{2} & \quad x_j = \cos \frac{2\pi j}{2n+1}, \quad H_j = \frac{2\pi(1-x_j)}{2n+1} \\
 \alpha = -\beta = -\frac{1}{2} & \quad x_j = \cos \frac{(2j-1)\pi}{2n+1}, \quad H_j = \frac{2\pi(1+x_j)}{2n+1}
 \end{aligned} \tag{4.9}$$

where  $j = 1, 2, \dots, n$

The inner integral of Equation (4.8) is then evaluated by using the third of Equation (4.9), With the previously defined notation then

$$\int_{-1}^{+1} \sqrt{\frac{1-\tilde{\xi}}{1+\tilde{\xi}}} F_n(\tilde{\xi}) d\tilde{\xi} = \frac{2\pi}{2L+1} \sum_{k=1}^L H_k F_n(\tilde{\xi}_k) \quad (4.10)$$

where  $H_k = 1 - \tilde{\xi}_k$

$$\tilde{\xi}_k = -\cos \left( \frac{2k-1}{2L+1} \pi \right)$$

Hsu pointed out that if the collocation points are interdigitated according to the formula

$$\tilde{x}_1 = -\cos \left( \frac{2j}{2L+1} \pi \right)$$

the inner integral is evaluated with the least squared error by Equation (4.10).

This minimization was of course achieved for a single surface, but the convention was retained for the tandem surface model.

Hsu did not take advantage of the fact that the number of collocation points does not need to be as great as the number of integration points. In the present method the computer program user may specify the number of integration points to be any positive integer times the number of chordwise collocation points, so long as the number of integration points is 40 or less. Sixteen, or more, chordwise integration points are recommended. Accurate results can be assured only if the user specified a sufficient number of quadrature points for the integral.

Substitution of Equation (4.10) into Equation (4.8) gives

$$D_{nm} = \frac{\pi s^2}{8\pi} \int_{-1}^{+1} \frac{\sqrt{1-\eta^2}}{(y-\eta)^2} G_{nm}(x, y-\eta) d\eta \quad (4.11)$$

where

$$G_{nm} = \frac{2\pi}{2L+1} P_m(\eta) \sum_{k=1}^L (1 - \xi_k^2) U_{n-1}(\xi_k) K_1(x - \xi_k, y - \eta); \quad 1 \leq n$$

The integral for  $D_{nm}$  is singular. The Gauss-Mehler technique is again followed. This time the first of Equations (4.9) is used to perform the integration, and the finite part modification is introduced. With these constraints, Hsu has shown that the evaluation for  $D_{nm}$  becomes

$$D_{nm} = -\frac{1}{8\pi} \left\{ \sum_{p=1}^{M+1} \frac{(1-\eta_p)^2}{(y-\eta_p)^2} G_{nm}(x, y-\eta_p) - \pi(M+1) G_{nm}(x, 0) \right\}$$

and

$$G_{nm}(x, 0) = -2 \int_{-1}^x P_m(y) f_n(\tilde{\xi}) e^{-i\frac{\omega}{U}(x-\xi)} d\tilde{\xi}$$

When the collocation point lies on the control surface this integral is taken over the wing, from the leading edge ( $\tilde{\xi} = -1$ ) to the trailing edge ( $\tilde{\xi} = +1$ ), and over the control surface, from the leading edge to the collocation point ( $\tilde{\xi} = x$ ). The integrand of this expression does not vary widely over the region of integration and is evaluated with sufficient accuracy by a six-point quadrature formula. It has been made a part of the computer program and may not be controlled by the user.

PART IV - SECTION B  
SUBSONIC AIC COMPUTER PROGRAM DESCRIPTION

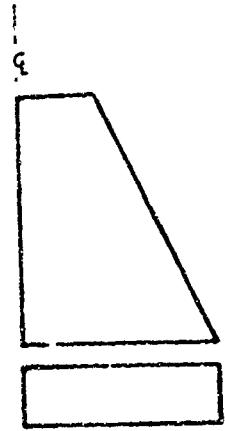
A FORTRAN IV computer program is presented which computes subsonic unsteady aerodynamic influence coefficients for a variety of tandem coplanar lifting surface configurations. The computer solution is based on a kernel function formulation which satisfies the linearized equations of motion of an inviscid, isentropic, compressible and irrotational fluid. The analysis is extended to include interaction effects between tandem surfaces and wake effects on the trailing surface.

The various configurations which can be analyzed are shown in Figure 4.1. The vehicle body is considered as a reflection plane for acoustic signals emanating from the aerodynamic surfaces thereby giving the surfaces a plane of symmetry, parallel to the free-stream flow. The upstream surface (wing) must have an unswept trailing edge and the rectangular trailing surface must have the same spanwise dimension as the trailing edge of the wing. The downstream surface lies in the wake of the wing; any non-negative value may be used for the gap dimension. A single surface cannot be analyzed, however, an option is provided which eliminates interaction effects. Thus it is possible to generate AIC's for individual surfaces isolated from disturbances in the flow field.

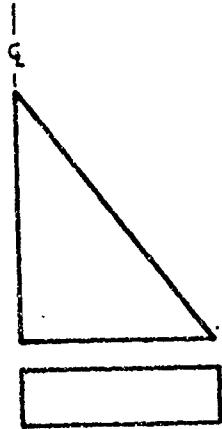
The program allows up to 40 AIC control points, 20 per surface. The AIC stations must satisfy the following requirements:

- (1) Both surfaces must have the same number of spanwise rows of control points. The chordwise location of respective rows on the surfaces need not be the same.
- (2) The chordwise rows must be parallel to the flow stream.
- (3) The chordwise rows on a surface must have the same number of control points.
- (4) The control points in each spanwise row must have the same fractional chord location.
- (5) The minimum number of chordwise or spanwise control points for a surface is two and the maximum number is ten.
- (6) The origin for the AIC station coordinates and the geometric coordinates for the planform must be at the leading edge root of the wing.

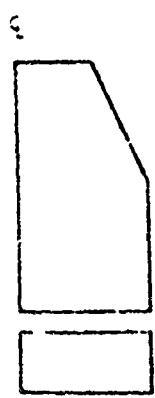
Examples of acceptable AIC control point patterns for the subsonic program are illustrated in Figure 4.2.



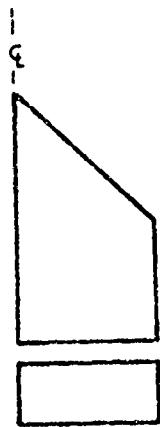
TRAPEZOIDAL



DELTA



TRAPEZOIDAL (CP DPLD)



DELTA (CROPPED)



RECTANGULAR

FIGURE 4.1 - TANDEM COPLANAR CONFIGURATIONS AT SUBSONIC MACH NUMBER

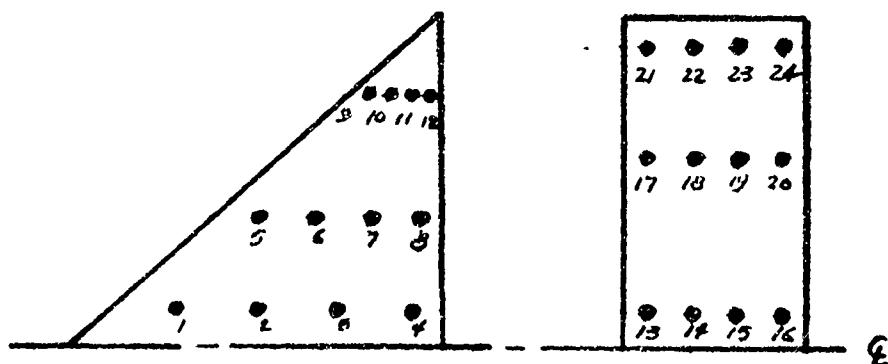
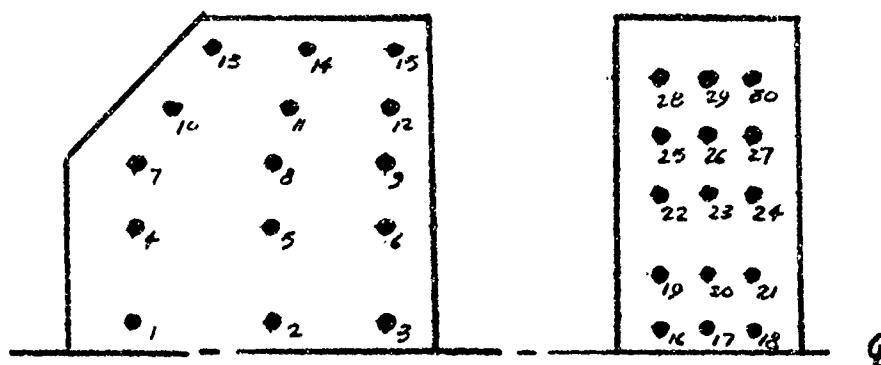
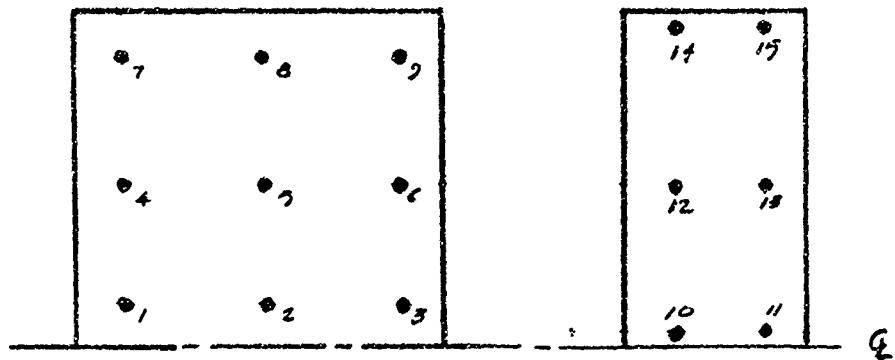


FIGURE 4.2 - EXAMPLES OF ACCEPTABLE AIC CONTOUR POINT PATTERNS FOR THE SISOMIC HEURISTIC

The computer program consists of a main program (MAIN) and 24 subroutines and functions subprograms. Execution begins with MAIN calling KFDA which reads input data and stores this information in core. The program then calls TRAMP which generates the substantial derivative matrix,  $[W]$ . The  $[W]$  matrix serves two functions. It relates the collocation stations of the unsteady aerodynamics to the control stations of the AIC matrix and it serves as a substantial derivative operator. Subroutines called by TRAMP are CMAT, SMAT, TMAT, BMAT, RMAT and MINV.

The next item computed is the kernel function matrix,  $[D]$ . The subroutine CORD is called for each unsteady aerodynamic collocation station and constructs the kernel function matrix which is dependent only on the relative location of the collocation stations and the Mach number-reduced frequency combination.

The pressure coefficients  $\{a_{nm}\}$  are found from the relation

$$\{a_{nm}\} = [D]^{-1} [W]$$

The program has been written such that the number of spanwise and chordwise pressure coefficient terms and the number of spanwise and chordwise collocation stations for the unsteady aerodynamics matches the respective number of AIC control points on each surface. Thus the Kernel function matrix is square and its inverse is computed directly. The subroutines employed for this operation are CGRED and XLSQ.

After deriving the pressure coefficients, the pressure terms are integrated spanwise and chordwise to obtain the force acting at each AIC control station. The resulting matrix, after it is multiplied by a non-dimensionalizing factor, is the final AIC matrix,  $[C_h]$ . By definition, the AIC matrix relates forces to displacements through the equation

$$\{F\} = \rho \omega^2 b_r^2 s \{C_h\} \{h\}$$

The semi-chord of the wing root is used as the reference chord,  $b_r$ .  $s$  is the semi-span of the wing (and tail) and  $\omega$  is the oscillatory frequency in radians/sec. This final phase of the subsonic AIC development uses the subroutines AICS, FORCE, ARCCOS, MINJS, and MINTC.

## 1.0 PROCESSING REQUIREMENTS

The input and output files used by the program are 05 and 06, respectively. All read and write statements are contained in the main program (MAIN) and the subroutines KFDA and KOUT. Peripheral tape and disc units are not used by the program. Approximately 40,000 cells of core storage is required. A standard input form of six 12-column fields per card is used by the program. Floating point numbers (6E12.5 format) may lie anywhere within the appropriate field, but fixed point numbers (6I12 format) must be right adjusted. Detailed instructions for data input are given and listings of data for sample problems are provided.

## 2.0 INPUT INSTRUCTIONS

Instructions for preparing input data for the subsonic AIC computer program are presented here. The field location and format for each input quantity is specified. Any set of units may be used for geometric dimensions and acoustic velocity as long as they are consistent, e.g., if feet is used for length then the acoustic velocity must have dimensions of feet per second.

### 1. Streamwise Coordinates (6E12.5 format)

Column	1-12	13-24	25-36	37-48	49-60	61-72
Name	X(1)	X(2)	X(3)	X(4)	X(5)	
Item	(1)	(2)	(3)	(4)	(5)	

- (1) X(1) Wing root leading edge streamwise coordinate
- (2) X(2) Wing tip leading edge streamwise coordinate
- (3) X(3) Wing trailing edge streamwise coordinate
- (4) X(4) Control surface leading edge streamwise coordinate
- (5) X(5) Control surface trailing edge streamwise coordinate

The technique for generating various configurations is shown in Table 4.1.

The origin for the planform and AIC station coordinates must be at the leading edge root of the wing therefore X(1) and Y(1), described below, must always be 0.0.

### 2. Spanwise Coordinates and Acoustic Velocity (6E12.5 format)

Column	1-12	13-24	25-36	37-48	49-60	61-72
Name	Y(1)	Y(2)	Y(3)	SOUND		
Item	(1)	(2)	(3)	(4)		

- (1) Y(1) Wing root spanwise coordinate
- (2) Y(2) Wing leading edge spanwise coordinate
- (3) Y(3) Wing (and control surface) tip spanwise coordinate
- (4) SOUND Acoustic velocity for altitude at which analysis is performed

FIGURE 1.3 - GEOMETRY DESCRIPTION

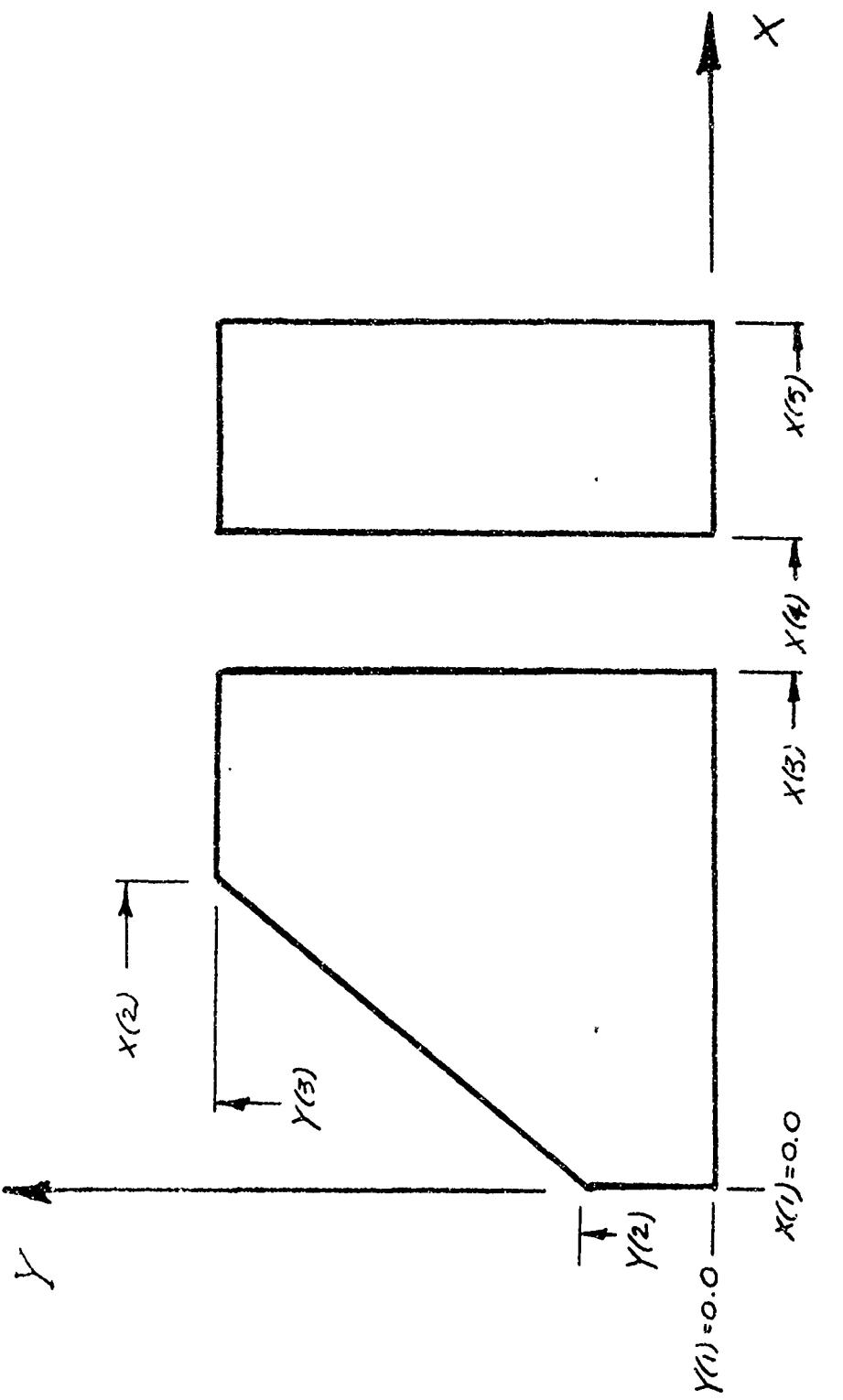


TABLE 4.1 - OPTIONAL CONFIGURATIONS

Configuration	Chordwise Coordinates	Spanwise Coordinates
Rectangular	X(1) = 0.0 X(2) = 0.0 X(3) > 0.0 X(4) > X(3) X(5) > X(4)	Y(1) = 0.0 Y(2) = 0.0 Y(3) > 0.0
Delta	X(1) = 0.0 X(2) > 0.0 X(3) = X(2) X(4) > X(3) X(5) > X(4)	Y(1) = 0.0 Y(2) = 0.0 Y(3) > 0.0
Trapezoidal	X(1) = 0.0 X(2) > 0.0 X(3) = X(2) X(4) > X(3) X(5) > X(4)	Y(1) = 0.0 Y(2) > 0.0 Y(3) > Y(2)
Trapezoidal (Cropped)	X(1) = 0.0 X(2) > X(1) X(3) > X(2) X(4) > X(3) X(5) > X(4)	Y(1) = 0.0 Y(2) > 0.0 Y(3) > Y(2)
Delta (Cropped)	X(1) = 0.0 X(2) > 0.0 X(3) > X(2) X(4) > X(3) X(5) > X(4)	Y(1) = 0.0 Y(2) = 0.0 Y(3) > Y(2)

3. General Information (6I12 format)

Column	1-12	13-24	25-36	37-48	49-60	61-72
Name	NMACH	KF	NFREQ	LCOLL	LPUNCH	
Item	(1)	(2)	(3)	(4)	(5)	

- (1) NMACH Number of Mach numbers (max. 6)
- (2) KF Option to input either frequencies or reduced frequencies:  
KF = 0 frequencies  
KF = 1 reduced frequencies
- (3) NFREQ Number of frequencies or reduced frequencies at each Mach number (max. 10)
- (4) LCOLL Option to print aerodynamic and AIC collocation station coordinates:  
LCOLL = 0 do not print  
LCOLL = 1 print collocation station coordinates
- (5) LPUNCH Option to punch AIC matrix on cards:  
LPUNCH = 0 do not punch  
LPUNCH = 1 punch AIC matrix for wing only  
LPUNCH = 2 punch AIC matrix for control surface only  
LPUNCH = 3 punch individual AIC matrix for wing and control surface  
LPUNCH = 4 punch total AIC matrix of combined wing and control surface

The AIC matrix is punched by rows with a 1P6E12.5 format. Each row of the matrix begins on a new card.

4. General Information (6I12 format)

Column	1-12	13-24	25-36	37-48	49-60	61-72
Name	NWCX	NCCX	NIONCX	NIY	ISOLAT	
Item	(1)	(2)	(3)	(4)	(5)	

- (1) NWCX Number of chordwise collocation stations on wing ( $2 \leq NWCX \leq 10$ )
- (2) NCCX Number of chordwise collocation stations on control surface ( $2 \leq NCCX \leq 10$ )
- (3) NIONCX Factor for number of chordwise integration stations. Set NIONCX such that  $NIONCX \cdot NWCX$  and  $NIONCX \cdot NCCX$  are greater than 15 (but less than 40) to insure sufficient quadrature points for accurate integration of the Kernel function. If AIC's are desired for, say, the wing only, set NIONCX such that  $NIONCX \cdot NWCX$  is greater than 15 and set NCCX equal to 2 to minimize computing time.
- (4) NIY Number of spanwise collocation stations (wing and control surface)
- (5) ISOLAT Option to isolate wing and control surface:  
 ISOLAT = 0 interference and gap effects considered  
 ISOLAT = 1 surfaces are isolated. AIC's will be for individual surfaces with no coupling effects.

5. Mach Numbers (6E12.5 format)

Column	1-12	13-24	25-36	37-48	49-60	61-72
Name	FMACH(1)	FMACH(2)	FMACH(3)	FMACH(4)	FMACH(5)	FMACH(6)
Item	(1)	(2)	(3)	(4)	(5)	(6)

(1) FMACH (1) Mach number

(2) FMACH (2) Mach number

. . . . .  
 . . . . .  
 . . . . .

(NMACH) FMACH(NMACH) Mach number

NMACH values of Mach number must be input (see Part 3, Item 1). Mach numbers must be greater than zero and less than 0.95.

6. Frequencies or Reduced Frequencies (6E12.5 format)

Column	1-12	13-24	25-36	37-48	49-60	61-72
Name	FREQ(1)	FREQ(2)	FREQ(3)	FREQ(4)	FREQ(5)	FREQ(6)
Item	(1)	(2)	(3)	(4)	(5)	(6)

If KF=0, input NFREQ values of frequency (cps). If KF=1, input NFREQ values of reduced frequency ( $k_r = \omega b_r / U$  where  $b_r$  = semi-chord of wing root, U = free stream velocity, and  $\omega$  = oscillatory angular frequency in radians/sec). Frequencies (and reduced frequencies) may not be zero.

- (1) FREQ(1) f(cps) or  $k_r$
- (2) FREQ(2) "
- .
- .
- .
- .
- .
- .
- .

(NFREQ) FREQ(NFREQ)

For NFREQ > 6, continue input on new card.

7. Spanwise Location of AIC Stations on Wing (6E12.5 format)

Column	1-12	13-24	25-36	37-48	49-60	61-72
Name	YAIC(1,W)	YAIC(2,W)	YAIC(3,W)	YAIC(4,W)	YAIC(5,W)	YAIC(6,W)
Item	(1)	(2)	(3)	(4)	(5)	(6)

- (1) YAIC(1,W) Spanwise coordinate of first row of AIC collocation stations on wing.
- (2) YAIC(2,W) Spanwise coordinate of second row of AIC collocation stations on wing.
- .
- .
- .

(NIY) YAIC(NIY,W) Spanwise coordinate of last row of AIC collocation stations on wing

Collocation station rows are numbered from root to tip. For NIY > 6, continue input of YAIC (7,W) to YAIC(NIY,W) on new card(s).

8. Spanwise Location of AIC Stations on Control Surface (6E12.5 format)

Column	1-12	13-24	25-36	37-48	49-60	61-72
Name	YAIC(1,CS)	YAIC(2,CS)	YAIC(3,CS)	YAIC(4,CS)	YAIC(5,CS)	YAIC(6,CS)
Item	(1)	(2)	(3)	(4)	(5)	(6)

(1) YAIC(1,CS) Spanwise coordinate of first row of AIC collocation stations on control surface.

(2) YAIC(2,CS) ..... second.....

• • • • • •

(NIY) YAIC(NIY,CS) ..... last.....

Collocation station rows are numbered from root to tip. If NIY > 6, continue input of YAIC(7,CS) to YAIC(NIY,CS) on new card(s).

9. Streamwise Location of AIC Stations on Wing (6E12.5 format)

Column	1-12	13-24	25-36	37-48	49-60	61-72
Name	XATC(W,1,1)	XATC(W,1,2)	XATC(W,1,3)	...	...	...
Item	(1)	(2)	(3)	(4)	(5)	(6)

(1) XATC(W,1,1) Streamwise coordinate of first AIC collocation station in first row on wing.

(2) XATC(W,1,2) ..... second.....

• • • •

(NXWING\*NYWING)

XATC(W,NYWING,NXWING) ..... last.....last row....

Streamwise numbering sequence if from leading edge to trailing (see Figure 4.2). Continue input of values for each row immediately after the last value of the preceding row, do not begin input of each new row on new card.

10. Chordwise Location of AIC Stations on Control Surface (6E12.5 format)

Column	1-12	13-24	25-36	37-48	49-60	61-72
Name	XATC(CS,1,1)	XATC(CS,1,2)	XATC(CS,1,3)	...	...	...
Item	(1)	(2)	(3)	(4)	(5)	(6)

Procedure to input streamwise coordinate location of AIC stations on control surface is the same as wing.

### 3.0 Sample Problems

Three sample problems are given to demonstrate the operation of the subsonic AIC program and to illustrate the options available. Trapezoidal, cropped trapezoidal, and delta configurations are analyzed. Explanation of input parameters and computer listings of input data cards and computer output are given for each problem.

#### Sample Problem 1

A cropped Delta wing-rectangular control surface combination is analyzed for  $M = 0.5$  and  $k_r = 0.10$ . The planform geometry and AIC control station locations are shown in Figure 4.4. The dimensional unit used for length is feet for this particular case, therefore the acoustic velocity is entered with units of feet per second. NIONCX is set equal to 8 which makes NIONCX\*NWCX and NIONCX\*NCCX greater than 15, thereby insuring sufficient chordwise quadrature points for accurate chordwise integration of the kernel function.

The surfaces have 5 spanwise collocation stations and the wing has 3 chordwise stations while the control surface has 2 chordwise stations.

Summarized below are input parameters. A listing of the data input cards and computer output follows.

X(1) = 0.0'	X(2) = 1.0'	X(3) = 2.0'	X(4) = 3.0'	X(5) = 4.0'
Y(1) = 0.0'	Y(2) = 0.0'	Y(3) = 2.0'		
SOUND = 1116.87 ft/sec	(analysis for sea level)			
NMACH = 1	number of Mach numbers			
KF = 1	Input reduced frequency			
NFREQ = 1	Number of reduced frequencies			
LCOLL = 1	Print collocation station coordinates			
LPUNCH = 4	Punch total AIC matrix on cards			
NWCX = 3	Number of chordwise AIC collocation stations on wing			
NCCX = 2	Number of chordwise AIC collocation stations on control surface			
NIONCX = 8	Factor for determining number of chordwise integration stations			
NIY = 5	Number of spanwise AIC collocation stations			
ISOLAT = 0	Surfaces are not isolated			
FMACH(1) = 0.5	Mach number			
FREQ(1) = 0.1	Reduced frequency			

YAIC(1,W) = 0.2'  
YAIC(4,W) = 1.4'

YAIC(2,W) = 0.6'  
YAIC(5,W) = 1.8'

YAIC(3,W) = 1.0'

YAIC(1,CS) = 0.1'  
YAIC(4,CS) = 1.5'

YAIC(2,CS) = 0.5'  
YAIC(5,CS) = 1.9'

YAIC(3,CS) = 1.0'

XAIC(1,1,W) = 0.575'  
XAIC(2,1,W) = 0.725'  
XAIC(3,1,W) = 0.875'  
XAIC(4,1,W) = 1.025'  
XAIC(5,1,W) = 1.175'

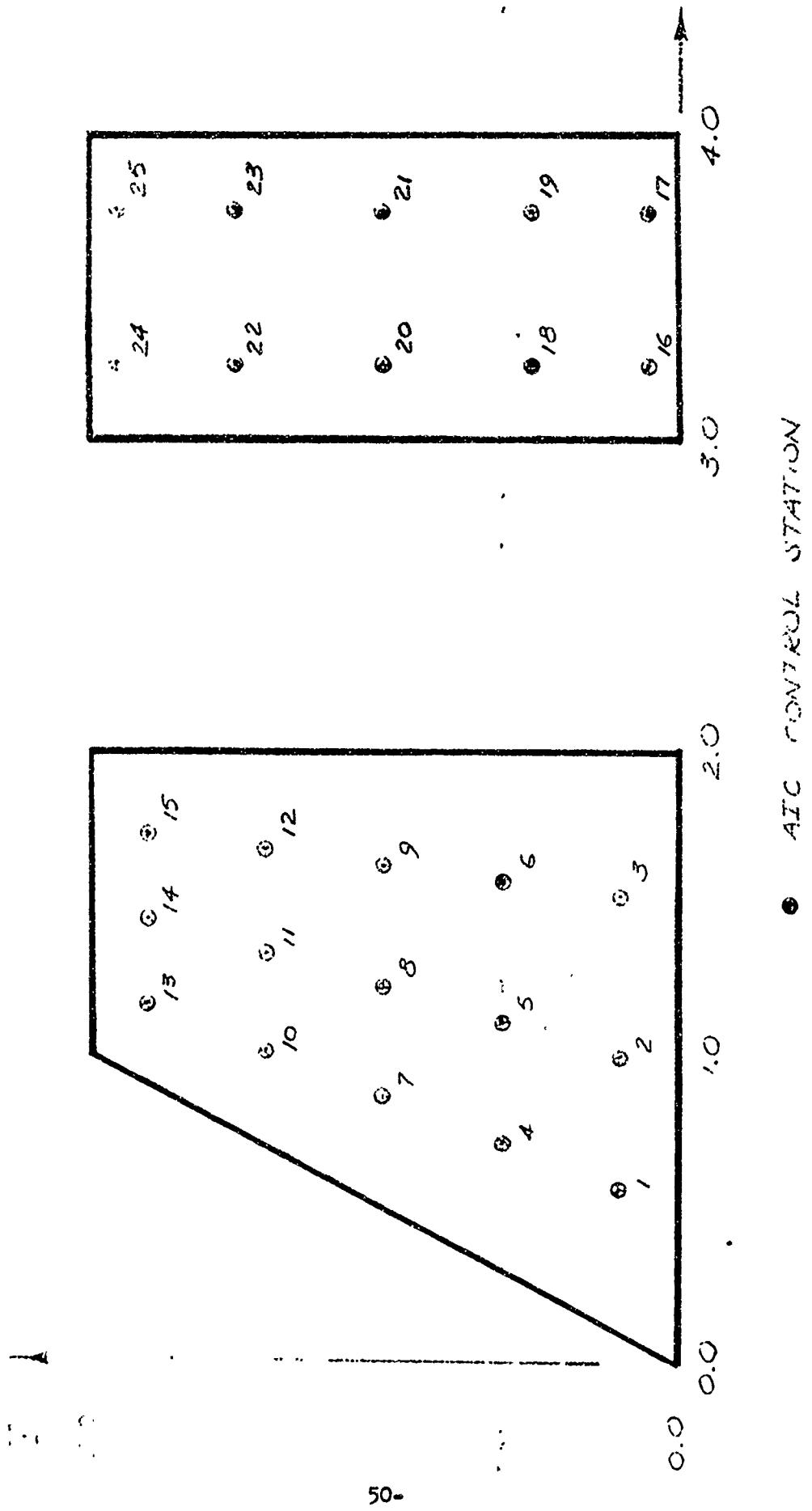
XAIC(1,2,W) = 1.050'  
XAIC(2,2,W) = 1.150'  
XAIC(3,2,W) = 1.250'  
XAIC(4,2,W) = 1.350'  
XAIC(5,2,W) = 1.450'

XAIC(1,3,W) = 1.525'  
XAIC(2,3,W) = 1.575'  
XAIC(3,3,W) = 1.625'  
XAIC(4,3,W) = 1.675'  
XAIC(5,3,W) = 1.725'

XAIC(1,1,CS) = 3.25'  
XAIC(2,1,CS) = 3.25'  
XAIC(3,1,CS) = 3.25'  
XAIC(4,1,CS) = 3.25'  
XAIC(5,1,CS) = 3.25'

XAIC(1,2,CS) = 3.75'  
XAIC(2,2,CS) = 3.75'  
XAIC(3,2,CS) = 3.75'  
XAIC(4,2,CS) = 3.75'  
XAIC(5,2,CS) = 3.75'

FIGURE 4.4 - Subsonic SAMPLE PROBLEM 1.



DATA CARD COLUMN NUMBER					
		MACH NO.		RED FREQ	
		X-WING		Y-TAIL	
0.4	1.0	2.0	3.0	1.800	-X-WING
0.6	0.0	0.0	1.160.81	1.900	X-WING
0.8	1	1	1	1.150	-Y-TAIL
1.0	3	8	1	1.350	X-WING
0.5				3.250	X-WING
0.1	0.600	1.000	1.400	3.250	X-TAIL
0.200	0.500	1.000	1.500	3.750	X-TAIL
0.100	0.500	1.000	1.600	3.750	X-TAIL
0.575	1.050	1.525	1.725	3.750	X-TAIL
0.875	1.250	1.875	2.075	3.750	X-TAIL
1.175	1.450	1.725	1.925	3.750	X-TAIL
2.250	3.750	5.250	3.750	3.750	X-TAIL
3.250	3.750	5.250	3.750	3.750	X-TAIL

FIGURE 4.5 - LISTING OF INPUT DATA CARDS FOR SUBSONIC SAMPLE PROBLEM 1.

## DUGGIES AIRCRAFT CO. SUBSONIC AIC PROGRAM

## FLIGHT CONDITIONS AND GEOMETRY

MACH NUMBER = 0.50000 SPEED OF SOUND = 1116.870 L/T RHO=0.1000000E 01

	L/ING	TAIL
L.E. STATION (L)	0'	3.000
ROOT CHORD (L)	2.000	1.000
L.E. SPAN (L)	0'	2.000
T.E. SPAN (L)	2.000	2.000
TIP CHORD (L)	1.000	1.000
TOTAL AREA (L*L)	6.000	4.000
SPAN COLL. STA.	9	5
CHORD COLL. STA.	3	2
CHORD INTG. STA.	24	16
SPAN PRES Holes	5	5
CHORD PRES Holes	3	?

JAMES AIRCRAFT CO. SURFACE AIC PROGRAM (CONT-D)

UNSTEADY AERO COLLOCATION STATION COORDINATES ON THE WING

S STA NO	YC	XC VALUES--
1	9.	0.481607E 00
2	3.618034E 00	0.716212E 00
3	9.117557E 01	0.927852E 00
4	3.161803E J1	3.109581E 01
5	3.190211E 01	3.120365E 01

INTEGRATION STATION COORDINATES ON THE WING

S STA NO	Y1	X1 VALUES--
1	0.312669E 00	0.158328E 00
2	9.907981E 00	0.455579E 00
3	0.141421E 01	0.708435E 00
4	9.178201E 01	0.892146E 00
5	1.197533E J1	1.958728E 00

1	0.146254E 01	0.199795E 01
2	0.154558E 01	0.19826E 01
3	0.16049E 01	0.19855E 01
4	0.167995E 01	0.19876E 01
5	0.171812E 01	0.19892E 01

1	0.376329E 00	0.458502E 00
2	0.67866E 00	0.873101E 00
3	0.96026E 00	0.105499E 01
4	0.122533E 01	0.134049E 01
5	0.165294E 01	0.174038E 01

1	0.191263E 01	0.196985E 01
2	0.466245E 00	0.493371E 00
3	0.639394E 00	0.707303E 00
4	0.96026E 00	0.105499E 01
5	0.135037E 01	0.144694E 01

1	0.176896E 01	0.178228E 01
2	0.194351E 01	0.197472E 01
3	0.190053E 01	0.197472E 01
4	0.719028E 00	0.740039E 00
5	0.861319E 00	0.918947E 00

1	0.113029E 01	0.120971E 01
2	0.145673E 01	0.153749E 01
3	0.176661E 01	0.181793E 01
4	0.195276E 01	0.197886E 01
5	0.199948E 01	0.198167E 01

1	0.904232E 00	0.919255E 00
2	0.102328E 01	0.10271E 01
3	0.125400E 01	0.132212E 01
4	0.153400F 01	0.160327E 01
5	0.179123E 01	0.184338E 01

1	0.199948E 01	0.198167E 01
2	0.203394E 00	0.247720E 00
3	0.458502E 00	0.550850E 00
4	0.673101E 00	0.98705E 00
5	0.105499E 01	0.115277E 01

1	0.144694E 01	0.153989E 01
2	0.178228E 01	0.1864649E 01
3	0.197472E 01	0.199365E 01
4	0.740039E 00	0.771125E 00
5	0.918947E 00	0.933710E 00

1	0.129148E 01	0.129148E 01
2	0.153749E 01	0.161522E 01
3	0.181793E 01	0.187162E 01
4	0.197886E 01	0.199469E 01
5	0.198167E 01	0.199545E 01

1	0.10271E 01	0.102827E 01
2	0.132212E 01	0.139226E 01
3	0.160327E 01	0.166995E 01
4	0.184338E 01	0.186988E 01
5	0.198167E 01	0.199545E 01

1	0.11347E 01	0.103781E 01
2	0.151043E 01	0.120426E 01
3	0.15904F 01	0.144524E 01
4	0.157663F 01	0.169673F 01
5	0.160943E 01	0.169948E 01

1	0.199345E 01	0.199584E 01
2	0.198167E 01	0.198167E 01
3	0.197886E 01	0.197886E 01
4	0.197472E 01	0.197472E 01
5	0.198167E 01	0.198167E 01

## UNSTEADY AERO COLLOCATION STATION COORDINATES ON THE TAIL

S STA NO	YC	XC VALUES--	XI VALUES--
1	0.	0.347621E 01 0.347621E 01 0.347621E 01 0.347621E 01 0.347621E 01	0.399774E 01 0.399774E 01 0.399774E 01 0.399774E 01 0.399774E 01
2	0.618034E 00	0.347621E 01 0.347621E 01 0.347621E 01 0.347621E 01 0.347621E 01	0.399774E 01 0.399774E 01 0.399774E 01 0.399774E 01 0.399774E 01
3	0.117557E 01	0.347621E 01 0.347621E 01 0.347621E 01 0.347621E 01 0.347621E 01	0.399774E 01 0.399774E 01 0.399774E 01 0.399774E 01 0.399774E 01
4	0.1616803E 01	0.347621E 01 0.347621E 01 0.347621E 01 0.347621E 01 0.347621E 01	0.399774E 01 0.399774E 01 0.399774E 01 0.399774E 01 0.399774E 01
5	0.190211E 01	0.347621E 01 0.347621E 01 0.347621E 01 0.347621E 01 0.347621E 01	0.399774E 01 0.399774E 01 0.399774E 01 0.399774E 01 0.399774E 01
INTEGRATION STATION COORDINATES ON THE TAIL			
S STA NO	YI	XC VALUES--	XI VALUES--
1	0.312869E 00	0.300226E 01 0.317257E 01 0.352379E 01 0.386187E 01	0.302025E 01 0.325000E 01 0.361788E 01 0.392063E 01
2	0.907981E 00	0.300226E 01 0.317257E 01 0.352379E 01 0.386187E 01	0.302025E 01 0.325000E 01 0.361788E 01 0.392063E 01
3	0.141421E 01	0.300226E 01 0.317257E 01 0.352379E 01 0.386187E 01	0.302025E 01 0.325000E 01 0.361788E 01 0.392063E 01
4	0.178201E 01	0.300226E 01 0.317257E 01 0.352379E 01 0.386187E 01	0.302025E 01 0.325000E 01 0.361788E 01 0.392063E 01
5	0.197538E 01	0.300226E 01 0.317257E 01 0.352379E 01 0.386187E 01	0.302025E 01 0.325000E 01 0.361788E 01 0.392063E 01

HUGHES AIRCRAFT CO. SURSONIC ATC PROGRAM (CONT'D)

AIG COLLOCATION STATION COORDINATES ON THE WING

Y AIC	X AIC VALUES--
0.200000E 00	0.575000E 00
0.600000E 00	0.725000E 00
0.100000E 01	0.875000E 00
0.140000E 01	0.102500E 01
0.180000E 01	0.117500E 01

	0.105000E 01	0.152500E 01	
	0.115000E 01	0.157500E 01	
	0.125000E 01	0.162500E 01	
	0.135000E 01	0.167500E 01	
	0.145000E 01	0.172500E 01	

HUGHES AIRCRAFT CO. SUBSONIC AIC PROGRAM (CONT-D)

AIC COLLOCATION STATION COORDINATES ON THE TAIL

XAIC VALUES--

0.100000E 00	0.325000E 01	0.375000E 01
0.500000E 00	0.325000E 01	0.375000E 01
0.100000E 01	0.325000E 01	0.375000E 01
0.150000E 01	0.325000E 01	0.375000E 01
0.190000E 01	0.325000E 01	0.375000E 01

## HUGHES AIRCRAFT CO. SUBSONIC AIC PROGRAM (CONT-D)

OSCILLATORY FREQUENCY (CPS) 8.88777E 00  
 REFERENCE CHORD 1.00000E 00  
 REDUCED FREQUENCY (REF. CHORD) 1.00000E-01  
 REDUCED VELOCITY (REF. CHORD) 1.00000E 01  
 FREE STREAM MACH NUMBER 5.00000E-01  
 FREE STREAM VELOCITY 5.58435E 02  
 DENSITY 1.00  
 DYNAMIC PRESSURE (1/2\*RH0\*VEL\*\*2) 1.55925E 05

## AERODYNAMIC INFLUENCE COEFFICIENTS

	RL	IM	RL	IM	RL	IM	RL	IM	RL	IM
)	ROW = 1									
)	1.9737E 03	-6.78820E 01	-3.4937E 03	9.1008E 01	1.5227E 03	-4.3777E 01	-3.8526E 03	1.1895E 02	6.9772E 03	-1.4104E 02
)	-2.7240E 03	7.0267E 01	2.7537E 03	-8.3180E 01	-4.6233E 03	1.0535E 02	-5.5529E 03	-7.9280E 02	1.6308E 01	
)	1.2850E 03	-8.0521E 00	-4.7241E 02	2.0849E 00	3.5502E 01	-2.1366E 00	2.9963E 01	1.6790E 00	-5.489E 00	-6.0153E-01
)	-57-	2.8760E 00	-2.8647E 00	-3.4308E 01	2.8840E 00	-2.1446E 01	-2.8742E 00	-3.5066E-01	3.920E 00	2.5789E-01
)	-3.1778E 00	-4.1736E-01	1.8022E 00	1.4465E-01	-1.7943E 00	-2.3558E-01	4.7363E-01	9.3344E-03	-4.7348E-01	-2.9053E-02
)	ROW = 2	2.5023E 10	1.6737E 03	5.5166E 01	-9.4930E 02	-5.8917E 01	1.5732E 03	5.9870E-01	-3.1097E 03	-1.0717E 02
)	1.5349E 03	1.0498E 02	-1.1665E 03	-3.4436E-01	2.3154E 03	6.9444E 01	-1.1480E 03	-6.6825E 01	3.2028E 02	6.6815E-01
)	-6.0623E 02	-1.6573E 01	2.8581E 02	1.4769E 01	-8.4283E 00	6.3100E 01	8.3867E 00	-2.0749E 00	7.6526E-03	1.6746E 00
)	4.7742E-01	-2.5529E-01	-4.9027E-01	2.3146E-01	5.5339E-01	-2.7463E-01	-5.6713E-01	2.4702E-01	7.6444E-01	-3.58871E-01
)	-7.6133E-01	3.0536E-01	5.3086E-01	-2.0854E-01	-5.41244E-01	1.8206E-01	1.5747E-01	-4.6454E-02	-1.59977E-01	3.8874E-02
)	ROW = 3									
)	-1.8133E 03	5.0187E 01	3.6031E 03	-5.5244E 00	-1.7894E 03	-4.3430E 01	3.7556E 03	-7.3264E 01	6.8783E 03	-2.6052E 01
)	3.1664E 03	9.1341E 01	-2.6049E 03	4.5166E 01	5.0399E 03	1.5665E 01	-2.4305E 03	-5.8232E 01	7.4842E 02	-6.6297E 00
)	-1.3071E 03	-1.6990E 01	6.3851E 02	2.0048E 01	-3.5167E 01	3.9273E-01	4.4976E 01	-8.1279E 01	-9.8485E 00	1.1417E 00
)	-8.6234E-01	-3.8770E-01	8.4218E-01	4.3076E-01	-7.7805E-01	-4.18736E-01	7.5660E-01	4.8766E-01	-6.83341E-01	-5.2082E-01
)	6.5679E-01	5.9498E-01	-2.6805E-01	-3.2426E-01	2.52428E-01	3.3772E-01	-4.4849E-02	-6.9013E-02	4.1348E-02	7.1216E-02
)	ROW = 4									
)	1.6134E 03	-5.6083E 01	-2.8560E 03	7.3909E 02	1.2448E 03	-3.5421E 01	-3.2326E 03	9.9479E 01	5.9245E 03	-1.1766E 02
)	-2.2921E 03	5.8317E 01	2.3850E 03	-7.1690E 01	-3.9881E 03	9.0136E 01	1.6150E 03	-4.7442E 01	1.3935E 02	
)	-1.0850E 03	-6.5647E 00	-4.0628E 02	1.4960E 00	2.7291E 01	-1.7299E 00	-1.6162E 01	1.3926E 00	-9.1375E 01	
)	2.5517E 00	9.7700E-02	-2.5461E 00	-2.1806E 01	2.6010E 00	9.7705E-02	-2.99528E 00	-2.2731E-01	2.9661E 00	1.3229E-01
)	-2.9549E 00	-2.51113E-01	1.7237E 00	5.2876E-02	-1.7204E 00	-1.3899E-01	4.6304E-01	-1.6912E-01	-4.6360E-01	-6.0257E-03
)	ROW = 5									
)	-6.7228E 02	2.1321E 00	1.3666E 03	4.4769E 01	-7.9350E 02	-4.7923E 01	1.3179E 03	5.5572E-01	-2.6054E 03	-1.9287E 01
)	1.2862E 03	8.7620E 11	-1.0127E 03	-4.2131E-01	2.0130E 03	6.0463E 01	-9.9632E 02	-5.9552E 01	2.7126E 02	5.4856E-01
)	-5.1250E 02	-1.3812E 11	2.4093E 02	1.2223E 01	-6.6433E 00	9.3766E-01	6.24148E 00	-7.7698E 00	4.1586E-01	1.4537E 00
)	4.3617E-01	-2.1397E-01	-4.6622E-01	1.9219E 01	5.0314E-01	-7.3009E-01	-5.14686E-01	2.8662E-01	6.9002E-01	-7.8871E-01
)	-7.0424E-01	2.5128E-01	4.7629E-01	-1.7567E-01	-4.84688E-01	4.9141R-01	1.4043J-01	-2.8611R-02	-1.64274E-01	3.1844E-02

ROW = 6	-1.4817E-03	4.1122E-01	2.9491E-03	-4.8952E-00	-1.4621F-03	-8.5217E-01	2.9799E-03	-6.3169E-01	-5.7635E-03	-7.5341E-00
	-2.7807E-03	7.6633E-01	2.6000E-03	4.2167E-01	4.3683E-03	5.1148E-01	6.3798E-02	5.1148E-01	6.3798E-02	5.2915E-01
	-1.1796E-03	-1.4543E-01	5.4130E-01	-2.8495E-01	2.7169E-01	3.5201E-01	-4.7572E-01	3.5201E-01	-4.7572E-01	3.6994E-01
	-6.6757E-01	-3.1363E-01	6.5130E-01	3.4696E-01	-6.0738E-01	-6.3954E-01	5.6002E-01	3.6994E-01	5.6002E-01	-4.2277E-01
	5.2533E-01	4.5012E-01	-2.2341E-01	-2.6196E-01	2.1002F-01	2.7314E-01	-3.8056E-02	-3.8056E-02	3.6132E-02	5.5789E-02
ROW = 7	-1.0435E-03	-3.76103E-01	-1.8449E-03	4.7281E-01	8.0280E-02	-2.12694E-01	-2.1633E-03	6.63322E-01	5.7006E-03	-7.8281E-01
	-1.5398E-03	3.8571E-01	1.6329E-03	-4.9044E-01	-2.7279F-03	6.1132E-01	1.0938E-03	-4.51593E-02	-5.12556E-01	-5.12556E-01
	-6.6756E-02	-2.94102E-00	-2.52214E-02	-3.99639E-02	1.3024F-01	-6.6098E-02	-2.1152E-02	7.3019E-01	-1.4266E-01	-1.4266E-01
	-2.0245E-00	-6.10269E-02	-2.0269E-00	-7.1741E-02	-1.5345F-00	-4.6373E-03	4.26673E-01	-4.3219E-02	5.51515E-01	-8.8515E-02
	-2.5157E-00	-3.6908E-02	-1.5345F-00	-7.1741E-02	-1.5345F-00	-4.6373E-03	4.26673E-01	-4.3219E-02	5.51515E-01	-8.8515E-02
ROW = 8	-4.3509E-02	1.4336E-00	8.0464E-02	2.8799E-01	-4.4933E-02	-7.3904E-01	8.7995E-02	-1.2660E-01	-1.7394E-03	-5.9255E-01
	-8.5698E-02	5.8260E-01	-6.9736E-02	-4.3407E-01	1.3844E-03	4.1943E-01	-6.8644E-02	-4.1113E-01	1.6062E-02	2.3373E-01
	-2.9819E-02	-7.9195E-00	1.3811E-02	6.7759E-00	-5.0339E-00	3.5630E-01	6.4900E-00	-4.1353E-01	1.3836E-00	5.61463E-01
	-3.6329E-01	-1.4989E-01	-3.7080E-01	1.3176E-01	4.1520F-01	-2.6241E-01	-4.2323E-01	5.4170E-01	5.6246E-01	-2.0233E-01
	-5.7271E-01	1.7423E-01	3.8535E-01	-1.2501E-01	-3.9155E-01	1.0586E-01	1.1392E-01	-2.7930E-02	-1.1530E-01	2.2323E-02
ROW = 9	-9.9414E-02	2.66685E-01	1.90435E-03	-3.38225E-00	9.4673F-02	-2.2648E-01	1.99075E-03	-4.2275E-01	-3.8446E-03	-1.4327E-01
	-1.8566E-03	5.0937E-01	-1.5538E-03	2.8599E-01	3.0027E-03	2.1093E-01	-1.4468E-03	-3.5722E-01	8.8339E-02	-3.1044E-03
	-7.0270E-02	-9.0221E-00	3.1946E-02	1.0096E-01	1.7516E-01	1.8686E-01	2.3346E-01	9.9989E-01	6.8338E-00	5.61463E-01
	-3.8227E-01	-2.0151E-01	3.7229E-01	2.2062E-01	-3.5056F-01	-2.1873E-01	3.3943E-01	2.3626E-01	8.2559E-01	-2.7343E-01
	-3.1150E-01	2.8962E-01	-1.3998E-01	-1.6899E-01	1.3132F-01	2.7600E-01	-2.5367E-02	-3.3956E-02	5.5293E-02	-2.3676E-02
ROW = 10	-7.54317E-06	-6.1884E-02	2.4578E-01	4.7794E-02	-1.9146F-01	-6.3614E-01	-1.4059E-01	1.4373E-01	3.2395E-01	-2.5621E-01
	-1.2314E-01	-8.7337E-02	2.7975E-01	-1.2123E-00	-2.5780E-01	1.6042E-00	-1.7651E-00	1.4930E-01	7.2277E-01	-2.2839E-00
	-1.71231E-00	3.3912E-01	-1.9410E-01	-2.0369E-01	5.7082E-01	-5.7082E-01	-2.6064E-01	8.3750E-01	5.6504E-00	-6.9802E-01
	-1.12317E-00	-3.71352E-01	-1.2471E-00	2.5205E-01	1.3504E-00	-3.3689E-01	-3.3689E-01	2.1559E-01	1.7330E-00	-4.3359E-01
	-1.75567E-00	3.3691E-01	1.1537E-00	-2.74395E-01	-1.1671F-00	2.1698E-01	3.4234E-01	-8.0369E-02	6.3790E-02	-6.3790E-02
ROW = 11	-4.9449E-00	-1.54437E-01	1.1752E-01	8.4297E-01	-6.7921F-00	-7.6690E-01	1.4399E-00	-1.0508E-01	-2.29935E-00	1.5682E-01
	-6.5625E-01	-9.3742E-02	-2.2368E-01	-2.5830E-01	4.6977F-01	1.20117E-00	-1.4579E-01	1.9059E-01	-4.4554E-01	-9.62072E-01
	9.1852E-01	3.0211E-00	-4.7222E-01	-2.8444E-01	-1.6339F-01	1.30117E-00	-3.5733E-01	9.1995E-01	-1.9382E-01	-8.0725E-01
	2.6602E-01	-4.2761E-02	-2.6101E-02	2.94835E-01	2.8889E-01	-4.6066E-02	-2.9114E-01	3.0876E-02	3.4448E-01	-5.9079E-02
	-3.6719E-01	4.0939E-02	2.3722E-01	-3.83858E-02	-2.3908F-01	2.6943E-02	6.9658E-02	-1.1057E-02	-7.0192E-02	7.5797E-03
ROW = 12	-6.6534E-00	-3.0121E-02	1.4069E-01	6.9090E-01	-7.3986F-00	-6.9651E-01	6.9487E-00	-2.4946E-01	-1.2204E-01	3.3249E-01
	-5.6623E-00	-1.2111E-01	-4.2377E-01	4.7897E-01	8.3673F-01	1.3473E-00	-4.1269E-01	1.7846E-00	-8.1562E-01	1.7759E-00
	1.67111E-02	1.6882E-00	-7.2808E-01	-2.4446E-01	-8.8789E-01	4.3094E-01	-6.3035E-01	5.5318E-01	-8.1582E-01	-7.5888E-01
	6.6187E-02	-1.1698E-02	-6.7672E-02	6.39446E-03	6.3720F-02	-1.2740E-01	-6.3899E-02	9.5838E-02	5.9381E-02	-1.6652E-02
	-6.0207E-02	1.3690E-02	2.64439E-02	-1.0446E-02	-2.7000F-02	4.1219E-03	6.4941E-03	-2.7732E-03	-6.6474E-03	2.4462E-03
ROW = 13	-4.8438E-03	1.75190E-02	8.0225E-03	-1.9702E-00	-3.5518F-03	8.9764E-01	9.30315E-03	-2.3745E-02	-1.58841E-04	3.3933E-02
	-6.5677E-03	-1.46882E-02	-6.6640E-03	1.9836E-02	1.1233F-04	-2.4766E-02	-4.5740E-03	1.2704E-02	1.9162E-03	-4.0759E-01
	-3.0149E-03	2.1190E-01	1.2012E-03	-6.8726E-00	-4.3178F-00	3.0200E-00	-4.3865E-01	8.2333E-01	4.8303E-01	-7.5014E-01
	-1.4583E-00	-1.4415E-00	1.0849E-00	1.4994E-00	-9.9173F-01	-4.7564E-00	8.13518E-01	1.5994E-00	-5.30416E-01	-1.9154E-00
	4.5556E-01	1.9421E-01	4.7373E-03	-1.8130E-00	-6.3852F-02	1.1808E-01	7.9348E-02	-2.5566E-01	-9.2085E-02	2.5144E-01
ROW = 14	-1.8156E-03	-7.5304E-26	-3.6787E-03	-1.1565E-02	1.5619E-03	1.2537E-02	-3.81335E-03	-1.3574E-00	7.54741E-05	2.5874E-02
	-3.7299E-03	-2.8395E-02	2.0856E-03	4.3072E-01	-5.9167E-03	-1.6239E-02	2.7282E-03	1.6089E-02	-7.9772E-02	-1.7759E-00
	1.5224E-03	4.1505F-02	-7.2435E-02	-3.7357E-01	-2.9587E-01	1.5331E-01	-1.5331E-01	7.5778E-01	7.6672E-00	-5.6082E-01
	1.60606E-01	3.6421E-01	-1.4139E-01	-3.6220E-01	6.8000E-01	6.8000E-01	-3.8377E-01	-4.8532E-02	-3.8722E-01	-1.2547E-01

ROW =1	1.4960E-01	-4.7150E-01	-1.9455E-01	2.8936E-01	2.0911E-01	-2.7969E-01	-6.6712E-02	9.0569E-02	6.9239E-02	-4.7109E-02	
ROW =15	4.0390E-03	-1.1450E-02	-8.0169E-03	1.9959E-01	3.9772E-03	9.0880E-01	-8.6044E-03	1.8186E-02	1.6645E-04	4.4711E-01	
)	-8.0386E-03	-2.2239E-02	6.2533E-03	-1.1627E-02	-1.2065E-04	-6.3097E-01	5.8106E-05	1.3906E-02	-1.3426E-03	1.6617E-01	
)	3.4283E-03	4.1152E-01	-1.5853E-03	-4.9407E-01	-1.2504E-01	9.5265E-01	8.8195E-01	2.3810E-00	-7.5581E-01	4.6680E-00	
)	-1.9360E-00	7.2871E-01	-1.6933E-05	-8.2541E-02	1.7871E-00	7.9066E-01	-1.7466E-00	-8.8041E-01	1.6943E-01	9.9026E-01	
)	-1.6437E-00	-1.3750E-00	7.8592E-01	6.1426E-01	-7.5455E-01	-4.5356E-01	1.6842E-01	1.1769E-01	-1.6248E-01	-1.2602E-01	
ROW =16	4.9351E-02	-4.71937E-01	-1.3211E-03	1.0776E-02	8.29452E-02	-8.0041E-01	-9.8790E-02	8.1179E-01	2.43350E-03	-2.0705E-02	
)	-1.6506E-03	9.71957E-01	7.59336E-02	-6.8511E-01	-2.0303E-03	1.7752E-02	1.2731E-03	-8.9871E-01	-2.2279E-02	1.8329E-01	
)	5.9091E-02	-4.4446E-01	-3.6859E-02	2.3411E-01	5.0370E-00	-3.1670E-01	-1.1328E-01	1.0358E-01	-6.2970E-01		
)	2.6160E-02	3.74669E-00	-2.6131E-02	-1.6534E-01	-4.0131E-02	-6.1960E-00	4.0050E-02	2.6229E-01	2.4349E-02	3.6910E-00	
)	-2.8296E-02	-1.7840E-01	-1.0703E-02	-1.6109E-00	1.0680E-02	7.1528E-00	2.2973E-01	2.5863E-01	-2.2981E-02	-1.4035E-00	
ROW =17	6.7398E-01	-1.79677E-31	-3.0549E-00	6.6494E-01	2.1961E-00	-4.2336E-01	8.7348E-00	-1.6910E-00	-2.3657E-01	4.5021E-00	
)	-1.4980E-01	-2.05504E-00	1.5270E-00	5.5941E-00	2.7914E-00	2.0521E-00	3.2698E-00	-1.1251E-00	5.4196E-00	-9.7271E-01	
)	-1.5573E-01	2.56889E-00	9.9815E-00	-1.5760E-00	-3.2647E-00	1.1465E-01	8.3732E-00	-2.0668E-01	-5.1096E-00	4.0635E-02	
)	9.2299E-01	2.53303E-01	-2.8589E-01	-2.5350E-01	5.9940E-00	-4.0362E-01	-7.0050E-00	4.0094E-01	3.6944E-00	2.6850E-01	
)	-3.0160E-00	-2.7035E-01	2.5286E-00	-1.0883E-01	-2.8006E-00	1.0757E-01	-6.7581E-01	2.3514E-00	7.3381E-01	-2.3177E-00	
ROW =18	6.2240E-02	-9.529746E-01	-1.6665E-03	1.3620E-02	1.0664E-03	-6.3370E-01	-1.2736E-03	1.0442E-02	3.3982E-03	-2.06627E-02	
)	-7.1286E-03	1.72589E-02	1.01519E-03	-9.1949E-01	-2.7143E-03	8.3707E-02	1.7023E-03	-1.0704E-02	-2.9235E-02	2.3624E-01	
)	-2.3725E-02	5.56664E-01	7.62279E-02	2.8691E-01	6.7064E-01	-5.6873E-01	-1.6159E-01	1.8562E-01	1.4955E-01	-1.1572E-00	
)	3.3216E-02	4.33487E-01	-3.3195E-02	-2.0228E-01	5.2143E-02	-8.0973E-01	5.2937E-02	3.4123E-01	3.6743E-02	5.0179E-00	
)	-3.8633E-02	-2.43366E-01	-1.4196E-02	-2.4361E-00	1.4165E-00	0.5215E-00	3.1284E-01	3.4523E-01	-3.1227E-01	-1.9066E-00	
ROW =19	4.9964E-01	-2.79702E-01	-2.3430E-00	9.5633E-00	1.8642E-01	1.8642E-00	-6.3571E-01	1.20659E-01	-2.2692E-00	-3.2741E-01	6.0430E-00
)	2.0734E-01	-3.64127E-00	2.9953E-00	-4.4185E-02	8.9911E-00	3.9627E-01	6.0181E-00	-1.9679E-01	5.5961E-00	-1.4296E-00	
)	-2.3725E-01	3.94746E-00	1.52404E-01	-2.3044E-01	4.0579E-00	9.8679E-02	1.0309E-01	-5.2290E-01	-5.2534E-00	-3.7174E-02	
)	1.0279E-00	3.2111E-01	-2.1013E-01	-3.2143E-01	8.1021E-00	-8.2559E-01	9.4224E-00	5.2159E-01	5.7024E-00	3.6573E-01	
)	-4.6342E-00	-3.6863E-01	3.8983E-00	-1.4711E-01	-4.2610E-00	1.4137E-01	-7.9375E-01	3.1770E-01	8.7160E-01	-3.1374E-00	
ROW =20	4.1581E-02	-3.616167E-01	-1.1249E-03	9.3407E-01	7.0669E-02	-4.3764E-01	-6.9241E-02	7.2711E-01	2.3907E-03	-1.8526E-02	
)	-1.4910E-03	8.73337E-01	7.4506E-02	-6.8334E-01	-1.9935E-03	1.7749E-02	1.2506E-03	-9.0338E-01	-1.7742E-02	1.2982E-01	
)	4.6881E-02	-3.2098E-01	-2.9131E-02	1.5150E-01	7.1522E-00	-1.2255E-00	-2.0713E-01	3.7760E-01	1.3669E-01	-2.3740E-00	
)	2.9272E-02	2.8563E-00	-2.2681E-02	-1.4198E-01	3.6916E-02	-9.8523E-00	3.6840E-02	2.4228E-01	2.4228E-01	-3.2441E-01	
)	-2.9621E-02	-1.93528E-01	-0.8517E-01	-1.65593E-00	8.8313E-01	6.0772E-00	2.3486E-01	-2.3486E-01	-2.3440E-01	-1.4048E-01	
ROW =21	-1.4660E-01	-3.14555E-01	-5.2318E-01	1.1249E-03	9.3407E-01	7.0669E-02	-4.3764E-01	-6.9241E-02	7.2711E-01	2.3907E-03	-1.8526E-02
)	-1.6481E-01	-2.51668E-00	4.1684E-00	-3.3627E-01	-1.2104E-01	1.4137E-00	7.9558E-00	-6.3592E-01	6.0431E-00	-1.3779E-01	
)	-2.5007E-01	3.8045E-00	1.6004E-01	-2.2022E-00	-1.4079E-00	-1.4336E-01	3.1825E-00	5.1625E-01	-1.7698E-00	-3.8261E-01	
)	7.9284E-01	2.1910E-02	-2.4273E-01	-2.1940E-01	6.4420E-00	-8.7356E-01	-7.3774E-00	3.7064E-01	6.1088E-00	2.7644E-01	
)	-5.4050E-00	-2.79350E-01	4.43347E-00	-9.4668E-00	-4.66684E-00	9.2469E-00	-1.18795E-01	2.2890E-00	1.75348E-01	-2.2831E-00	
ROW =22	-1.1293E-02	7.03593E-00	2.9914E-02	-4.6859E-01	-1.8651E-01	6.3355E-00	2.6300E-02	-2.2614E-01	-7.0340E-02	5.8168E-01	
)	4.4127E-02	-2.9059E-01	-1.7956E-02	1.3592E-01	4.7625F-02	-3.3906E-01	-2.9711E-02	1.5939E-01	1.0969E-02	-1.1896E-01	
)	-2.9565E-02	3.1423E-01	1.3628E-02	-1.7138E-01	2.5128E-01	-3.9233E-00	-1.0348E-01	1.0922E-01	4.5102E-01	-4.5624E-00	
)	-5.6761E-01	-1.1098E-00	5.0629E-01	3.9429E-01	1.1045E-02	1.1624E-00	-1.1624E-02	-7.1946E-01	-5.2904E-01	-1.1624E-01	
)	5.2770E-01	3.8C30E-02	5.03508E-01	5.0507E-01	-5.8215E-01	-3.6054E-00	7.6305E-01	-5.3144E-02	-7.6941E-01	1.9901E-02	
ROW =23	3.6086E-00	-7.03852E-01	-1.0263E-01	2.2322E-00	6.6306E-00	-1.0202E-00	-4.57768E-01	1.0048E-02	5.0340E-02	5.8168E-01	
)	-5.1940E-01	1.2633E-01	4.40558E-01	-9.1643E-01	-1.2374E-01	2.5227E-00	5.0068E-00	-1.5049E-01	3.5843E-00	-5.2173E-01	
)	-1.0131E-01	1.49223E-00	6.3634E-00	-8.74469E-01	4.3144E-00	-5.4418E-01	-1.1917E-01	3.9138E-00	7.4138E-00	-8.7225E-01	

2	4373E	00	-6.73885E	00	-2.56887E	00	5.96768E	00	1.51378E	00	-1.0868E	00	-1.0447E	00	-5.0648E	00
-3	.7917E	00	5.7825E	00	2.8869E	00	5.0320E	00	-2.7547E	00	-3.1762E	00	-1.2694E	00	-1.2159E	-01
Row =24																
-1	.3938E	03	1.9189E	02	3.4917E	03	-2.5788E	02	-2.1879E	03	1.1464E	02	2.9303E	03	-2.4337E	02
-4	.9030E	03	-2.9571E	02	-2.2298E	03	1.0412E	02	5.9487E	03	-4.9910E	02	-6.4931E	02	6.1998E	02
-6	.8066E	03	1.5469E	02	1.1292E	03	-2.0189E	02	1.5511E	02	-5.0119E	01	-6.2079E	01	-6.0612E	01
-6	.9467E	02	-1.0211E	01	4.9329E	02	4.4889E	01	1.2467E	03	1.1046E	01	-1.2463E	03	-6.1678E	01
6	.1539E	02	5.2787E	01	3.4581E	02	4.9497E	00	-3.4534E	02	-2.2210E	01	-5.7624E	01	5.7584E	01
Row =25																
1	.7523E	01	-2.75877E	00	-6.7038E	01	6.7689E	00	2.9615E	01	-8.4344E	00	-2.1443E	01	4.1273E	00
-3	.5914E	01	6.0922E	00	7.0994E	00	-2.5525E	00	-1.9117E	01	6.8158E	00	1.2086E	01	-6.0813E	00
2	.9320E	01	-3.72024E	00	1.72045E	01	1.3039E	01	-1.3039E	01	-3.5520E	01	3.8354E	01	-1.4359E	00
-2	.9596E	00	-6.79510E	01	-1.0697E	01	6.9065E	01	-6.7407E	00	1.2310E	00	-1.2281E	02	-2.2663E	01
-1	.7855E	00	7.7931E	01	-1.8376E	00	3.3712E	01	2.6840E	00	-3.3621E	01	3.5945E	00	-3.3280E	00

### Sample Problem 2

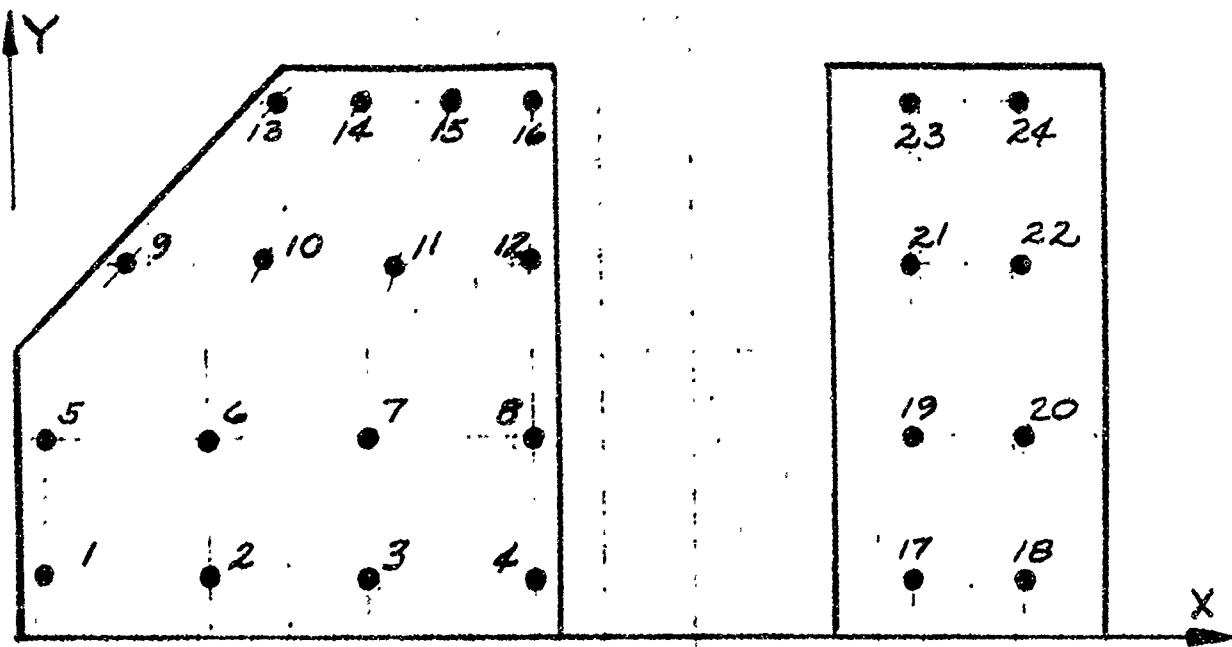
A cropped trapezoidal wing is analyzed for  $M = 0.5$  and  $k_r = 0.10$ . Since the subsonic AIC program requires a control surface, a dummy surface is added with a minimal number of chordwise collocation stations (2) to minimize computing time. The surfaces are isolated and the option LPUNCH is input as 1 to punch the AIC matrix for the wing only. The wing has 4 chordwise and 4 spanwise collocation stations. Planform geometry and AIC control station locations are shown in Figure 4.6. Summarized below are input parameters. A listing of the data input cards and computer output follows.

X(1) = 0.0'      X(2) = 1.0'      X(3) = 2.0'      X(4) = 3.0'      X(5) = 4.0'  
Y(1) = 0.0'      Y(2) = 1.0'      Y(3) = 2.0'

SOUND = 1116.87 ft/sec

NMACH = 1	Number of Mach numbers	
KF = 1	Input reduced frequency	
NFREQ = 1	Number of reduced frequencies	
LCOLL = 1	Print collocation station coordinates	
LPUNCH = 1	Punch AIC matrix for wing	
NWCX = 4	Number of chordwise AIC collocation stations on wing	
NCCX = 2	Number of chordwise AIC collocation stations on control surface	
NIONCX = 4	Factor for determining number of chordwise integration stations	
NIY = 4	Number of spanwise AIC collocation stations	
ISOLAT = 1	Isolate wing and control surface	
FMACH (1) = 0.5	Mach number	
FREQ(1) = 0.10	Reduced frequency	
YAIC(1,W) = 0.2'	YAIC(2,W) = 0.7'	YAIC(3,W) = 1.3'
YAIC(4,W) = 1.8'		
YAIC(1,CS) = 0.2'	YAIC(2,CS) = 0.7'	YAIC(3,CS) = 1.3'
YAIC(4,CS) = 1.8'		

$XAIC(1,1,W) = 0.10'$	$XAIC(1,2,W) = 0.70'$	$XAIC(1,3,W) = 1.30'$
$XAIC(1,4,W) = 1.90'$		
$XAIC(2,1,W) = 0.10'$	$XAIC(2,2,W) = 0.70'$	$XAIC(2,3,W) = 1.30'$
$XAIC(2,4,W) = 1.90'$		
$XAIC(3,1,W) = 0.38'$	$XAIC(3,2,W) = 0.90'$	$XAIC(3,3,W) = 1.405'$
$XAIC(3,4,W) = 1.915'$		
$XAIC(4,1,W) = 0.86'$	$XAIC(4,2,W) = 1.22'$	$XAIC(4,3,W) = 1.58'$
$XAIC(4,4,W) = 1.94'$		
$XAIC(1,1,CS) = 3.25'$	$XAIC(1,2,CS) = 3.75'$	
$XAIC(2,1,CS) = 3.25'$	$XAIC(2,2,CS) = 3.75'$	
$XAIC(3,1,CS) = 3.25'$	$XAIC(3,2,CS) = 3.75'$	
$XAIC(4,1,CS) = 3.25'$	$XAIC(4,2,CS) = 3.75'$	



• AJC CONTROL STATION

FIGURE 4.6  
SUBSONIC SAMPLE PROBLEM #2

DATA CARD COLUMN NUMBER

卷之三

FIGURE 4.7 - LISTING OF INPUT DATA CARDS FOR SUPERSONIC SAMPLE PROBLEM 2

## HUGHES AIRCRAFT CO. SUPERSONIC AIC PROGRAM

## FLIGHT CONDITIONS AND GEOMETRY

MACH NUMBER = 1.50000      SPEED OF SOUND = 1116.870 L/T      RHO=0.1000000E 01

## WING

L.E. STATION (L)	0.
ROOT CHORD (L)	2.000
L.E. SPAN (L)	1.000
T.E. SPAN (L)	2.000
TIP CHORD (L)	2.000
TOTAL AREA (L*L)	7.000
SPAN COLL. STA.	4
CHORD COLL. STA.	4
CHORD INTG. STA.	16
SPAN PRES MODES	4
CHORD PRES MODES	4

-6-

## TAIL

3.000
1.000
2.000
2.000
1.000
1.000
4.000
4
2
8
4
2

LIGHTS AIRCRAFT C7. SUBSONIC ATC PROGRAM (CONT-n)

UNSTEADY AERO COLLOCATION STATION COORDINATES ON THE WING

S STA	Y0	YC	XC VALUES--
1	0.	0.276266E 00	0.952418E 00
2	.765367E 01	0.276266E 00	0.952418E 00
3	.141421E 01	0.633263E 01	0.116938E 01
4	0.184776E 01	0.100692F 01	0.139847E 01

INTEGRATION STATION COORDINATES ON THE WING

S STA	Y0	Y1	XI VALUES--
1	0.390181E 01	0.452807E-02	0.405070E-01
2	.111114E 01	0.115417F 00	0.149396E 00
3	0.166294E 1	0.665966E 00	0.690019E 00
4	0.196157E 01	0.963922E 00	0.982602E 00

HIGHES AIRCRAFT CO. SURSONIC AIC PROGRAM (CONT'D)

UNSTEADY AERO COLLOCATION STATION COORDINATES ON THE TAIL.

S STA #D	YC	XC VALUES--
1	6.	0.345387E 01      0.399149E 01
2	.755367E .03	0.345387E 01      0.399149E 01
3	.141421E .11	0.345387E .11      0.399149F 01
4	.184776E .03	0.345387E 01      0.399149E 01

INTEGRATION STATION COORDINATES ON THE TAIL.

S STA #D	YI	XI VALUES--
1	0.390181E .00	0.300051E 01      0.307489E 01      0.319868E 01      0.336317E 01
		0.354613E 01      0.3722287E 01      0.386950E 01      0.396624E 01
2	0.111114E .01	0.300851E .01      0.307489E 01      0.319868E 01      0.336317E 01
		0.354613F .01      0.3722287E 01      0.386950E 01      0.396624E 01
3	0.166294E .01	0.300851E 01      0.307489E 01      0.319868E 01      0.336317E 01
		0.354613E 01      0.3722287E 01      0.386950E 01      0.396624E 01
4	.196157E .02	0.300851E 01      0.307489E 01      0.319868E 01      0.336317E 01
		0.354613E 01      0.3722287E 01      0.386950E 01      0.396624E 01

HUGHES AIRCRAFT CO. SUBSONIC AIC PROGRAM (CONT'D)

AIC COLLOCATION STATION COORDINATES ON THE MING

Y-AIC	X-AIC VALUES--
0.260000E 00	0.100000E 00
0.700000E 00	0.100000E 00
0.130000E 01	0.380000E 00
0.180000E 01	0.860000E 00

HUGHES AIRCRAFT CO. SURSONIC AIC PROGRAM (CONT-D)

AIC COLLOCATION STATION COORDINATES ON THE TAIL

YAIC	XAIC VALUES--
0.200000E 00	0.325000E 01
0.706000E 00	0.325000E 01
0.130000E 01	0.325000E 01
0.180000E 01	0.325000E 01

HUGHES AIRCRAFT CO. SUBSONIC AIC PROGRAM (CONT'D)

Oscillator Frequency (cps)      8 887775 00

REFERENCE CHORD 1.00000E+00

REINFORCED FREQUENCY (REF. CH020) 1 000000 00

THE JOURNAL OF CLIMATE

“**THE DOGHOUSE**” (1935). (Courtesy: **Columbia Pictures**)

FREE STREAM HACH NUMBER 5.00000E-01

FREE STREAM VELOCITY 5.58435E 02

DENSITY 1.00 DYNAMIC PRESSURE 14.22 DYNAMIC HEAD

סְרִירָה

AERODYNAMIC STABILITY

ROW = 6  
6.-679E 01 -1.4648E 02 -2.6468E 02 1.9922E 00 3.7066E 02 8.2695E 00 -1.7038E 02 -1.0909E 01 -7.5857E 01 1.3904E 00  
3.-675E 02 -2.2438E 02 -4.2802E 02 -1.0628E 01 1.8684E 02 1.2297E 01 -1.2306E 00 -2.7545E 02 1.9763E 00  
3.-9519F 02 7.3449E 00 -1.8181E 02 -9.8388E 01 -3.3263E 01 6.6336E-01 1.0193E 02 1.7567E-01 -1.1463E 02 -2.7928E 00  
4.-5541F 01 2.3699E 02 0. 0. 0. 0. 0. 0. 0. 0. 0.  
0. 0. 0. 0. 0. 0. 0. 0. 0. 0.  
ROW = 7  
-1.5219E 02 5.5205E 01 2.3393E 02 4.8690E 00 -1.0440E 02 -1.0909E 01 -9.9578E-01 1.8222E 00 1.5333E 02 -6.3050E 00  
-3.-76E 02 -4.1516E 01 2.0786E 02 1.3047E 01 -4.0722E 01 -4.2358E 00 -1.2315E 02 4.4603E 00 2.2623E 02 4.2519E 00  
-9. 5611E 02 -9.5611E 01 -9.1653E 00 1.3951E 00 5.9340E 01 -1.0576E 00 -8.1925E 01 -1.3560E 00 1.5280E 01 1.0896E 00  
7.2765E 01 2.6233E-01 0. 0. 0. 0. 0. 0. 0. 0.  
0. 0. 0. 0. 0. 0. 0. 0. 0. 0.  
ROW = 8  
-1.5118E 02 6.2412E 00 5.9137E 02 -1.0005E 00 -3.7849E 02 -9.8672E 00 1.3054E 02 6.1771E 00 1.7172E 02 -7.2691E 00  
-5.-712E 02 -8.7469E 01 1.3338E 02 5.4807E 00 7.0677E 01 -1.4915E 00 -1.3744E 02 5.1976E 00 3.9474E 02 -9.6239E-01  
-3.-9150E 02 -6.0459E 01 0. 0. 0. 0. 0. 0. 0. 0.  
-3.-9172E 01 -1.0529E 01 0. 0. 0. 0. 0. 0. 0. 0.  
0. 0. 0. 0. 0. 0. 0. 0. 0. 0.  
ROW = 9  
4.6979E 01 -1.1843E 00 -1.0236E 02 -1.2399E 00 9.3337E 01 1.5168E 00 -4.0002E 01 -1.2296E 00 -5.6749E 01 1.2945E 00  
1.4682E 02 1.8743E 00 -1.3198E 02 -1.0504E 00 4.1829E 01 4.3986E 00 1.1167E 02 "2.032E 00 -2.3048E 02 -3.2393E 00  
1.-9391E 02 6.0459E 01 -7.5104E 01 -4.0479E 00 -1.8902E 01 1.7013E-01 1.3020E 01 7.4965E-01 1.6267E 01 -6.1641E-01  
-1.1207E 01 1.5619E-01 0. 0. 0. 0. 0. 0. 0. 0.  
0. 0. 0. 0. 0. 0. 0. 0. 0. 0.  
ROW = 10  
1.-3925E 01 -2.7235E-01 -5.9586E 01 6.86621E-01 8.8990E 01 1.1332E 00 -4.3271E 01 -2.2388E 00 -1.6181E 01 4.0905E-01  
7.2.55E 01 -5.9037E-01 -9.6177E 01 -2.3731E 00 4.0247E 01 2.5899E 00 3.2251E 01 -6.0941E-01 1.4708E 02 1.1821E 00  
2.-892E 02 3.8027E 00 -1.0317E 02 -5.4764E 00 -8.3388E 00 2.6659E-01 9.5617E 00 3.5495E-01 5.9130E 00 -6.0830E-01  
-2.2432E 00 -2.1548E-02 0. 0. 0. 0. 0. 0. 0. 0.  
0. 0. 0. 0. 0. 0. 0. 0. 0. 0.  
ROW = 11  
-2.7412E 01 1.-3036E 01 5.0347E 01 1.0822E 00 -1.9762E 01 -2.5424E 00 -2.7807E 00 2.8109E-01 3.4722E 01 "1.4633E 00  
-8.-6232E 01 -4.6331E-01 7.0856E 01 3.2160E 00 -2.0395E 01 -1.5715E 00 -6.4063E 01 2.9212E 00 1.1232E 02 2.4260E 00  
-3.-5871E 01 -5.0829E 00 -1.2233E 01 4.1498E-01 1.2479E 01 1.1393E-02 -9.3474E 00 -1.8208E-01 -4.0810E 00 -6.4229E-01  
-9.-150E-01 2.8642E-01 0. 0. 0. 0. 0. 0. 0. 0.  
0. 0. 0. 0. 0. 0. 0. 0. 0. 0.  
ROW = 12  
-3.-261E 01 1.4017E 01 6.4463E 01 -2.8477E-01 -8.2248E 01 -2.1176E 00 2.8106E 01 1.2449E 00 3.6287E 01 -1.6621E 00  
-1.-2568E 02 1.1429E 00 1.4010E 02 2.5728E 00 -5.2752E 01 -2.2764E 00 -7.0847E 01 2.7464E 00 2.0339E 02 -3.9999E-01  
-1.-AC2E 02 -4.6879E 00 6.5604F 01 2.7877E 01 1.6746E 01 -1.9716E-01 -2.0533E 01 -3.3236E-01 3.1910E 00 -1.4875E-03  
5.-7792E-01 8.6263E-02 0. 0. 0. 0. 0. 0. 0. 0.  
0. 0. 0. 0. 0. 0. 0. 0. 0. 0.  
ROW = 13  
-4.-3238E 02 9.11445E 01 9.0571E 02 1.7560E 01 -7.1672E 02 -3.7351E 01 2.4511E 02 2.3084E 01 7.3188E 02 -1.6371E 01  
-1.-5378E 03 -2.6432E 01 1.3925E 03 6.5947E 01 -4.86621E 02 -4.1930E 01 -4.1622E 02 8.2079E 00 8.8129E 02 1.3087E 01  
-6.-9704E 02 -3.1538E 01 2.3176E 02 1.9440E 01 2.6766E 02 -3.5799E 00 -4.5456E 02 -6.5103E 00 2.8251E 02 8.9503E 00  
-9.-574E 01 -5.2163F 0. 0. 0. 0. 0. 0. 0. 0.  
0. 0. 0. 0. 0. 0. 0. 0. 0. 0.  
ROW = 14  
-1.4151E 02 3.3710E 00 5.1639E 02 -2.8059E 00 -6.8630E 02 -1.8196E 01 3.0095E 02 2.0501E 01 2.1543E 02 -5.1456E 00  
-9.-387F 02 0.9104E 01 1.2463E 03 2.9452F 03 5.5610E 02 -5.6036E 01 1.2577E 02 2.4229F 00 5.3123E 02 -2.7508E 00  
-7.-2457E 02 -1.6163E 01 6.1676E 02 1.8436E 01 8.7939E 01 -1.5304E 00 -2.9630E 02 3.6949E 02 6.3263E 00



```

0. 0. 0. 0. 0. 0. 0.
-1.5643E 02 0. -3.1144E 00 -1.6762E 02 -3.3919E 00 1.6724E 02 1.1759E 01 3.0324E 02 4.1393E 00 -3.0267E 02 -1.9276E 01
-1.5669E 01 1.5607E 02 1.0923E 01 6.9669E 01 6.1505E-01 -6.9544E 01 -4.2933E 00
R04 =24
0. 0. 0. 0. 0. 0. 0.
0. 0. 0. 0. 0. 0. 0.
0. 0. 0. 0. 0. 0. 0.
0. 0. 0. 0. 0. 0. 0.
0. 0. 0. 0. 0. 0. 0.
0. 0. 0. 0. 0. 0. 0.
4.6866E 00 -1.5706E 01 -4.4734E 00 1.5502E 01 -3.8450E-01 6.5085E 00 5.4729E-01 -6.4892E 00

```

Sample Problem 3

A  $45^\circ$  delta wing-control surface combination is analyzed for  $M = 0.5$  and  $f = 5.0$  cps. There are 4 spanwise and 4 chordwise AIC control stations for both the wing and control surface. The planform geometry and AIC control station locations are shown in Figure 4.8. The input parameters are summarized below and a listing of the data input cards and computer output follows.

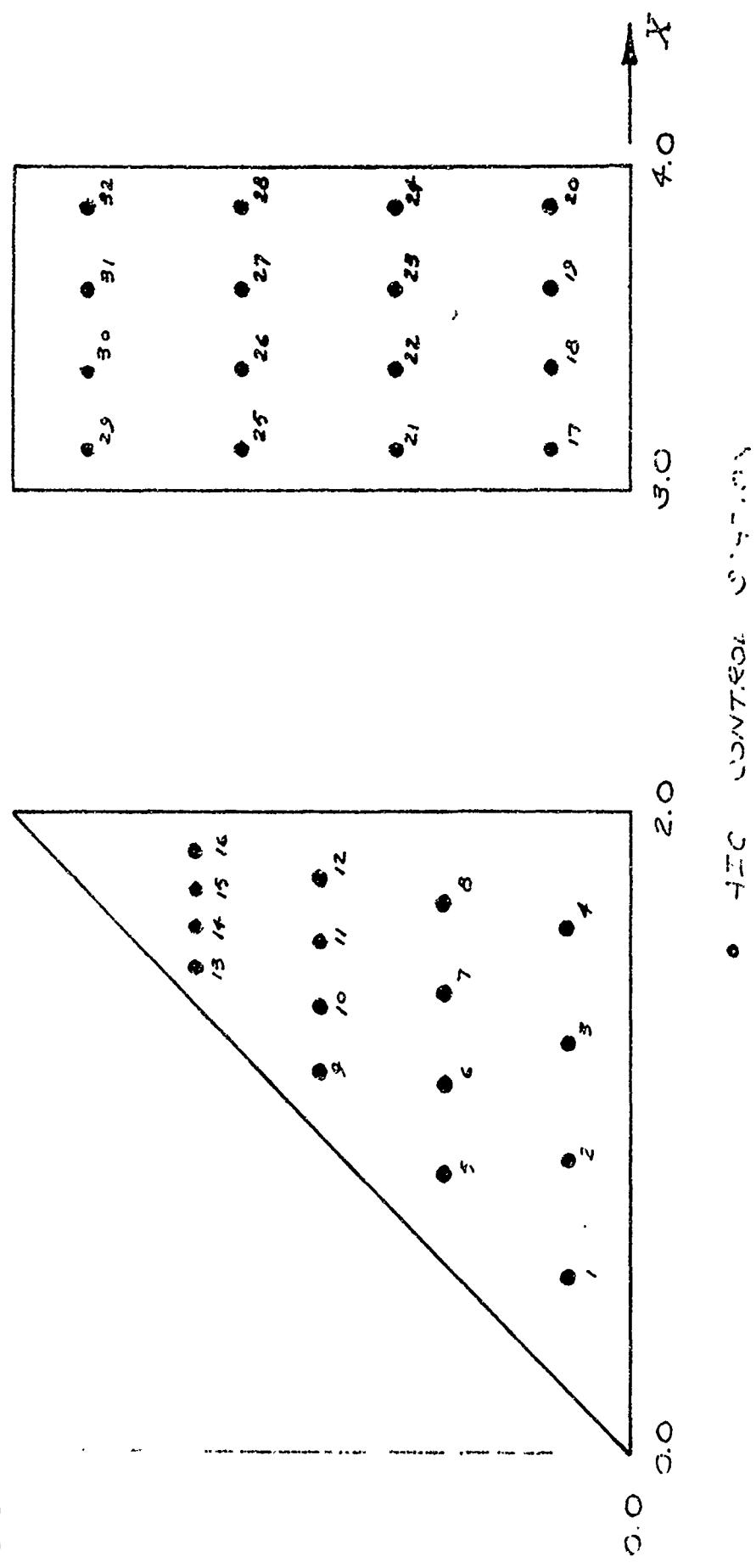
$X(1) = 0.0'$      $X(2) = 2.0'$      $X(3) = 2.0'$      $X(4) = 3.0'$      $X(5) = 4.0'$   
 $Y(1) = 0.0'$      $Y(2) = 0.0'$      $Y(3) = 2.0'$

SOUND = 1116.87 ft/sec

NMACH = 1	Number of Mach numbers
KF = 0	Input frequencies
NFREQ = 1	Number of frequencies
LCOLL = 1	Print collocation station coordinates
LPUNCH = 4	Punch cards for total AIC matrix
NWCX = 4	Number of chordwise AIC collocation stations on wing
NCCX = 4	Number of chordwise AIC collocation stations on control surface
NIONCX = 4	Factor for determining number of chordwise integration stations
NIY = 4	Number of spanwise AIC collocation stations
ISOLAT = 0	Surfaces are not isolated
FMACH(1) = 0.5	Mach number
FREQ(1) = 5.0	Frequency
YAIC(1,W) = 0.2'	YAIC(2,W) = 0.6'    YAIC(3,W) = 1.0'
YAIC(4,W) = 1.4'	
YAIC(1,CS) = 0.25'	YAIC(2,CS) = 0.75'    YAIC(3,CS) = 1.25'
YAIC(4,CS) = 1.75'	

XAIC(1,1,W) = 0.56'	XAIC(1,2,W) = 0.92'	XAIC(1,3,W) = 1.28'
XAIC(1,4,W) = 1.64'		
XAIC(2,1,W) = 0.88'	XAIC(2,2,W) = 1.16'	XAIC(2,3,W) = 1.44'
XAIC(2,4,W) = 1.72'		
XAIC(3,1,W) = 1.20'	XAIC(3,2,W) = 1.40'	XAIC(3,3,W) = 1.60'
XAIC(3,4,W) = 1.80'		
XAIC(4,1,W) = 1.52'	XAIC(4,2,W) = 1.64'	XAIC(4,3,W) = 1.76'
XAIC(4,4,W) = 1.88'		
XAIC(1,1,CS) = 3.125'	XAIC(1,2,CS) = 3.375'	XAIC(1,3,CS) = 3.625'
XAIC(1,4,CS) = 3.875'		
XAIC(2,1,CS) = 3.125'	XAIC(2,2,CS) = 3.375'	XAIC(2,3,CS) = 3.625'
XAIC(2,4,CS) = 3.875'		
XAIC(3,1,CS) = 3.125'	XAIC(3,2,CS) = 3.375'	XAIC(3,3,CS) = 3.625'
XAIC(3,4,CS) = 3.875'		
XAIC(4,1,CS) = 3.125'	XAIC(4,2,CS) = 3.375'	XAIC(4,3,CS) = 3.625'
XAIC(4,4,CS) = 3.875'		

Figure 4.8 - 4EC COUNTING SURVEY POINTS



DATA CARD COLUMN NUMBER				MACH NO.	FREQ.	Y-WING	Y-TAIL	X-WING	X-TAIL	X-TAIL
0.0	2.0	2.0	4.0							
0.1	0.0	2.0	1116.87							
	1	0	1	1						
	4	4	4	4						
0.5										
5.0										
0.200	0.600	1.000	1.400							
0.250	0.750	1.250	1.750							
0.560	0.920	1.280	1.640	0.880	1.160					
1.440	1.720	1.200	1.400	1.600	1.800					
1.520	1.640	1.760	1.880							
3.125	3.375	3.625	3.875	3.125	3.375					
3.625	3.875	3.125	3.575	3.625	3.875					
3.125	3.375	3.625	3.875							

## HUGHES AIRCRAFT CO. SURSONIC AIC PROGRAM

## FLIGHT CONDITIONS AND GEOMETRY

MACH NUMBER = 0.50000 SPEED OF SOUND = 1116.870 L/T

RHO=0.10000000E 01

	WING	TAIL
L.E. STATION (L)	0.	3.000
ROOT CHORD (L)	2.000	1.000
L.E. SPAN (L)	0.	2.000
T.E. SPAN (L)	2.000	2.000
TIP CHORD (L)	0.	1.000
TOTAL AREA (L*L)	4.000	4.000
SPAN COLL. STA.	4	4
CHORD COLL. STA.	4	4
CHORD INTG. STA.	16	16
SPAN PRES MODES	4	4
CHORD PRES MODES	4	4

## HUGHES AIRCRAFT CO. SUPERSONIC AIC PROGRAM (CONT-D)

## UNSTEADY AERO COLLOCATION STATION COORDINATES ON THE WING

S STA	VO	YC	XC VALUES--
1	0.	0.276266E 00	0.952418E 00 0.105486E 01 0.199547E 01
2	0.765367E 00	0.935910E 00	0.135331E 01 0.178694E 01 0.199720E 01
3	0.141421E 01	0.149513E 01	0.169317E 01 0.189891E 01 0.199847E 01
4	0.184776E 01	0.186879E 01	0.192026E 01 0.197373E 01 0.199966E 01

## INTEGRATION STATION COORDINATES ON THE WING

S STA	VO	YI	XI VALUES--
1	0.390181E 00	0.391625E 00	0.422785E 00 0.479638E 00 0.562389E 00
		0.667967E 00	0.792239E 00 0.931630E 00 0.108054E 01
		0.123339E 01	0.130403E 01 0.152949E 01 0.166198E 01
		0.177763E 01	0.187222E 01 0.194234E 01 0.198545E 01
2	0.111114E 01	0.111315E 01	0.112914E 01 0.116055E 01 0.120672E 01
		0.126493E 01	0.133336E 01 0.140215E 01 0.149232E 01
		0.157672E 01	0.166035E 01 0.174196E 01 0.181336E 01
		0.187722E 01	0.192945E 01 0.196016E 01 0.199197E 01
3	0.166294E 01	0.166370E 01	0.166977E 01 0.168167E 01 0.169960E 01
		0.172111E 01	0.174720E 01 0.178355E 01 0.180446E 01
		0.183949E 01	0.187120E 01 0.190468E 01 0.192935E 01
		0.195344E 01	0.197329E 01 0.198793E 01 0.199995E 01
4	0.196157E .J1	0.196166E 01	0.196235E 01 0.196371E 01 0.196588E 01
		0.196820E 01	0.197118E 01 0.197450E 01 0.197805E 01
		0.198170F 01	0.198532E 01 0.198877E 01 0.199093E 01
		0.199469E 01	0.199695F 01 0.199862E 01 0.199949E 01

HUGHES AIRCRAFT CO. SURSONIC AIC PROGRAM (CONT-D)

UNSTEADY AERO COLLOCATION STATION COORDINATES ON THE TAIL

S STA	X0	YC	XC VALUES--
1	0.	0.313813E 91	0.347621E 01 0.382743E 01 0.399774E 01
2	0.765367E 01	0.313813E 01	0.347621E 01 0.382743E 01 0.399774E 01
3	0.141421E 11	0.313813E 91	0.347621E 01 0.382743E 01 0.399774E 01
4	0.184776E 01	0.313813E 01	0.347621E 01 0.382743E 01 0.399774E 01

INTEGRATION STATION COORDINATES ON THE TAIL

S STA	X0	Y1	X1 VALUES--
1	0.390181E 05	0.300226E 01	0.302025E 01 0.309558E 01 0.310497E 01
	0.317257E 01	0.325000E 01	0.333647E 01 0.342884E 01
	0.352379E 01	0.361788E 01	0.370771E 01 0.379003E 01
	0.386187E 01	0.392063E 01	0.396418E 01 0.399096E 01
2	0.111114E 01	0.300226E 01	0.302025E 01 0.309558E 01 0.310697E 01
	0.31257E 01	0.325000E 01	0.333647E 01 0.342884E 01
	0.352379E 01	0.361788E 01	0.370771E 01 0.379003E 01
	0.386187E 01	0.392063E 01	0.396418E 01 0.399096E 01
3	0.166294E 01	0.300226E 01	0.302025E 01 0.309558E 01 0.310697E 01
	0.317257E 01	0.325000E 01	0.333647E 01 0.342884E 01
	0.352379E 01	0.361788E 01	0.370771E 01 0.379003E 01
	0.386187E 01	0.392063E 01	0.396418E 01 0.399096E 01
4	0.196157E 01	0.300226E 01	0.302025E 01 0.309558E 01 0.310697E 01
	0.317257E 01	0.325000E 01	0.333647E 01 0.342884E 01
	0.352379E 01	0.361788E 01	0.370771E 01 0.379003E 01
	0.386187E 01	0.392063E 01	0.396418E 01 0.399096E 01

HUGHES AIRCRAFT CO. SUBSONIC AIC PROGRAM (CONT'D)

AIC COLLOCATION STATION COORDINATES ON THE WING

YAIC	XAIC VALUES--
0.200000E 01	0.560000E 00
0.600000E 00	0.880000E 00
0.100000E 01	0.120000E 01
0.140000E 01	0.152000E 01

YAIC	XAIC VALUES--
0.200000E 01	0.920000E 00
0.600000E 00	0.116000E 01
0.100000E 01	0.140000E 01
0.140000E 01	0.164000E 01

YAIC	XAIC VALUES--
0.200000E 01	0.128000E 01
0.600000E 00	0.144000E 01
0.100000E 01	0.160000E 01
0.140000E 01	0.176000E 01

HUGHES AIRCRAFT CO. SUBSONIC AIC PROGRAM (CONT'D)

AIC COLLOCATION STATION COORDINATES ON THE TAIL

YAIC	XAIC VALUES--	YAIC VALUES--	XAIC VALUES--
0.25000E 00	0.312500E 01	0.337500E 01	0.362500E 01
0.75000E 00	0.312500E 01	0.337500E 01	0.362500E 01
0.12500E 01	0.312500E 01	0.337500E 01	0.362500E 01
0.17500E 01	0.312500E 01	0.337500E 01	0.362500E 01

## HUGHES AIRCRAFT CO. SUBSONIC AIC PROGRAM (CONT-D)

OSCILLATORY FREQUENCY (CPS)	5.0000E 00
REFERENCE CHORD	1.0000E 00
REDUCED FREQUENCY (REF. CHORD)	5.62571E-02
REDUCED VELOCITY (REF. CHORD)	1.77756E 01
FREE STREAM MACH NUMBER	5.00000E-01
FREE STREAM VELOCITY	5.58435E 02
DENSITY	1.00
DYNAMIC PRESSURE (1/2*RH0*VEL**2)	1.555925E 05

## AERODYNAMIC INFLUENCE COEFFICIENTS

	RL	IM	RL	IM	RL	IM	RL	IM	RL	IM	RL	IM
RW = 1												
2.5673E 03	-2.9785E 01	-7.7904E 01	-4.5876E 01	9.4193E 03	2.0440E 02	-3.1958E 03	-1.3970E 02	-4.9141E 03	5.0965E 01			
1.2869E 04	4.3412E 01	-1.2358E 04	-2.2343E 02	4.4032E 03	1.5052E 02	3.3245E 03	-6.6726E 01	-2.6779E 00	-6.9088E 03	-2.6779E 01		
9.2755E 03	7.3226E 01	-3.6510E 03	-5.9478E 01	-8.1422E 02	1.0365E 01	2.6406E 01	-8.112E 01	-3.4314E 03	3.6715E 01			
1.6515E 03	-1.4966E 01	4.4291E 00	-2.0916E -01	4.0959E 01	1.5137E 01	2.0381E 01	-2.0327E 00	-1.4235E 01	1.2149E 00			
7.2944E -01	-2.3879E -02	-2.0411E 00	1.7339E -01	4.3454E 00	-4.7356E -01	-3.0321E 00	2.8997E -01	2.5813B 00	-1.1019E -01	1.9735E 00		
5.7725E 00	5.3841E 09	5.3522E -01	1.3635E 01	-1.4009E 00	-9.5079E 00	8.4097E -01	7.6408E -01	-2.7008E -02	-2.3881E 00	1.9735E 00		
RW = 2	7.5375E 00	-9.6302E 02	-5.0438E 00	2.0128E 03	2.0049E 01	-1.0495E 03	-2.4288E 01	-4.6365E 01	-6.6186E 00			
-3.1106E 03	5.5177E 00	-3.1298E 03	-2.9621E 01	1.5653E 03	3.1467E 01	6.4005E 01	3.7660E 00	-1.1280E 03	-2.9843E 00			
2.89E 03	1.1118E 01	-1.048E 03	-1.2304E 01	1.3121E 01	-4.6586E 01	1.4578E 02	2.2442E 00	-2.3786E 02	-4.0268E 00			
7.4959E 01	1.6202E 03	1.2082E 00	-2.2042E -01	4.2680E 00	5.2242E 01	9.8038E 00	-2.1423E 00	-6.7560E 00	1.3716E 00			
5.1165E -01	-4.9175E -02	-1.2879E 00	2.0630E -01	2.4659E 00	-4.9277E 01	-1.6907E 00	3.1573E -01	1.1702E 00	-1.5044E -01			
-3.1138E 00	4.4067E -01	7.2114E 00	-1.5131E 00	-4.9709E 00	9.6830E -01	5.5073E -01	-5.5023E -02	-1.5352E 00	2.7458E -01			
3.593E 01	-6.5627E -01	-2.1776E 00	4.1625E -01									
RW = 3												
6.413E 02	2.2031E 01	1.4974E 03	-7.7901E 00	-9.1550E 02	-2.7591E 01	9.2525E 01	1.2217E 01	1.3025E 03	-2.8957E 01			
2.514E 03	1.1957E 01	1.2856E 03	2.3651E 01	5.6336E 01	-9.7148E 00	-5.5753E 02	1.3013E 01	1.6842E 03	-7.8314E 00			
-9.116E 01	-6.8127E 01	1.4361E 02	3.0957E 00	2.3739E 02	-1.4094E 00	-6.3986E 02	6.4704E 00	7.5844E 02	-9.8509E 00			
-3.5752E 02	5.4903E 00	-1.4641E 00	-2.0096E 01	-4.4114E 00	8.9416E -01	9.4105E 00	-2.1318E 00	-6.4762E 00	1.3685E 00			
4.125E 01	-5.1321E -02	-1.1241E 03	2.1284E -01	2.2900E 00	-5.0107E -01	-1.5805E 00	3.2049E 01	1.1459E 00	-1.5560E -01			
-3.725E 00	6.4241E -01	-6.8259E 00	-1.5306E 00	-4.7090E 00	9.8139E -01	5.2442E -01	-6.1521E -02	-1.4632F 00	2.8859E -01			
2.0879E 01	-6.5366E -01	-2.0572E 00	4.3342E -01									
RW = 4												
5.15E 03	4.75E 02	5.1629E 01	-5.3857E 01	-6.3603E 01	-6.4825E 01	2.1073E 03	5.5107E 01	3.4227E 03	-6.7138E 01			
-1.426E 02	4.1162E 03	2.5354E 01	-5.5564E 01	-5.9912F 01	-5.9912F 01	-2.1198E 03	2.7931E 01	6.6552F 03	-2.3235E 01			
-6.516E 03	-2.4146E 01	2.4525E 03	5.7895E 01	-1.1506E 00	-2.0137E 03	7.0142E 00	2.5907E 03	-8.2366E 00				
-1.72E 01	3.4604E 00	-1.2978E 00	-2.2978E 00	-9.7291F 01	3.7732E -01	1.5677E 01	-2.3302F 00	-1.1572E 01	1.3473E 00			
3.192E 00	-4.4614E 02	-1.2978E 00	2.3408E 01	5.3703E 00	-5.6366E -01	-2.3938F 00	3.4867E -01	2.2181E 00	-1.2075E -01			

NOT REPRODUCIBLE

4.3971E 00 -7.8007E-01 -3.0374E 00 4.8182E-01

ROW = 5  
1.7828E 03 -2.0541E 01 -5.4233E 03 -3.0736E 01 5.9027E 03 1.3374E 02 -2.2619E 03 "9.8660E 01 -3.5449E 03 3.6887E 01

9.2700E 03 2.8965E 01 -8.8956E 03 0.5040E 02 3.1688E 03 1.0372E 02 2.1053E 03 "2.204E 01 -7.6227E 01 1.9227E 03 1.9227E 01

7.7771E 03 5.4610E 01 -3.0622E 03 -7.3925E 02 0.4410E 02 1.3203E 01 1.3203E 01 -2.1771E 01 -2.7335E 03 2.9037E 01 2.9037E 01

1.2456E 03 -1.1380E 01 5.2399E 00 -4.110E-01 -1.3203E 01 1.6814E 00 2.6097E 01 -3.997E 00 -1.8117E 01 2.4832E 00 2.4832E 00

9.9515E-01 -7.6419E-02 -2.7582E 00 3.715E-01 5.7702E 00 -9.2799E-01 4.0118E 00 5.0888E-01 3.2677E 00 -2.5902E-01

-6.7199E 00 1.1579E 00 1.7826E 01 -2.7946E 00 -1.2389E 01 1.7523E 00 1.0872E 00 -9.0476E-02 -3.2939E 00 4.6801E-01 4.6801E-01

7.1522E 00 -1.1618E 00 -4.9460E 00 7.3066E-01 3.5074E-01

ROW = 6  
1.1520E 00 5.2419E 00 -6.6942E 02 -3.5382E 00 1.3979E 03 1.3829E 01 "7.2039E 02 -1.4799E 01 -3.4799E 01 -4.6350E 00

1.1546E 03 4.0155E 00 -2.2355E 03 -2.1204E 01 1.1153E 03 2.2304E 01 5.7774E 01 2.7304E 00 -9.6800E 02 -2.6757E 00

1.6222E 03 1.0513E 01 -8.6881E 02 -1.0063E 01 0.0612E 00 3.0581E-02 1.2056E 02 1.6942E 00 -1.7208E 02 1.5353E 00

4.474E 01 1.2465E 00 1.2114E 00 1.8274E-01 -3.9101E 00 7.7147E-02 8.7121E 00 -1.0330E 00 -6.0122E 00 1.1511E 00

4.4798E-01 -4.1164E-02 1.0245E 00 1.7462E-01 -2.1634E 00 -4.1020E-01 1.4882E 00 2.6144E-01 1.0795E 00 -1.2545E-01

-3.0537E 00 5.3661E-01 0.3631E 00 -1.2776E 00 4.3951E 00 0.1533E-01 4.9377E-01 -4.9550E-02 -1.3533E 00 2.3129E-01

2.7670E 00 -5.5415E-01 -1.9106E 00 3.5074E-01

ROW = 7  
-4.6615E 02 1.5235E 01 1.0358E 03 -5.5881E 00 -6.3566E 02 -1.8617E 01 6.4249E 01 8.2244E 00 9.3998E 02 -2.0519E 01

-1.8313E 03 6.7439E 00 9.5866E 00 9.9278E 01 1.6589E 01 -5.1261E 00 2.1943E 01 -7.3016E 01 -2.5047E 02 4.7515E 00 6.4436E 03

-7.0213E 02 -3.0586E 00 1.1282E 00 -1.3596E-01 -3.3322E 00 6.1258E-01 7.0628E 00 -1.4712E 00 -4.2650E 00 9.3988E-01

-3.0312E 02 2.7021E 00 1.4220E 00 -1.7227E 00 -3.4848E-01 1.1947E 00 2.2559E-01 6.0033E-01 -9.8367E-02

3.2742E-01 -3.4203E-02 -8.6264E-01 1.4720E-01 1.7227E 00 -1.0591E 00 -3.5502E 00 6.7572E-01 4.2134E-01 -4.2014E-02 -1.9884E-01

-2.4932E 00 4.4155E 01 5.1361E 00 -1.5297E 01 1.2040E 01 2.1633E 00 -3.0888E 01 1.5425E 00 1.1878E-01 1.5011E 00 -1.3826E-02

2.2498E 00 -4.7310E-01 -1.5531E 00 2.9839E-01

ROW = 8  
-1.1832E 01 3.2339E 01 3.9887E 03 -2.3755E 01 -4.4091E 03 -4.6522E 01 1.6038E 03 3.7974E 01 2.4776E 03 -4.7571E 01

-7.1189E 03 3.2763E 01 7.0706E 01 5.3171E 01 -4.2256E 03 4.2028E 01 2.0456E 01 5.6045E 01 5.6528E 01

-5.7.40E 03 -1.9501E 01 2.0450E 03 1.9446E 01 5.4530E 02 -4.2312E-01 1.7709E 03 4.2176E 00 2.1884E 03 -5.0720E 01

-9.5988E 02 -6.0947E-01 3.04855E 00 -5.5044E-02 -6.3n59E 00 4.3121E-01 1.0645E 01 -1.2178E 00 -7.4194E 00 7.4072E-01

2.2571E-01 -2.0621E-02 6.5297E-01 1.2040E-01 2.1633E 00 -3.0888E-01 1.5425E 00 1.1878E-01 1.5011E 00 -1.3826E-02

-3.63330E 00 3.4229E-01 7.0578E 00 -9.0191E-01 4.9387E 00 5.5030E-01 5.4053E-01 -2.6091E-02 -1.4111E 00 1.7095E-01

2.0269E 00 -4.1985E-01 -1.9596E 00 2.507E-01

ROW = 9  
9.5645E 02 -1.1028E 01 -2.9560E 03 -1.4255E 01 3.2488E 03 6.9578E 01 -1.2891E 03 -4.9226E 01 -2.1012E 03 2.2125E 01

5.4931E 03 1.4455E 01 -5.2529E 03 -8.7369E 01 1.8600E 03 5.9753E 01 2.1345E 01 1.7277E 01 5.4415E 03 5.8145E 03

5.4405E 03 2.9088E 01 -2.1349E 03 -2.6469E 01 2.4178E 02 4.3493E 00 6.1025E 01 6.1158E 01 5.4599E 02 2.0468E 01

4.1509E 02 -9.5236E 00 5.9732E 00 -6.3446E-01 -1.5818E 01 2.6068E 00 3.1964E 01 -6.158E 00 -2.2178E 01 3.8917E 00

1.5.79E 00 -1.3681E-01 -3.5606E 00 5.9535E-01 7.3288E 00 -1.4356E 00 5.0844E 00 9.1894E-01 4.0121E 00 -4.2966E 01

-1.0879E 01 1.8255E 00 2.2328E 01 -4.3375E 00 -1.5487E 01 2.7643E 00 1.4943E 00 -1.4944E-01 4.3661E 00 7.6845E-01

9.7413E 00 -1.8516E 00 -6.3858E 00 1.177E 00

ROW = 10  
1.7910E 00 2.7901E 00 -3.15619E 02 -1.2543E 00 7.4255E 02 6.8169E 00 -3.8880E 02 -6.2675E 00 -2.1692E 01 -2.5370E 01

6.7372E 02 2.3095E 00 -1.2950E 03 -7.2112E 01 6.4223E 02 1.2565E 01 4.0095E 01 1.3762E 00 -6.8659E 02 -1.8096E 01

1.2505E 03 6.0533E 00 5.9033E 02 5.8330E 01 3.7078E 00 -5.3475E 02 4.8248E 00 1.0296E 03 -4.9056E 03

1.2775E 02 -3.29901-01 1.03631E 00 -1.3484E-01 3.1484E 00 5.7349E-01 6.8186E 00 -1.3491E 00 -4.7336E 00 8.5945E-01

3.5471E-01 -3.1021E-02 6.7702E-01 1.3222E-01 1.6831E 00 -3.1710E-01 1.1619E 00 2.0201R-01 8.8880E-01 -9.3704E-02

-2.4226E 00 4.0367E-01 4.9647E 00 -9.1494E-01 -3.4373E 00 6.1232E-01 4.0330E-01 -3.5577E-02 -1.0591E 00 2.7409E-01

ROW = 11  
-2.484E 02 8.0778E 00 5.6376E 02 -3.2049E 00 -3.6576E 02 -9.6402E 00 5.0335E 01 4.4228E 00 5.5591E 02 -1.1745E 01

-1.1133E 03 5.2493E 00 5.9033E 02 5.8330E 01 3.7078E 00 -5.3475E 02 4.8248E 00 1.0296E 03 -4.9056E 03

-5.4277E 02 -3.9764E-01 6.2197E 01 6.2412E 01 7.2416E 00 -7.3110E 01 8.3519E 00 2.4156E 02 -1.6493E 02

-2.4558E 02 1.4022E 00 5.6338E 01 4.9287E-02 -1.6937E 00 2.4844E-01 3.5830E 00 -6.12294E-01 2.4531E 00 5.8644E-01

-1.9613E-01 -1.35689E-02 6.2117E-02 6.2117E-02 9.0159E-01 -1.4911E-01 5.0313E-01 5.1031E-02 -3.7831E-02

**NOT REPRODUCIBLE**

-1.	244E 0U	1.3244E-01	2.6478E 00	-4.4768E-01	-1.8369E 00	2.8151E-01	2.5584E-01	-1.7010E-02	-6.1630E-01	8.4056E-02
1.	1.757E 03	-2.3277E-01	-8.1636E-01	1.2572E-01						
ROW = 12										
-6.	15E 02	1.7122E 01	2.1526E 03	-1.3304E 01	-2.4085E 03	-2.3440E 01	8.8816E 02	1.9622E 01	1.4750E 03	-2.7304E 01
-4.	497E 03	1.4971E 01	4.2398E 03	1.1599E 01	-1.4567E 03	-2.5555E 01	-1.4992E 03	1.9608E 01	1.0841E 03	-1.2228E 01
-4.	23E 03	-1.2208E 01	1.4274E 03	1.2668E 01	1.9472E 02	2.2163E 00	-6.9105E 02	-2.0595E 01	9.8534E 02	-2.1597E 00
-4.	906E 02	-6.7221E-01	1.0851E 00	6.9464E-02	-1.8820E 00	-1.5166E-01	2.6831E 00	2.2597E-01	-1.8864E 00	-1.7463E-01
5.	494E-02	-2.0856E-02	-1.7922E-01	4.9763E-01	4.0244E-02	-3.7156E-01	5.475E-02	5.2367E-01	4.0166E-02	
-1.	153E 00	-8.4554E-02	1.7189E 00	1.3494E-01	-1.2277E 00	-1.0841E-01	2.1011E-01	1.1977E-02	-4.1485E-01	-2.2623E-02
6.	-17E-01	4.3815E-02	-4.7705E-01	-3.6794E-02						
ROW = 13										
-4.	228E 03	5.6888E 01	1.3184E 04	6.4762E 01	-1.4163E 04	-3.4484E 02	5.2221E 03	2.3301E 02	1.0798E 04	-1.2234E 02
-2.	8314E 04	-6.3205E 01	2.7306E 04	4.3190E 02	-9.7894E 03	-2.9774E 02	-8.2225E 03	7.6447E 01	2.1478E 04	-3.3629E 02
-2.	672E 04	-1.0101E 02	8.4224E 03	9.6452E 01	4.9774E 03	-4.1204E 01	1.4292E 04	9.6451E 01	1.6977E 04	-1.2647E 02
-7.	62E 03	4.9455E 01	1.4143E 01	-1.9295E 00	-3.9119E 01	8.1451E 00	8.0080E 01	-1.9278E 01	5.3228E 01	1.2459E 01
3.	792E 01	-4.8493E-01	9.4176E 00	2.005E 00	1.9255E 01	-4.6676E 00	1.3351E 01	2.9031F 00	1.0294E 01	1.4057E 00
-2.	153E 01	5.9176E 00	5.7702E 01	-1.3967E 01	-3.9935E 01	9.0199E 00	4.5863E 00	-6.1016E 01	-1.2399E 01	2.6735E 00
2.	5133E 01	-6.2423E 00	-1.7358E 01	3.9805E 00						
ROW = 14										
7.	93E 00	-1.1196E 01	1.5007E 03	4.4376E 00	-3.1704E 03	-2.4133E 01	1.6215E 03	3.3013E 01	1.1475E 02	1.2142E 01
-3.	178E 03	-1.0137E 01	6.8081E 03	5.9956E 01	-3.4045E 03	-6.3787E 01	-1.8567E 02	-3.7168E 00	2.6479E 03	3.5437E 00
-4.	867E 03	-2.2053E 01	2.3245E 03	2.2744E 01	6.5204E 01	6.2568E 00	-1.4605E 03	-4.9959E 00	2.6784E 03	3.1001E 01
-1.	632E 03	-6.7399E 00	1.8057E 00	1.0618E-01	-2.5961E 00	-3.5252E 01	2.8661E 00	6.9951E-01	2.0732E 00	-3.9424E-01
-1.	2117E-01	2.4670E-02	-6.8280E-02	2.1133E-01	1.4332E-01	-1.9282E-01	1.0389E-01	4.8333E-01	7.3410E-02	
-7.	4679E-01	-2.3396E-01	1.2712E 00	4.8595E-01	-3.5484E-01	-3.4124E-01	8.4124E-03	2.8205E-02	-3.5497E-02	-1.0290E-01
1.	3492E-01	2.2848E-01	-1.4958E-01	-1.5518E-01						
ROW = 15										
1.	563E 03	-3.5888E 01	-2.7377E 03	1.1241E 01	1.9651F 03	5.5479E 01	-3.6473E 02	-2.6833E 01	-2.8511E 03	6.0016E 01
5.	647E 03	-2.6845E 01	-2.3473E 03	4.6152E 01	1.6016E 02	1.8633E 01	2.1346E 03	1.8961E 01	-4.1721E 03	1.7917E 01
2.	721E 03	7.6722E 00	4.3473E 02	-6.6150E 02	-1.2718E 03	7.4944E 00	2.7094E 03	-1.8993E 01	1.4297E 03	2.4858E 01
7.	211E 02	-9.6715E 00	-7.4027E 01	3.2179E-01	3.3049E 00	-1.3224E 00	-7.9245E 00	3.0722E 00	5.3794E 00	-2.0202E 00
-4.	75E-01	A.3988E-02	1.1.19E 00	-3.2535E-01	2.1730E 00	7.4214E-01	1.4866E 00	-4.8362E-01	-9.3099E-01	2.3910E 01
-2.	110E 00	-9.6785E-01	-6.2.35E 00	2.2454F 00	4.2394E 00	-1.4718E 00	5.9007E-01	1.0470E-01	1.5351E 00	-4.4896E-01
-2.	816E 03	1.9357F 00	-6.6775F-01	2.429E 00						
ROW = 16										
2.	7750E 03	-1.0093E 04	5.7141E 01	1.1241E 03	1.1241E 04	1.1241E 04	1.2243E 03	1.0281E 02	-7.5168E 03	1.4046E 02
2.	623E 04	-9.4371E 01	-2.1473E 04	-1.5772E 02	7.3722E 01	1.2804E 02	5.8412E 03	-5.7742E 01	-1.6278E 04	4.7005E 01
1.	297E 04	5.2158E 01	-5.8612E 03	-5.5666E 01	-3.3464E 03	1.3469E 01	7.9252E 03	-2.6316F 01	-1.0927E 04	2.1124E 01
4.	478E 03	1.2551E 00	6.5579E 00	5.0583E-01	1.4692E 01	-2.2959E 00	2.6248E 01	5.6489E 00	1.8106E 01	-3.6275E 00
-3.	246E-01	1.3552F-01	2.0194E 00	-6.0403E-01	-5.5478E 00	1.4088E 00	3.3410E 00	8.3592E-01	-3.2039E 00	3.8498E-01
8.	326E 00	-1.7371F 00	-1.7861E 01	4.1747E 00	1.2404F 01	-2.6800E 00	-1.3418E 00	1.7793E-01	3.7144E 00	-8.2538E-01
-7.	471E 06	1.9269E 00	-1.22331E 00	5.1861E 00						
ROW = 17										
-2.	60E 02	1.7164E 01	1.3656E 03	-1.3216E 02	-5.3104E 03	2.7296E 02	2.9241E 03	-1.3558E 02	4.4566E 02	-2.3438E 01
-3.	519F 07	1.9876F 02	0.3621E 03	-4.1074F 12	-4.8576F 03	2.016E 02	-3.4383E 02	2.1404F 01	2.8840E 03	-1.6737E 02
-6.	R2/E 03	3.4667E 01	5.5433E 03	-1.8757E 02	6.9626E 01	7.8264E-01	-7.8320E 02	1.8608F 01	1.6728E 03	-4.1729E 01
-9.	66F 7	2.0205F 01	5.4853E 03	-2.1451F 01	-7.6048E 03	2.7020E 01	-7.3996E 03	7.3626E 00	4.8154E 01	-2.4303E 01
-4.	92E 01	2.2916E 01	1.4665E 04	4.4581E 01	-8.6131E 03	-1.2630E 02	2.8423E 03	7.7423F 01	2.9092E 03	-1.7963E 01
-6.	624F 02	-2.3233F 01	5.275F 13	6.4565F 01	-1.6217E 03	-4.1280F 01	-7.0299E 02	4.2435E 00	1.5375F 03	7.5715E 00
-3.	154F 4	-2.1144F 01	5.5174F 02	1.2842F 01						
ROW = 18										
-4.	7206E 01	3.1764E 06	3.9558E 02	-2.3552E 01	-8.3832E 02	4.8799E 01	4.9024E 02	-2.4605F 01	6.83332E 01	-3.6674E 00
-6.	897E 02	3.1992F 41	5.289E 13	-6.4077E 61	-7.4920E 02	3.2399E 01	5.5649E 01	3.6730E 00	4.6073E 02	-2.8043E 01
-9.	245E 02	5.85635E 01	5.6758E 02	-3.1741E 01	4.1626E 00	9.50948E-01	-8.32635E 01	-1.6746E 00	2.81668E-02	-2.7768E 00

NOT REPRODUCIBLE

-9.	.496E 02	5.4501E 01	4.1637E 03	-5.2199E -01	-5.8196E 03	-4.8602E 01	2.5906E 03	4.7850E 01	5.4909E 02	-2.6334E 00
-2.	.937E 03	8.0441E -01	5.5495E 03	2.7242E 01	-1.6078E 03	-2.8248E 01	-1.3413E 02	5.5698E -01	5.9941E 02	1.8293E -01
-6.	.741E 02	-7.8756E 01	3.6209E 02	7.2713E 00						

R54 = 9

4.	.37E 01	-2.1610E 00	-5.7455E 02	1.8540E 01	7.9232E 02	-3.8099E 01	-4.6042E 02	1.8291E 01	-8.2628E 01	4.3365E 00
7.	.133E 02	-3.5761E 01	-5.5371E 03	7.6560E 01	8.9276E 02	-3.8656E 01	5.5182E 01	-3.1123E 01	-4.7595E 02	2.5762E 01
1.	.246E 03	-5.3457E 01	-5.8174E 02	2.8339E 01	-2.2849E 01	1.3424E 00	1.9436E 01	-2.1212E 01	-4.757F 02	2.3381E 01
2.	.445E 02	-1.2917E 01	-4.3205E 03	1.6849E 01	2.1047E 03	5.6222E 00	-4.7444E 02	-1.9436E 01	-3.0953E 02	1.5817E -01
1.	.325E 03	-2.2201E 01	-3.0822E 03	-9.0241E 00	8.9286E 02	2.8745E 01	3.0661E 02	-2.6146E 00	-1.1060E 03	1.3695E 01
1.	.69E 03	5.3765E 01	-4.4703E 02	-1.6805E 01	-2.3168E 02	8.1385E -01	2.7411E 02	-3.0786E 00	-4.5736E 02	-1.4536E 00
1.	.086E 02	4.3495E 00	3.3357E 01	-6.2692E -01						

R54 = 20

A.	F 01	-4.7162E 00	-7.2823E 02	3.8361E 01	1.5413E 03	-7.9052E 01	-8.9719E 01	3.8612E 01	-1.5077E 02	6.0150E 00
1.	.7312E 01	-6.8373E 01	-7.8148E 03	1.4134E 02	1.6349E 03	-7.1461E 01	1.0435E 02	-6.1964E 00	-6.9125E 02	5.0190E 01
1.	.4615E 03	-1.9425E 02	-1.0915E 03	5.9666E 01	-3.2648E 01	1.3179E 00	3.0245E 02	-1.4259E 01	-6.3873E 02	3.0093E 01
3.	.6897E 02	-1.6262E 01	-2.6067E 03	3.1754E 01	6.8721E 03	-1.0718E 01	-6.3885E 03	-4.1347E 01	2.1226E 03	2.6833E 01
3.	.4525E 03	-4.3689E 01	-9.9372E 03	1.3163E 01	9.3094E 03	6.2797E 01	-3.1228E 03	-4.1858E 01	-2.1920E 03	2.6246E 01
5.	.74E 03	-8.3538E 01	-5.4247E 03	-3.6060E 01	1.8095E 03	2.3601E 01	5.4268E 02	-6.1483F 00	-1.4529E 03	1.3706E 00
1.	.729E 05	1.0263E 01	-4.6267E 02	-6.8235E 00						

R54 = 21

-1.	.4463E 02	1.1055E 01	1.3866E 03	-8.1074E 01	-2.9355E 03	1.6735E 02	1.7146E 03	-8.4055E 01	2.7759E 02	-1.4588E 01
-2.	.735E 03	1.2247E 02	2.2313E 03	-2.5227E 02	-3.0363E 03	1.2661E 02	-2.7208E 02	1.6705E 01	2.3107E 03	-1.3253E 02
-4.	.631E 03	2.7663E 02	2.8453E 03	-1.4868E 02	2.9266E 01	3.6733E 00	-5.0763E 02	-1.4170E 00	1.0999E 03	1.2609E -01
-6.	.153E 02	-3.086E 01	2.0386E 02	2.2580E 01	-4.4601E 03	1.4292E 01	3.7757E 03	3.9014E 01	-1.3541E 03	-2.5801E 01
-2.	.379E 03	1.2697E 01	6.4277E 03	2.7009E 01	-5.1578E 03	-7.5374E 01	1.6870E 03	4.6730E 01	2.2048E 03	-1.3700E 01
-4.	.192E 03	-1.7185E 01	4.2020E 03	4.7641E 01	-1.4662E 03	-3.0775E 01	-5.3205E 02	3.2073F 00	1.1658E 03	5.9644E 00
-9.	.357E 02	-1.6742F 01	2.7553F 02	1.0039E 01						

R54 = 22

-2.	.6466E 01	2.1446E 01	2.3579E 02	-1.5065E 01	-4.9956E 02	3.1196E 01	2.9260E 02	-1.5971E 01	4.1775E 01	-2.2550E 00
-3.	.574E 02	1.8841E 01	7.9554E 02	-3.8820F 01	-4.6174E 02	1.9568E 01	-4.3297E 01	2.8412E 00	3.6493E 02	-2.2008E 01
-7.	.131E 02	4.664E 01	4.5022E 02	-2.4962E 01	-4.1075E 00	1.4876E 00	-2.6701E 01	-5.4707E 00	6.3762E 01	1.0738E 01
-3.	.526E 01	-6.7386E 01	3.6333E 02	-1.7022E 00	-1.7471E 03	8.0924E -01	2.5222E 03	1.7823E 01	-1.9430E 03	1.0430E 01
-5.	.5655E 02	3.3985E 02	2.5001E 03	-3.1857F 01	-3.4744E 03	-2.9156E 01	1.5398E 03	2.8482E 01	4.1184E 02	-2.0035E 01
-1.	.692E 03	6.3365E -01	2.7154E 03	2.0591E 01	-1.2379E 03	-2.1647E 01	-7.1216E -01	4.5302F 02	1.5506E 02	1.5506E 01
-6.	.98E 02	-6.3598F 01	2.6653E 02	5.4552E 00						

R54 = 23

2.	.366E 01	-1.249E 00	-2.1564E 02	1.0332E 01	4.5582E 02	-2.1143E 01	-2.6458E 02	1.0059E 01	-5.3377E 01	2.7796E 00
4.	.74E 02	-2.3569E 01	-9.8961E 02	4.8588E 01	5.74465E 02	-2.4456E 01	4.4891E 01	-2.4809E 00	-3.0740E 02	2.0742E 01
3.	.76 E 02	-4.3164E 01	-4.7422E 02	2.7994E 01	-2.1084E 01	1.1375E 00	1.4876E 02	-9.8811E 00	-3.8422E 02	2.0838E 01
2.	.266E 02	-1.1738E 01	-6.6773E 02	9.8946E 00	1.2205E 03	3.2072E 00	-2.6339E 02	-1.1276E 01	-1.0876E 02	-4.8823E -02
1.	.719E 03	-1.3145E 01	-1.8634E 03	-5.5085E 00	5.6233E 02	1.7345E 01	1.6900E 02	-1.9500E 01	-8.3776E 02	1.0588E 01
1.	.195E 02	3.7546E 00	-5.0841E 02	-1.2658E 01	-1.9333E 02	3.2097E -01	2.0916E 02	-2.2580E 00	-3.5316E 02	-1.1529E 00
1.	.456E 02	3.3662E 03	1.6444E 01	-6.1242F 01						

R54 = 24

2.	.366 01	-1.249E 00	-2.1564E 02	1.0332E 01	4.5582E 02	-2.1143E 01	-2.6458E 02	1.0059E 01	-5.3377E 01	2.7796E 00
4.	.74E 02	-2.3569E 01	-9.8961E 02	4.8588E 01	5.74465E 02	-2.4456E 01	4.4891E 01	-2.4809E 00	-3.0740E 02	2.0742E 01
3.	.76 E 02	-4.3164E 01	-4.7422E 02	2.7994E 01	-2.1084E 01	1.1375E 00	1.4876E 02	-9.8811E 00	-3.8422E 02	2.0838E 01
2.	.266E 02	-1.1738E 01	-6.6773E 02	9.8946E 00	1.2205E 03	3.2072E 00	-2.6339E 02	-1.1276E 01	-1.0876E 02	-4.8823E -02
1.	.719E 03	-1.3145E 01	-1.8634E 03	-5.5085E 00	5.6233E 02	1.7345E 01	1.6900E 02	-1.9500E 01	-8.3776E 02	1.0588E 01
1.	.195E 02	3.7546E 00	-5.0841E 02	-1.2658E 01	-1.9333E 02	3.2097E -01	2.0916E 02	-2.2580E 00	-3.5316E 02	-1.1529E 00
1.	.456E 02	3.3662E 03	1.6444E 01	-6.1242F 01						

R54 = 25

-4.	.335E 01	4.2571E 01	2.7334E 02	-2.6615E 01	-7.8906E 02	5.46662E 01	4.6234E 02	-2.8633E 01	7.66665E 01	-3.0461E 00
-2.	.2424E 02	-3.2508E 02	1.5234E 03	-6.6020E 01	-7.83A38E 02	3.2494E 01	6.7582E 01	-5.0705E 02	-4.4123E 01	-2.4763E 00
-1.	.568E 01	7.9754E 01	-5.4774E 02	-5.3590E 01						

R54 = 26

**NOT REPRODUCIBLE**

ROW = 26	-8.033E 0.	9.6116E-11	6.8351E 01	-5.7602E 00	-1.4468E 02	1.1907E 01	8.5319E 01	-6.4041F 00	1.0211E 01	-5.4684E-01
-1.89E 02	4.5689E 03	2.1410E 02	-9.2599E 00	-1.2347E 02	4.5518E 00	-1.2296E 01	8.8346E-01	1.1833E 02	-7.3361E 00	
-2.538E 02	1.5566E 01	1.7979E 02	-8.5044E 00	-2.8065E 01	2.8261E 02	-1.6006E 02	-1.6169E 01	-3.2922E 02	3.3230E 01	
-1.7728E 02	-1.9257E 01	1.1013E 02	-4.1617E-01	-4.9705E 02	6.6486E-01	7.2970E 02	3.5009E 00	-3.4279E 02	-4.6774E 00	
-1.538E 02	1.2096E 00	7.7671E 02	-8.4070E-02	-1.0559E 03	-9.1239E 00	4.5957E 02	8.6143E 00	2.0930E 02	-8.58629E-01	
-9.1365E 02	4.1279E-01	1.4486E 03	1.0478E 01	-6.7114E 02	-1.1438E 01	-2.1769E 01	3.1282E-01	7.0896E 01	-9.7942E-02	
-6.-7.766E 01	-1.2271E 00	1.6641E 01	6.39969E-01							
ROW = 27	5.752E 01	-2.1919E-01	-5.4193E 01	2.0154E 01	1.1411E 02	-4.0663E 00	-6.5774E 01	1.7402E 00	-1.8434E 01	9.0384E-01
1.-2.86E 02	-7.7933E 01	-3.337E 02	1.5781E 01	1.9899E 02	-7.8344E 01	1.7471E 01	-8.3420E 01	1.5870E 02	7.6904E 00	
3.552E 02	-1.5987E 01	-1.9436E 02	8.3331E 00	-3.6292E 03	-8.2933E-03	4.3525E 01	-9.8609E 01	-9.2307E 01	2.0473E 00	
5.412E 01	-9.4397E-01	-2.3937E 02	2.8245E 01	3.2839E 02	7.8340E-01	-5.6259E 01	-3.0239E 00	-6.3022E 01	-2.0751E-01	
3.537E 02	-3.8694E 01	-5.9496E 02	-1.8343E 00	2.0596E 02	5.5222E 00	3.4592E 01	-9.3292E-01	-4.3254E 02	5.7845E 00	
6.-659E 02	1.8778E 01	-1.2002E 02	-6.4395E 01	-1.2431E 02	-2.5392E-01	3.7939E 01	-9.6994E-02	-7.4973E 01	-3.3088E-01	
6. 930E 01	7.1402E-01	-2.0891E 01	-5.3439E-01							
ROW = 28	1.2989E 01	-8.1266E-01	-1.1312E 02	5.9237E 00	2.3863E 02	-1.2027E 01	-1.3856E 02	5.8772E 00	-3.1400E 01	1.5813E 00
2.6255E 02	-1.3631E 01	-5.9641E 02	2.7484E 01	3.4537E 02	-1.3659E 01	3.0844E 01	-1.6448E 01	-2.6252E 02	1.4677E 01	
5.4908E 02	-3.0662E 01	-3.449E 02	1.6207E 01	8.0918E 03	-1.3603E 00	-1.3505E 01	6.2712E 00	2.3732E 01	-1.2844E 01	
-1.-347E 01	7.7929E 00	-4.1899E 02	5.2152E 01	1.1039E 03	-2.1141E 00	-1.0231E 03	-5.6867E 00	3.3829E 02	3.6045E 01	
7.-466E 02	-7.963E 01	-2.9632E 03	2.9545E 02	1.7971E 03	1.2104E 01	0.0866E 02	-8.2671E 00	8.4332E 02	1.0611E 01	
2.-253E 01	-3.0016E 00	-2.0606E 03	-1.3696E 01	6.7895E 02	8.6617E 00	8.3177E 01	-5.7338E-01	-2.2995E 02	-9.3523E-02	
2.-45E 02	1.799E 01	-8.3667E 01	-1.4052E 00							
ROW = 29	3.-46E 02	-1.7125E 01	-3.2874E 03	1.4814E 02	6.9453E 03	-3.0215E 02	-4.0301E 03	1.4116E 02	-6.3892E 02	4.3098E 01
7.-482E 02	-3.6337E 02	-1.5516E 04	7.4868E 02	9.0099E 03	-3.7590E 02	6.7782E 02	-3.6124E 01	-5.8145E 03	3.0402E 02	
1.-244E 04	-6.2325E 02	-7.1288E 03	3.2858E 02	-3.7303E 02	2.2725E 01	3.1078E 03	-1.8109E 02	-6.5337E 03	3.7705E 02	
3.-796E 03	-5.0895E 02	-4.8394E 03	2.9131E 01	1.0538E 01	4.5923E 01	8.4763E 03	-1.7240E 02	2.7729E 03	7.9139E 01	
8.-319E 02	-5.5086E 01	-1.9617E 04	-7.9469E 01	1.5923E 04	2.2150E 02	-5.2981E 03	-1.3850E 02	-5.3059E 03	3.2351E 01	
1.-579E 04	4.9659E 01	-9.3374E 03	-1.3859E 02	3.0670E 03	8.6167E 01	1.8045E 03	-1.1165E 01	-3.9625E 03	-1.5767E 01	
7.-158E 03	4.4208E 01	-1.6976E 03	-2.7722E 01							
ROW = 30	5.-6677E 01	-2.4919F 01	-4.9859E 02	2.2077E 01	1.0533E 03	-4.4995E 01	-6.1080E 02	2.0883E 01	-1.2893E 02	6.6986E 00
1.-283E 03	-5.6254E 01	-2.3821E 03	1.5942E 02	1.3833E 03	-5.8284E 01	1.0168E 02	-5.3931E 00	-6.7417E 00	4.5254E 01	
1.-443E 03	-9.3661E 01	-1.6681E 03	4.9323E 01	-5.8690F 01	1.7917E 00	4.8262E 02	-2.9371E 01	-1.0135E 03	6.1059E 01	
5.-584E 02	-5.3962F 01	-9.2999E 02	5.4953E 00	4.1147E 03	-2.8464E-01	-5.7229E 03	-4.8551E 01	2.5379E 03	4.7325E 01	
1.-711E 04	-9.8874E 01	-7.6616E 03	1.3821E 00	1.0730F 04	8.7834F 01	-4.7880E 03	-8.7301E 01	-1.0109E 03	5.9478E 00	
4.-228E 03	-4.0801E-01	-6.3263E 03	-5.3595E 01	2.8142E 03	5.2462E 01	3.3754E 02	-1.8534E 00	-1.5508E 03	1.66672E-01	
2.-46E 03	1.8334E 01	-9.3129E 02	-1.8280E 01							
ROW = 31	-7.-48E 01	3.6160F 01	2.3146E 02	-3.0265E 01	-1.3345E 03	6.1938E 01	7.7506E 02	-2.9465E 01	1.5455E 02	-8.1112E 00
-1.-482E 04	6.8518E 01	2.4687E 03	-1.4125E 02	-1.6652E 03	7.1152E 01	-1.2133E 02	6.6841E 00	1.0436E 03	-5.5557E 01	
-2.-687F 02	1.1517E 02	1.2767E 03	-6.0947E 01	5.4776E 01	-3.0210E 00	-4.7829E 02	2.6067E 01	1.076F 03	-5.4422E 01	
5.-42F 12	2.9925E 01	1.6625E 03	-2.1650F 01	-1.6617E 03	-9.2571E 00	9.1385E 02	2.9029F 01	2.8509E 02	-3.4458E 00	
-1.-52F 11	4.1932E 01	1.6383E 03	-1.6137E 01	-5.2496E 01	-1.5150F 00	-6.9350E 02	4.7577F 00	-1.452F 03	-2.4012E 01	
-3.-11E 04	-1.095F 01	0.7231E 02	3.2027E 01	1.7339F 02	-3.5150F 02	8.3838F 00	1.1299F 03	3.4134E 00		
-3.-25F 12	-1.1753E 01	-1.3219E 02	7.1500F-01							
ROW = 32	-1.-962E 02	6.4139E 00	1.1462E 03	-5.4467E 01	2.4129E 03	1.1134E 02	-1.4050E 03	-3.2818E 01	2.8230E 02	-1.4873E 01
-1.-452E 04	5.6212E 02	2.4627E 03	-1.4227E 02	2.4027E 02	1.4770E 02	-1.4770E 02	1.4770E 02	-1.4770E 02	1.4770E 02	-1.4770E 02

-5.	-225E 07	2.6709E 02	2.2245E 03	-1.0953E 02	1.0152E 02	-5.8813E 00	-6.7547E 02	4.9387F 01	1.8428F 03	-1.0297E 02
-5.	.59 E 01	5.6707E 01	3.7169E 03	-4.2925E 01	-9.8610E 03	1.2447E 01	9.2562E 03	6.3215E 01	-3.1063E 03	-4.2293E 01
-6.	-32E 03	8.0550E 01	1.8222E 04	-2.4602E 01	-1.7077E 04	4.1418F 02	5.7265E 03	7.5999E 01	4.0589F 03	-4.7270E 01
-7.	-84E 14	1.3519E 01	1.0117E 04	7.0204E 01	-3.3922E 03	-4.6667F 01	-1.3615E 03	1.6095E 01	3.6355E 03	-4.2501E 00
-3..	-58F 6	-2.4606F 0.	1.1419E 03	1.5990E 01						

PART IV - SECTION B4.0

LISTING OF SUBSONIC AIC COMPUTER PROGRAM

```

      CMAIN      MAIN
      COMPLEX A,AA,ANM,CZERO,WASH,AIC
      DIMENSION TEMP(40,40),AIC(40,40),WASH(40),FM(40,40)
      COMMON/C1/A(40,40),AA(40,40),ANM(40,40),CZERO
      COMMON/C2/HKFR(20),ZKER(20),FMACH(6),FREQ(10),NOM(5),IL(60),
      1          HCOR(6),ZCOR(6),WXCHN(11),WBCN(11),WRIN(11),WT(90),
      2          XE(5),YE(5),UX(10),UY(10),WXIMN(11),SIX(40),SCX(10,2),
      3          ETAC(1)
      COMMON/C3/Y(11),XAIC(10,10,2),YAIC(10,2),B(40,40),R(40,40),
      1          C(10,40),T(40,40),TM(40,40),TR(40,40),TI(40,40)
      COMMON/C4/CLFN,NGSKRN,NPY,SOUND,NMACH,NFREQ,MAUG,NIONCX,RHO,
      6          NMODES,LCOLL,LPRWSH,LPRCO,IIY,IIX,NSURF,ISOLAT,FM,FC,
      /          NCOLS,NOMIT,MACH,XCOLL,YCOLL,PI,U,QWCX,CXMN,IMOD,IRON,
      8          EM,FK,B,NWIX,NCIX,CRON,NWCY,IFR,E1,E2,QWY,QWGX,
      9          SN,WRO,NIY,NWCX,NCCX,NWPX,NCPX,NXWING,NYWING,NXCS,NYCS
      COMMON/C5/LPUNCH,KF
      EQUIVALENCE (AA,AIC),(A,WASH),(FM,T)

C ***
C ***
      WRITE(6,66)
      66 FORMAT(1H1)
      1 CALL KFDA
      FW = 2*NWIX + 1
      FC = 2*NCIX + 1
      QWGX = 2.0*PI/FW
      QWCX = 2.0*PI/FC
      QWY = PI/FLOAT(2*NIY)
      CALL GEOM
      CALL TRAMP(NIY,NWCX,NCCX,NXWING,NYWING,NXCS,NYCS,2,WRO,SN)
      NRS=NIY*(NWCX+NCCX)
      NCS=NXWING+NYWING+NXCS+NYCS
      DO 100 NIT=1,NRS
      DO 200 MIT=1,NCS
      200 TEMP(NIT/MIT)=TR(NIT/MIT)
      CALL TRAMP(NIY,NWCX,NCCX,NXWING,NYWING,NXCS,NYCS,1,WRO,SN)
      DO 201 NIT=1,NRS
      DO 201 MIT=1,NCS
      201 TR(NIT/MIT)=TEMP(NIT/MIT)
      DO 100 MACH=1,NMACH
      MACH = MACH
      EM = FMACH(MACH)
      U = FM*SOUND
      RHO = WRO/U
      R2 = 1.0 - 1.0*EM
      CALL KOUT(1)
      IF (LCOLL .NE. 0) CALL KOUT(2)
      DO 100 IFR=1,NFREQ
      IFR = IFR
      IF (KF .EQ. 1) FREQ(IFR)=FREQ(IFR)*U/(WRO*2.0*PI)
      FK=1.0*PI*FRFO(IFR)*WRO/U
      NSURF = 1 (WTNA) OR 2 (CONTROL SURFACE)
      NCX = NWCX
      MOMIT = 1
      NMODES = NXWING+NYWING + NXCS+NYCS
      MAUG = NCOLS + NMODES
      DO 4 J=1,NCOLS
      TI(J) = 0
      DO 4 K=1,MAUG
      4 AAC(J,K) = CZERO
      IROW = 1
      DO 15 NSURF=1,2

```

NSURF = NSURF  
DO 14 IY=1,NTY  
IIY = IY  
IF(NOMIT-MOMIT.LT.0) GO TO 7  
IF(IY-NOM(MOMIT).EQ.0) GO TO 10  
7 YCOLL = SN\*Y(IY)  
DO 12 IX=L,NCX  
IIX = IX  
XCOLL= XS(1,NSURF,IX,IY)  
CALL CORD  
DO 10 M=1,NHONFS  
SR = IR(IRON,M)  
SI = II(IRON,M)\*EK/WBO  
MNC = NCOLS + M  
50 WASH(MNC) = CMPLX(SR,SI)  
DO 60 N=1,NCOLS  
60 CALL CGREFD(A,N,N)  
IROW = IRON + 1  
12 CONTINUE  
GO TO 14  
13 MOMIT = MOMIT + 1  
14 CONTINUE  
NCX = NCNX  
15 CONTINUE  
CALL XLSQ  
CALL ATCS  
CALL KOUT(6)  
IF (LPUNCH .NE. 0) CALL KOUT(/)  
160 CONTINUE  
GO TO 1  
END

```

CKFDA      KFDA
SUBROUTINE KFDA
COMPLEX A,AA,ANM,CZERO,WASH,AIC
DIMENSION AIC(40,40),WASH(40)
COMMON/C1/A(R**),AA(40,40),ANM(40,40),CZERO
COMMON/C2/HKFR(20),ZKER(20),FMACH(6),FRFQ(10),NOM(5),IL(50),
1      HCOR(6),ZCOR(6),WXCMN(11),HBCN(11),WRIN(11),WT(40),
2      XF(5),YE(5),UX(10),UY(10),WXIMN(11),SIX(40,1),SCX(30,1),
3      ETAC(11)
COMMON/C3/Y(11),XAIC(10,10,2),YAIC(10,2),B(40,40),R(40,40),
1      C(10,10),T(10,40),TM(40,40),TR(10,40),TI(40,10)
COMMON/C4/CLEN,NGSKRN,NPY,SOUND,NMACH,NFREQ,HAUG,NIONCX,RHO,
1      NNODES,LCOLL,LPRWSH,IPRCO,IIY,IIX,NSURF,ISOLAT,FH,FC,
2      NCOLS,NOMIT,MACH,XCOLL,YCOLL,P1,U,QWCX,CXMN,IMOD,IROW,
3      EM,ER,B,NWIX,NCTX,CRON,NWCY,IFR,E1,F2,QHY,QWWX,
4      SN,WRO,NIY,NWCX,NCCX,NWPX,NCPX,NXWING,NYWING,NXCS,NYCS
COMMON/C5/LPUNCH,KF
EQUIVALENCE (AA,AIC),(A,WASH)
11 FORMAT(6F12.8)
12 FORMAT(6I12)
READ(5,11)(XF(I),I=1,5)
READ(5,11)(YE(I),I=1,3),SOUND
RHO=1.0
READ(5,12) NMACH,KF,NFREQ,LCOLL,LPUUNCH
READ(5,12) NWCX,NCCX,NIONCX,NIY:ISOLAT
NWTS=0
NWPX=NWCX
NXWING=NWCX
NCPX=NCCX
NXCX=NCCX
NWCY=NIY
NPY=NIY
NYWING=NIY
NYCS=NIY
NCOLS=NPY*(NWPX+NCPX)
NCTX=NCCX*NIONCX
NWIX=NWCX*NIONCX
NWTS = NWCY*NWCX + NIY*NCCX
DO 40 I=1,NWTS
40 WT(I) = 1.0
IF(INWTS.NE.0) READ(5,11)(WT(I),I=1,NWTS)
NCOLS = NPY * (NWPX + NCPX)
NCTX = NCCX*NIONCX
NWIX= NWCX*NIONCX
NOMIT = 0
DO 41 I=1,5
41 NOM(I) = 0
IF(NWCY.0.E.NIY) GO TO 5
NOMIT = NIY-NWCY
READ(5,12)(NOM(I),I=1,NOMIT)
42 READ(5,11)(FMACH(I),I=1,NMACH)
DO 43 I=1,NMACH
43 IF(FMACH(I).LT.0.10) GO TO 7
WRITIE(6,13)
13 FORMAT(7H     A MACH NUMBER GREATER THAN 0.90 HAS BEEN READ IN---,
1CASE TERMINATED)
CALL EXIT
/ CONTINUE
READ(5,11)(FRFQ(I),I=1,NFREQ)
READ(5,11)(YAIC(1,1),I=1,NYWING)
READ(5,11)(YAIC(1,2),I=1,NYCS)

```

```
READ(5,11) ((XAIC(I,J,1),I=1,NXWING),J=1,NYHNG)
READ(5,11) ((XAIC(I,J,2),I=1,NXCS),J=1,NYCS)
IF(NCIX.GT.40.OR.NHIX.GT.40) GO TO 86
IF(NNCX+NHCY+NCCX+NIY.GT.90) GO TO 86
IF(NPY+(NWPX+NCPX).GT.50) GO TO 86
IF(NWPX.GT.10.OR.NCPX.GT.10.OR.NPY.GT.10) GO TO 86
RETURN
86 FM = FMACH(1)
CALL KOUT(1)
CALL KOUT(5)
RETURN
END
```

```

CKOUT      KOUT
SUBROUTINE KOUT(IND)
COMPLEX A,AA,ANH,CZERO,WASH,AIC
DIMENSION SURF(2,2),XPR(50),AIC(40,80),WASH(40)
COMMON/C1/A(80),AA(40,80),ANH(40,40),CZERO
COMMON/C2/HKFR(20),ZKER(20),FMACH(6),FREQ(10),NOM(5),IL(50),
1          HCOR(6),ZCOR(6),WXCMN(11),WBCN(11),WBIN(11),WT(90),
2          XE(5),YE(3),UX(10),UY(10),WXIMN(11),SIX(40,2),SCX(10,2),
3          ETA(11)
COMMON/C3/Y(11),XAIC(10,10,2),YAIC(10,2),B(40,40),R(40,40),
1          C(40,40),T(40,40),TM(40,40),TR(40,40),TI(40,40)
COMMON/C4/CLFN,NGSKRN,NPY,SOUND,NMACH,NFREQ,MAUG,N10MCX,RHO,
6          NMODFS,LCOLL,LPRWSH,LPRCO,IIY,IIX,NSURF,ISOLAT,FN,FC,
7          NCOLS,NOMIT,MACH,XCOLL,YCOLL,P1,U,QWCX,CXMN,IMOD,IROW,
8          EM,FK,B2,NWIX,NCIX,CBON,NWCY,IFR,E1,E2,QHY,QWDX,
9          SN,WB0,NIY,NWCX,NCCX,NWPX,NCPX,NXWING,NYWING,RXCS,NYCS
COMMON/C5/LPUNCH,KF
EQUIVALENCE (AA,AIC),(A,WASH),(XPR,IL)
DATA (SURF(1,1),I=1,2)/8HWING ,RHTAIL /
GO TO (10,20,30,40,50,60,70), IND
*****  

C
10 XV=XE(5)-XE(4)
XX=XE(3)-XE(2)
AW=2.0*(XE(3)*YE(3)-0.5*XE(2)*(YE(3)-YE(2)))
AT=2.0*XV*YE(3)
WRITE(6,11)EM,SOUND,RHO,XE(1),XE(4),XE(3),XV,YE(2),YE(3),YE(3),
1YE(3),XX,XV,AW,AT,NWCY,NIY,NWCX,NWIX,NCIX,NPY,NPY,NWPX,NCPX
11 FORMAT(1H1// 32X,41HHUGHES AIRCRAFT CO. SUBSONIC AIC PROGRAM
1 // 32X,30HFLIGHT CONDITIONS AND GEOMETRY/1H0//15X, 13HMACH NUMBER
2 =,F8.5,4X,16HSPEED OF SOUND =F10.3,4H L/T,4X,4HRHO=,E14.8//1H0/
354X,4HWING,18X,
3 4HTAIL//22X,16HL.E. STATION (L),2F22.3//22X,16HROOT CHORD (L),
4 2F22.3// 22X,16HL.F. SPAN (L),2F22.3//22X,16HT.E. SPAN (L),
5 2F22.3// 22X,16HTIP CHORD (L),2F22.3//22X,16HTOTAL AREA (L+L)
6 2F22.3//22X,16HSPAN COLL. STA.,I19,I22//22X,16HCHORD COLL. STA.
7 I19,I22//22X,16HCHORD INTG. STA.,I19,I22//22X,16HSPAN PRES MODES
8,I19,I22//22X,16HCHORD PRES MODES,I19,I22)
IF(FMACH(MACH).LE.0.95) GO TO 15
WRITE(6,14)
14 FORMAT(92H A MACH NUMBER GREATER THAN 0.95 HAS BEEN USED-----
1 USE CAUTION IN APPLYING CASE RESULTS)
15 IF(NOMIT.EQ.0) RETURN
WRITE(6,12)(NOM(I),I=1,NOMIT)
12 FORMAT(1H0,15X,51HTHE SPANWISE COLLOCATION STATION(S) OMITTED ON W
1ING,915)
RETURN
*****  

C
20 NCX=NWCX
NIX=NWIX
DO 150 NS=1,2
WRITE(6,22)(SURF(1,NS),I=1,2)
22 FORMAT(1H1,///30X,50HHUGHES AIRCRAFT CO. SUBSONIC AIC PROGRAM (CO
1INT-0) //////
220X,5,SHUNSTEADY AERO COLLOCATION STATION COORDINATES ON THE 2A6/1H
30,12H S STA NO,7X,2HYC,8X,/X,11HXC VALUES--)
DO 123 IY=1,NIY
YC=WB0*SN*Y(IY)
DO 120 IX=1,NCX
120 XPR(IX)=WB0*XS(1,NS,IX,IY)
123 WRITE(6,124) IY,YC,(XPR(IX),IX=1,NCX)

```

```

124 FORMAT(1H0,I12,5E17.6/(1H ,29X,4E17.6))
      WRITE(6,105) (SURF(I,NS),I=1,2)
105 FORMAT(1H0,24X,39HINTEGRATION STATION COORDINATES ON THE 2A6/1H0,
112H   S STA NO.7X,2HY1,8X,7X,11HXI VALUES--)
      DO 106 IY=1,NY
      YI=WBO*SH*ETA(IY)
      DO 126 IX=1,NIX
126 XPR(IX)=WBO*XS(2,NS,IX,IY)
106 WRITE(6,124) IY,YI,(XPR(IX),IX=1,NIX)
      NCX=NCCX
      NIX=NCIX
150 CONTINUE
      NXS=NXWING
      NYS=MYWING
      DO 200 NS=1,?
      WRITE(6,201) (SURF(I,NS),I=1,?)
201 FORMAT(1H1,///30X,50HHUGHES AIRCRAFT CO. SUBSONIC AIC PROGRAM (CO
1NT-D)      //////
228X,43HAIIC COLLOCATION STATION COORDINATES ON THE 2A6/1H0,
319X, 4HYAIC,13X,13HXAIC VALUES--)
      DO 202 IY=1,NYS
      YC=YAIC(IY,NS)
202 WRITE(6,203) YC,(XAIC(IX,IY,NS),IX=1,NXS)
      NYS=NYCS
200 NXS=NXCS
203 FORMAT(1H0,12X,5E17.6/(1H ,29X,4E17.6))
      RETURN
*****C*****
50 DO 34 NS = 1,2
      WRITE(6,21) FREQ(IFR),NMODES,EK,EM
21 FORMAT(1H1,31X,42HMISSILE SUBSONIC AIRLOADS PROGRAM (CONT-D)//1H /
1 9X,27HOSCILLATORY FREQUENCY (CPS),F12.5,14X,12,15H COLL. STATIONS
2 /1H0,8X,30HREDUCED FREQUENCY (SEMI-CHORD),F9.5,14X,23HFREE STREA
3M MACH NUMBER,F9.3/1H )
      WRITE(6,31) IMOD
31 FORMAT(31X,40HPRESSURE COEFFICIENTS FOR COLL. STA. NO.13//19X,1H11
21X,10HR COEFF(1)12X,10H1 COEFF(1) 9X,9HSPAN MODE 3X,10HCHORD MODE)
      WRITE(6,32)(SURF(KI,NS),KI=1,2)
32 FORMAT(1H0,9X,2A6//)
      GO TO(2,3),NS
? NL = NWPX
? ML = NPY
: IK = 1
: GO TO 4
3 NL = NCPX
ML = NPY
IK = NWPX+NPY+1
4 DO 6 IMM=1,ML
DO 6 INN=1,NI
      WRITE(6,33) IK,ANH(IK,IMOD),IMM,INN
33 FORMAT(1H0,119,1P/E22.5,2)13)
6 IK = IK + 1
34 CONTINUE
      RETURN
*****C*****
40 WRITE(6,41)
41 FORMAT(1H0,20X,58HERROR IN INPUT DATA (NO TAIL) REQUIRES//,21X,19H
1TERMINATION OF CASE)
      CALL EXIT
*****C*****
50 WRITE(6,51)

```

```

51 FORMAT(1H0,/9X,63HNUMBER OF COLLOCATION OR INTEGRATION STATIONS OR
1 PRFSSURE TERMS//1X,25HEXCEEDS ALLOWABLE MAXIMUM//35X,18HCASE IS
2 TERMINATED)
CALL EXIT
*****  

C 60 VEL=FM*SOUND
0=0.5*RHO*VEL**2
EK1=1.0/EK
REFC=(XE(3)-XE(1))/2.0
WRITE(6,220) FREQ(IFR),REFC,EK,EK1,EM,U,RHO,0
220 FORMAT(1H1,31X,5IH HUGHES AIRCRAFT CO. SURSONIC AIC PROGRAM (CONT
1-D)//9X,28H OSCILLATORY FREQUENCY (CPS),4X,1PE12.5./1H0,9X,15HRE
2FERFNC CHORD,4X,1PE12.5./1H0,9X,30HREDUCED FREQUENCY (REF. CHORD)
3.4X,1PE12.5./1H0,9X,29HREDUCED VELOCITY (REF. CHORD).4X,1PE12.5,
4/1H0,9X,23HFREF STREAM MACH NUMBFR.4X,1PE12.5./1H0,9X,20HFREE STRE
5AM VELOCITY,4X,1PE12.5./1H0,9X,7HDFNSITY,4X,0PF5+2./1H0,9X,33HDYNA
6MIC PRESSURE (1/2*RHO*VEL**2),4X,1PE12.5,///)
WRITE(6,221)
221 FORMAT(//35X,34HAERODYNAMIC INFLUENCE COEFFICIENTS,//1X,2HRL,10X,
12HIM,10X,2HRL,10X,2HIM,10X,2HRL,10X,2HIM,10X,2HRL,10X,2HIM,10X,2HRL
2L,10X,2HIM,/)
NROWS=NYWING*NXWING+NXCS*NYCS
DO 222 NROW=1,NROWS
WRITE(6,223)NROW
WRITE(6,224) (AIC(NROW,NCOL),NCOL=1,NROWS)
223 FORMAT(/ 5HROW = I2)
224 FORMAT(1P10E12.4)
222 CONTINUE
RETURN
*****  

C /0 NW=NXWING*NYWING
NC=NXCS*NYCS
NT=NW+NC
NW1=NW+1
GO TO (81,82,83,84),LPUNCH
81 CONTINUE
DO 301 I=1,NW
PUNCH 85, (AIC(I,J),J=1,NW)
301 CONTINUE
85 FORMAT (1P6F12.5)
RETURN
82 CONTINUE
DO 302 I=NW1,NT
PUNCH 85, (AIC(I,J),J=NW1,NT)
302 CONTINUE
RETURN
83 CONTINUE
DO 303 I=1,NW
PUNCH 85, (AIC(I,J),J=1,NW)
303 CONTINUE
DO 304 I=NW1,NT
PUNCH 85, (AIC(I,J),J=NW1,NT)
304 CONTINUE
RETURN
84 CONTINUE
DO 305 I=1,NT
PUNCH 85, (AIC(I,J),J=1,NT)
305 CONTINUE
1000 RETURN
END

```

GATCS

```
SUBROUTINE ATCS
COMPLFX A,AA,ANH,CZERO,WASH,AIC
DIMENSION AIC(40,40),WASH(40),FM(40,40)
COMMON/C1/A(40),AA(40,40),ANH(40,40),CZERO
COMMON/C2/HKER(20),ZKER(20),FMACH(6),FREQ(10),NOM(5),IL(50),
1      HCOR(6),ZCOR(6),WXCMN(11),WBCN(11),WRIN(11),WT(90),
2      XF(5),YE(5),UX(10),UY(10),WXIMN(11),SIX(40,2),SCX(10,2),
3      ETA(11)
COMMON/C3/Y(11),XAIC(10,10,2),YATC(10,2),B(40,40),R(40,40),
1      C(40,40),T(40,40),TH(40,40),TR(40,40),TI(40,40)
COMMON/C4/CLFN,NGSKRM,NPY,SOUND,NMACH,NFREQ,MAUG,N10CX,RHO,
6      NMODES,LCOLL,LPRMSH,LPRCO,IIY,IIIX,NSURF,ISOLAT,FH,FC,
7      NCOLS,NOMET,MACH,XCOLL,YCOLL,P1,U,QWCX,CXMN,IMOD,IROW,
8      EM,EK,R2,NWIX,NCIX,CHON,NWCY,IFR,E1,E2,QHY,QWX,
9      SN,WRO,NIY,NWCX,NCCX,NWPX,NCPX,NXWING,NYWING,NXCS,NYCS
EQUIVALENCE (AA,AIC),(A,WASH),(FM,T)
NCOLS=NPY*(NWPX+NCPX)
NROWS=NXWING+NYWING+NYCS+NXCS
CALL FORCE
DO 100 I=1,NROWS
DO 100 J=1,NCOLS
SR=FM(I,J)
SI=0.0
200 AA(I,J)=COMPLX(SR,SI)
DO 300 I=1,NROWS
DO 300 J=1,NCOLS
A(J)=(0.0,0.0)
DO 400 K=1,NCOLS
200 A(J)=A(J)-AA(I,K)*ANH(K,J)
DO 225 I=1,NROWS
225 AIC(I,I)=(YE(1)-YE(1))*A(L)/(1.0*EK**2)
300 CONTINUE
RETURN
END
```

```

CCGRFD      CGRED
SUBROUTINE CCGRFD(V,IR,IC)
COMPLEX ANM,CZFR0,AIC,WASH
DIMENSION AIC(40,80),WASH(40),V(2,1)
COMMON/C1/A(?,80),AA(2,40,80),ANM(40,40),CZERO
COMMON/C2/HKFR(20),ZKER(20),FMACH(6),FREQ(10),NOM(5),IL(50),
1          HCOR(6),ZCOR(6),WXCMN(11),WBCN(11),WBIN(11),WT(90),
2          XE(5),YE(3),UX(10),UY(10),WXIMN(1L),SEX(40,2),SCX(10,2),
3          ETA(11)
COMMON/C3/Y(11),XAIC(10,10,2),YAIC(10,2),B(40,40),R(40,40),
1          C(40,40),T(40,40),TM(40,40),TR(40,40),TI(40,40)
COMMON/C4/CLFN,NGSKRN,NPY,SOUND,NMACH,NFREQ,MAUG,NIONCX,RHO,
6          NMODES,LCOLL,LPRWSH,LPRCO,IIY,IIX,NSURF,ISGLAT,FN,FC,
7          NCOLS,NOMIT,MACH,XCOLL,YCOLL,PI,U,ONCX,CXMN,IMOD,IERM,
8          FM,FK,R/,NWIX,NCIX,CRON,NWCY,IFR,E1,E2,ONY,ONW,
9          SN,WRO,NIY,NWCX,NCCX,NWPX,NCPX,NXWING,NYWING,NXCS,NYCS
EQUIVALENCE (AA,AIC),(A,WASH)
RMN = SORT(AA(1,IR,IC)**2 + AA(2,IR,IC)**2)
IF(AA(2,IR,IC).LE.E2) GO TO 34
CR = AA(1,IR,IC)/RMN
CI = AA(2,IR,IC)/RMN
DO 10 N=IC,MAUG
   TI = CR*AA(1,IR,N) + CI*AA(2,IR,N)
   AA(2,IR,N) = CR*AA(2,IR,N) - CI*AA(1,IR,N)
20 AA(1,IR,N) = TI
30 RAN = SORT(V(1,IC)**2 + V(2,IC)**2)
IF(RAN.LE.E2) GO TO 60
RAN = SORT(RAN**2 + RMN**2)
CR = V(1,IC)/RAN
CI = V(2,IC)/RAN
RMN = RMN/RAN
DO 40 N=IC,MAUG
   AIR = RMN*AA(1,IR,N) + CR*V(1,N) + CI*V(2,N)
   AII = RMN*AA(2,IR,N) + CR*V(2,N) - CI*V(1,N)
   VR = RMN*V(1,N) - CR*AA(1,IR,N) + CI*AA(2,IR,N)
   VI = RMN*V(2,N) - CR*AA(2,IR,N) - CI*AA(1,IR,N)
   AA(1,IR,N) = AIR
   AA(2,IR,N) = AII
   V(1,N) = VR
50 V(2,N) = VI
60 RETURN
END

```

## CFORCE

SUBROUTINE FORCE

```

DIMENSION FM(40,40)
COMMON/C3/Y(11),XATC(LB,10,2),YATC(10,2),B(40,40),R(10,40),
1      C(40,40),T(40,40),TM(40,40),TR(40,40),TI(40,40)
COMMON/C2/HKFR(20),ZKER(20),FMACH(6),FREQ(10),NOM(5),IL(50),
1      HCOR(6),ZCOR(6),WCMMN(11),WBCN(11),WRIN(11),WT(90),
2      XE(5),YE(3),UX(10),UY(10),WXIMN(11),SIX(40,2),SCX(10,2),
3      ETA(11)
COMMON/C4/CLEN,NGSKRN,NPY,SOUND,NMACH,NFREQ,MAUG,NIONCX,RHO,
6      NMODES,LCOLL,LPRHSH,LPRCG,IIY,IIX,NSURF,ISOLAT,FH,FC,
7      NCOLS,NOMIT,MACH,XCOLL,YCOLL,P1,U,WCX,CXMM,IMOD,IRW,
8      EM,EK,B2,NWIX,NCIX,CRON,NWCY,IFR,E1,E2,WNW,WNWX,
9      SN,WRO,NIY,NWCX,NCCX,NWPX,NCPX,NXWING,NYWING,NXCS,NYCS
EQUIVALENCE (FM,T)
MROWS=NIY*(NWGX+NCCX)
MCOLS=NPy*(NWPX+NCPX)
DO 100 I=1,MROWS
DO 100 J=1,MCOLS
100 FM(I,J)=0.0
C *** BEGIN TO ASSEMBLE FM(IRW,ICOL) MATRIX STARTING WITH WING
IRW=1
DO 300 I=1,NIY
IF (I.EQ.1) GO TO 105
IF (I.EQ.NIY) GO TO 110
SNL=(0.5*(YAIC(I-1,1)+YAIC(I,1))-YE(1))/(YE(3)-YE(1))
SNU=(0.5*(YAIC(I,1)+YAIC(I+1,1))-YE(1))/(YE(3)-YE(1))
GO TO 115
105 SNI=0.0
SNU=(0.5*(YAIC(1,1)+YAIC(2,1))-YE(1))/(YE(3)-YE(1))
GO TO 115
110 SNL=(0.5*(YAIC(NIY-1,1)+YAIC(NIY,1))-YE(1))/(YE(3)-YE(1))
SNU=1.0
115 CONTINUE
DO 400 J=1,NWGX
IF (J.EQ.1) GO TO 120
IF (J.EQ.NWGX) GO TO 125
CNL=(0.5*(XATC(J,1,1)+XAIC(J-1,1,1))-XE(1)-0.5*(XE(3)-XE(1)))/
1(0.5*(XF(3)-XF(1)))
CNU=(0.5*(XATC(J+1,1,1)+XAIC(J+1,1))-XE(1)-0.5*(XE(3)-XE(1)))/
1(0.5*(XE(3)-XF(1)))
GO TO 130
120 CNL=-1.0
CNU=(0.5*(XATC(1,1,1)+XAIC(2,1,1))-XE(1)-0.5*(XE(3)-XE(1)))/
1(0.5*(XE(3)-XF(1)))
GO TO 130
125 CNL=(0.5*(XATC(NWGX-1,1,1)+XAIC(NWGX,1,1))-XF(1)-0.5*(XE(3)-XE(1)))/
1(0.5*(XF(3)-XF(1)))
CNU=1.0
130 CONTINUE
ICOL=1
DO 700 K=1,NPY
CALL MINTS(K,SNL,SNU,FS)
DO 700 L=1,NWPX
CALL MINTC(L,CNL,CNU,FC)
FM(IRW,ICOL)=FS*FC
700 ICOL=ICOL+1
700 IRW=IRW+1
C *** ASSEMBLE CONTROL SURFACE CONTRIBUTION
DO 600 I=1,NIY
IF (I.EQ.1) GO TO 505

```

```

IF (I .EQ. NIY) GO TO 510
SNL=(0.5*(YAIC(I-L,2)+YAIC(I,2))-YE(1))/(YE(3)-YE(1))
SNU=(0.5*(YAIC(I,2)+YAIC(I+1,2))-YE(1))/(YE(3)-YE(1))
GO TO 515
505 SNL=0.0
SNU=(0.5*(YAIC(1,2)+YAIC(2,2))-YE(1))/(YE(3)-YE(1))
GO TO 515
510 SNL=(0.5*(YAIC(NIY-1,2)+YAIC(NIY,2))-YE(1))/(YE(3)-YE(1))
SNU=1.0
515 CONTINUE
DO 600 J=1,NCCX
IF (J .EQ. 1) GO TO 720
IF (J .EQ. NCCX) GO TO 725
CNL=(0.5*(XAIC(J,1,2)+XAIC(J-1,1,2))-XE(4)-0.5*(XE(5)-XE(4)))/
1(0.5*(XF(5)-XF(4)))
CNU=(0.5*(XAIC(J+1,1,2)+XAIC(J,1,2))-XE(4)-0.5*(XE(5)-XE(4)))/
1(0.5*(XF(5)-XF(4)))
GO TO 730
720 CNL=-1.0
CNU=(0.5*(XAIC(1,1,2)+XAIC(2,1,2))-XE(4)-0.5*(XE(5)-XE(4)))/
1(0.5*(XE(5)-XE(4)))
GO TO 730
725 CNL=(0.5*(XAIC(NCCX-1,1,2)+XAIC(NCCX,1,2))-XF(4)-0.5*(XE(5)-XE(4))-
1)/(0.5*(XE(5)-XE(4)))
CNU=1.0
730 CONTINUE
ICOL=NPY*NWPX+1
DO 400 K=1,NPY
CALL MINTS(K,SNL,SNU,FS)
DO 400 L=1,NCPX
CALL MINTC(L,CNL,CNU,FC)
FM(IROW,ICOL)=FS*FC
800 ICOL=ICOL+1
600 IROW=IROW+1
RETURN
END

```

```

CCORD      CORD
          SURROUNTE CORD
          COMPLEX A,AA,ANH,CZERO,WASH,AIC,AK,H2,TRM,D1,CRNL
          DIMFNSION AIC(40,80),WASH(40)
          COMMON/C1/A(R0),AA(40,80),ANH(40,40),CZERO
          COMMON/C2/HKFR(20),ZKER(20),FMACH(6),FREQ(10),NOM(5),IL(50),
1           HCOR(6),ZCOR(6),WXCMN(11),WBCN(11),WBIN(11),WT(90),
2           XE(5),YE(3),UX(10),UY(10),WXIMN(11),SIX(40,2),SCX(10,2),
3           ETA(11)
          COMMON/C3/Y(11),XAIC(10,10,2),YAIC(10,2),B(40,40),R(40,40),
1           C(40,40),T(40,40),TM(40,40),TR(40,40),TI(40,40)
          COMMON/C4/CLFN,NGSKRN,NPY,SOUND,NMACH,NFREQ,MAUG,NIONCX,RHO,
6           NMODFS,LCOLL,LPRWSH,LPRCD,IY,IIX,NSURF,ISOLAT,FW,FC,
7           NCOLS,NOMIT,MACH,XCOLL,YCOLL,PI,U,QWCX,CXMN,IMOD,IRW,
8           EM,EK,B2,NWIX,NCIX,CRON,NWCY,IFR,E1,E2,QWY,QWGX,
9           SN,WRO,NIY,NWCX,NCCX,NWPX,NCPX,NXWING,NYWING,NXCS,NYCS
          EQUIVALENCE (AA,AIC),(A,WASH)

C THIS SUBROUTINE CONSTRUCTS A ROW OF THE DOWNWASH MATRIX
C THE PRESSURE SERIES IS A PRODUCT OF CHEBYSHEV POLYNOMIALS IN THE
C NEGATIVE OF PERCENT SEMI-CHORD FROM THE MID-CHORD AND PERCENT
C SEMI-SPAN FROM THE ROOT.

DO 6 JC=1,NCOLS
6  A(JC) = CZERO
  IC1 = 0
  NIX = NWIX
  QWX = -QWGX*SN**2/(8.0*PI)
  NPX = NWPX
C THE DO 14 LOOP COMPUTES THE NON-SINGULAR PORTION OF R(N,M)
C DUE TO BOTH SURFACES
  DO 14 MSURF=1,2
    IF(MSURF.NE.NSURF.AND.ISOLAT.NF.0) GO TO 13
    DO 12 IY=1,NIY
      ETAI = SN*ETA(IY)
      ET2 = ETAI(IY)**2
      IF(NPY.GT.1) CALL CHEB(NPY-1,ETAI,UY(2))
      UY(1) = 1.0 -ET2
      DO 3 K=2,NPY
3   UY(K) = ET2*UY(1)*UY(K)
      DO 10 IX=1,NIX
        XI = XS(?,MSURF,IX,IY)
        XID = XCOLL -XI
        AK = CRNL(EK,XID,YCOLL-ETAI,EM,B2) + CRNL(EK,XID,YCOLL+ETAI,EM,B2)
        IC = IC1 +1
        H2 = AK*QWX*QWY
        IF(NPX.GT.1) CALL CHEB(NPX-1,-SIX(IX,MSURF),UX(2))
        UX(1) = 1.0 -SIX(IX,MSURF)
        DO 4 K=2,NPX
4   UX(K) = (1.0 +SIX(IX,MSURF))*UX(1)*UX(K)
C     ** ADD AN INCREMENT TO EACH ELEMENT OF THE ROW FOR (XI,ETAI) **
        DO 10 NY=1,NPY
          TRM = H2 * UY(NY)
        DO 10 NX=1,NPX
          A(IC) = A(IC) +TRM*UX(NX)
10  IC = IC+1
C     ** IC EQUALS NPY*NWPX+1 AT THE END OF THE FIRST PASS **
12  CONTINUE
13  NIX = NCIX
  QWX = -QWCX*SN**2/(8.0*PI)
  NPX = NCPX
14  IC1 = NPY*NWPX
  IC1 = 0

```

```

NPX = NWPX
XCOLS = XS(1,NSURF,IIX,IIY)
Y2 = Y(IIY)**/2
CALL CHEB(NPY-1,Y(IIY),UY(2))
UY(1) = -2.0
DO 15 K=2,NPY
15 UY(K) = -2.0*Y2*UY(K)
DO 40 MSURF=1,NSURF
C   ** THIS LOOP ADDS THE CONTRIBUTION OF THE SINGULAR INTEGRAL
      ALONG THE LINE FROM THE WING L.F. TO THE COLLOCATION POINT
      IF(MSURF.NE.NSURF.AND.ISOLAT.NE.0) GO TO 23
      IF(NSURF.LE.MSURF) GO TO 16
      UPLIM = PI
      GO TO 18
16 XT = SCX(IIX,NSURF)
      UPLIM = -ATAN(SQRT(1.0-XT**2)/XT)
      IF(UPLIM.LT.0.0) UPLIM=UPLIM+PI
18 QWSNG = FLOAT(2*NIY)*UPLIM/8.0
      DO 22 N=1,6
      IC = IC+1
      C   ** THIS LOOP CONSTRUCTS D(n,m) ,M=0,1,...,NPX-1
      VINT = UPLIM*ZCOR(N)
      C = COS(VINT)
      CALL CHEB(NPX-1, C,UX(2))
      UX(1) = 1.0 +C
      DO 19 K=2,NPX
19 UX(K) = (1.0 -C)*UX(1)*UX(K)
      ARG = EK*(XCOLS -WXCMN(IIY) +C*WRCN(IIY))
      IF(MSURF.EQ.2) ARG=EK*(XCOLS-CXHN+C*CBON)
      C1 = COS(ARG)
      S1 = SQRT(1.0 -C1**2)
      D1 = CMPLX(C1,-S1)*HCOR(N)
      DO 22 NY=1,NPY
      TRM = QWSNG*UY(NY)*D1
      DO 22 NX=1,NPX
      A(IC) = A(IC) +TRM*UX(NX)
22 IC = IC+1
23 IC1 = NPY*NWDX
40 NPX = NCPX
      RETURN
      END

```

```

CCRN1      CRNL
  COMPLEX FUNCTION CRNL(CK,X,Y,CH,R2)
  COMMON/C2/HKFR(20),ZKER(20),FMACH(6),FRDQ(10),NUM(5),IL(50),
  1      HCDR(6),ZCDR(6),WXCKN(11),WBCN(11),WBIN(11),WT(90),
  2      XF(-1,Y(-1),UX(10),UY(10),WXIMN(11),SIX(40),SCX(10,Z),
  3      FTA(11))
  COMMON/C4/CLFN,NGSKRN,NPY,SOUND,NMACH,NFREQ,MAUG,N10,CX,RHO,
  4      NMODES,LCOLL,LPRMSH,LPRCO,IIY,IIX,NSURF,ISLAT,FH,FC,
  5      NCOLS,NOMIT,MACH,XCOLL,YCOLL,P1,U,ONCX,CXMN,IMOD,IRON,
  6      EH,EK,R1,NNIX,NCIX,CRON,NMCY,IFR,F1,E2,QWY,QWGX,
  7      SN,WRO,NIY,NHCX,NCCX,NMPX,NCPX,NXING,NYHNG,NXUS,NYCS
  R=AH*S(Y)
  R=R*R
  CK1 = CK*R
  R1 = R*R
  R3 = R*R
  R4 = R*R
  S2 = X*X + R1*R2
  S = SQRT(S)
  U1 = (CM*S-X)/(R1*R2)
  UK = CK1*U1
  U0 = R1 = 1.0*NGSKRN
  U2 = U1*ZKER(1)
  UZ2 = U2*S2
  R=UX*ZKER(1)
  F = HKFR(1)*SORT(1.0+UZ2)*UZ*U1
  G1=1.0+F*COS(G)
  G4=1.0+F*SIN(G)
  V = 1.0 - ZKER(1)*V
  F = HKFR(1)*V - V* EXP(-CK1*V)* SORT(1.0+V)
  G1=1.0+F
  G2 = G1 + G4
  XS = X/S
  IF(UK,NE,0..) GO TO 20
  F14 = 1.0
  GO TO 21
  22 F14 = CK1*BESI(CK1)
  23 G1=CK1*R4-F14-XS*COS(UK)
  G2=CK1*R4+XS*SIN(UK)
  XK = CK*X
  CO = COS(XK)
  SI = SIN(XK)
  CHNI = CMPLX((CO*G1+SI*G2)/R2,(CO*G2-SI*G1)/R2)
  RETURN
END

```

```

CRFSI      RESL
FUNCTION BESL(X)
IF(X.GT.2.0)  GO TO 50
T=X/3.75
T=T*T
RSI1=0.5+T*(0.97890594+T*(0.51498869+T*(0.15084934+T*(0.01265875+T
1*(0.00301532+T*(0.00032411))))) )
RSI1=RSI1*X
Y=Y/2.0
RSK1=X*ALOG(Y)*RSI1+1.0
Y=Y*Y
RSK1=RSK1+Y*(0.15443144+Y*(-0.67278579+Y*(-0.18156897+Y*
1(-0.01919402+Y*(-0.00110404+Y*(-0.00004686))))))
RESI =RSK1/X
GO TO 60
50   Y=2.0/X
RSK1=1.25331414+Y*(0.23498619+Y*(-0.03655620+Y*(0.01504268+Y*
1(-0.00780354+Y*(0.00325614+Y*(-0.00068245))))))
RESI =RSK1/(SQR(X)*EXP(X))
50 RETURN
END

```

CCHER CHEB

```
SUBROUTINE CHEB(N1,X,UX)
DIMENSION UX(1)
DO 10 I=1,N1
10 UX(I) = 0.0
UX(1) = 1.0
UX(2) = 2.0*X
IF (N1.LT.3) RETURN
DO 20 I=3,N1
20 UX(I) = 2.0*X*UX(I-1) -UX(I-2)
RETURN
END
```

```

CCONS1      CONS1
BLOCK DATA
COMPLEX A,AA,ANM,CZERO,WASH,AIC
DIMENSION AIC(40,80),WASH(40)
COMMON/C1/A(80),AA(40,80),ANM(40,40),CZERO
COMMON/C2/HKER(20),ZKER(20),FMACH(6),FREQ(10),NOM(5),IL(50),
1      HCOR(6),ZCOR(6),WXCMN(11),WBCN(11),WBIN(11),WT(90),
2      XE(5),YE(3),UX(10),UY(10),WXIMN(11),SIX(40,2),SCX(10,2),
3      ETA(11)
COMMON/C4/CLEN,NGSKRN,NPY,SOUND,NMACH,WFREQ,WAUG,NIDNCX,RHO,
6      NMODFS,LCOLL,LPRWSH,LPRCO,IY,IIX,NSURF,ISLAT,FH,FC,
7      NCOLS,NOMIT,MACH,XCOLL,YCOLL,PI,U,QWCX,CXMN,IMOD,IRON,
8      EM,EK,B2,NWIX,NCIX,CRON,NWCY,IFR,E1,E2,QWY,QWHX,
9      SN,WRO,NIY,NWCX,NCCX,NWPX,NCPX,NXWING,NYHNG,NXCS,NYCS
EQUIVALENCE (AA,AIC),(A,WASH)
DATA PI/3.14159265/
DATA HCOR/0.08566225,0.18038079,0.2539569/,0.23395697,0.18038079,
10.08566225/
DATA ZCOR/0.03376524,0.16939531,0.38069041,0.61930959,0.85060469,
10.96673476/
C ***** NGSKRN SHOULD BE COMPATIBLE WITH HKER AND ZKER LISTS *****
C DATA NGSKRN/R/
DATA (HKFR(I),I=1,8)/0.05061427,0.11119052,0.15685332,0.18134189
X,0.18134189,0.15685332,0.11119052,0.05061427/
DATA (ZKER(I),I=1,8)/0.01985507,0.10166676,0.23723380,0.40828266
X,0.59171732,0.76276620,0.89833424,0.98014493/
C ***** END *****
C DATA E1/0.0000001/,E2/0.0000001/,CZERO/(0.0,0.0)/
END

```

```

CXS      XS
FUNCTION XS(L,NS,I3,J3)
COMMON/C2/HKER(20),ZKER(20),FMACH(6),FREQ(10),NOM(5),IL(50),
1      HCOR(6),ZCOR(6),WXCMN(11),WBCN(11),WBIN(11),WT(90),
2      XF(5),YE(3),UX(10),UY(10),WXIMN(11),SIX(40,2),SCX(10,2),
3      ETA(11)
COMMON/C4/CLFN,NBSKRN,NPY,SOUND,NMACH,NFREQ,MAUG,NIONCX,RHO,
6      NMODFS,LCOLL,LPRNSH,LPRCO,IIY,IIX,NSURF,ISOLAT,FN,FC,
7      NCOLS,NOMIT,MACH,XCOLL,YCOLL,PI,U,QWCX,CXMN,IMOD,IRW,
8      EM,EK,BZ,NWIX,NCIX,CRON,NWCY,IFR,E1,E2,QWY,QWX,
9      SN,WRO,NIY,NWCX,NCCX,NWPX,NCPX,NXWING,NYHNG,NXCS,NYCS
GO TO (10,40),L
10 GO TO (20,30),NS
20 XS = WXCMN(J3) + WBCN(J3) * SCX(I3,1)
      RETURN
30 XS = CXMN + CRON * SCX(I3,2)
      RETURN
40 GO TO (50,60),NS
50 XS = WXIMN(J3) + WBIN(J3) * SIX(I3,1)
      RETURN
60 XS = CXMN + CRON * SIX(I3,2)
      RETURN
END

```

```

C      XINT
FUNCTION XINT (IY,IX,NIY,NS,WBO,SN)
COMMON/C3/Y(11),XAIC(10,10,2),YAIC(10,2),B(40,40),R(40,40),
1           C(40,40),T(40,40),TM(40,40),TR(40,40),TI(40,40)
COMMON/C2/HKFR(20),ZKER(20),FMACH(6),FREQ(10),NOH(5),IL(50),
1           HCOR(6),ZCOR(6),WXCMN(11),WBCN(11),WBIN(11),WT(90),
2           XE(5),YE(3),UX(10),UY(10),WXIMN(11),SIX(40,2),SCX(10,2),
3           ETA(11)
IF (NS .EQ. 1) GO TO 200
XINT=WBO*XS(1,2,IX,1)
RETURN
200 IF (YAIC(IY,1) .GT. YE(2)) GO TO 300
XINT=WBO*XS(1,1,IX,1)
RETURN
300 SLOPE=(WBO*SN*Y(NIY)-YE(2))/(WBO*XS(1,1,IX,NIY)-WBO*YS(1,1,IX,1))
XIN1=WBO*XS(1,1,IX,1)+(YAIC(IY,1)-YE(2))/SLOPE
RETURN
END

```

CARCCOS

```
FUNCTION ARCCOS(X)
C *** DEFINE F(X)=A(0)+A(1)*X+A(2)*X**2+...+A(8)*X**8
C *** THEN ARCCOS(X)=F(X)*(1-X)**0.5 IF X.LT.1 AND .GT.0
C *** AND ARCCOS(X)=PI-(1-ABS(X))**0.5+F(ABS(X)) IF X.LT.0 AND .GT.-1
C *** ARCCOS(X) IN RADIANS *** VALID FOR 0 TO PI RADIANS
C *** ACCURATE TO AT LEAST 6 SIGNIFICANT FIGURES UNLESS X APPROACHES 1.0
A0=1.57079633
A1=-.21460184
A2=.08904567
A3=-.05072733
A4=.03313246
A5=-.02199838
A6=.01261235
A7=-.00499706
A8=.00095128
IF (X .GE. 0.0) GO TO 100
Z=AHS(X)
ARCCOS=3.1415927-(1.0-Z)**0.5*(A0+A1*Z+A2*Z**2+A3*Z**3+A4*Z**4
1+A5*Z**5+A6*Z**6+A7*Z**7+A8*Z**8)
RETURN
100 ARCCOS=(1.0-X)**0.5*(A0+A1*X+A2*X**2+A3*X**3+A4*X**4+A5*X**5
1+A6*X**6+A7*X**7+A8*X**8)
RETURN
END
```

```
CMINTC
      SUBROUTINE MINTC(IS,CNL,CNU,FC)
C *** CHORDWISE PRESSURE INTEGRATION
C *** CNL=LOWER INTEGRATION LIMIT
C *** CNU=UPPER INTEGRATION LIMIT
      CL=ARCCOS(CNL)
      CU=ARCCOS(CNU)
      SI=FLOAT(IS-1)
      IF (IS .EQ. 1) GO TO 10
      IF (IS .EQ. 2) GO TO 20
      FC=(SIN((SI+1.0)*CU))/(2.0*(SI+1.0))-(SIN((SI-1.0)*CL))/(2.0*(SI-
      1-1.0))-(
      2 (SIN((SI+1.0)*CL))/(2.0*(SI+1.0))+SIN((SI-1.0)*CL))/(2.0*(SI-
      1-1.0))
      GO TO 100
10  FC=SIN(CU)-CU-SIN(CL)+CL
      GO TO 100
20  FC=(SIN(2.0*CL))/4.0-CU/2.0-(SIN(2.0*CL))/4.0+CL/2.0
100 CONTINUE
      RETURN
      END
```

C MINTS

SUBROUTINE MINTS(SI, SNL, SNU, FS)  
C \*\*\* SPANWISE PRESSURE INTEGRATION  
C \*\*\* SNL=LOWER INTEGRATION LIMIT  
C \*\*\* SNU=UPPER INTEGRATION LIMIT  
SI=ARCCOS(SNL)  
SU=ARCCOS(SNU)  
IF (IS .EQ. 1) GO TO 10  
IF (IS .EQ. 2) GO TO 20  
IF (IS .EQ. 4) GO TO 40  
SI=FLOAT(SI-1)  
FS=(1.0/R.0)\*((1.0/(SI-1.0))\*  
1 (SIN((SI-1.0)\*SU)-SIN((SI-1.0)\*SL))  
2 -(1.0/(SI+1.0))\*  
3 (SIN((SI+1.0)\*SU)-SIN((SI+1.0)\*SL))  
-(1.0/(SI-3.0))\*  
-(1.0/(SI+3.0))\*  
GO TO 100  
10 FS=.5\*(SU-SI-SNU\*(1.0-SNU\*\*2)\*\*0.5+SNL\*(1.0-SNL\*\*2)\*\*0.5)  
GO TO 100  
20 FS=.25\*(SNU\*(1.0-SNU\*\*2)\*\*1.5-SNL\*(1.0-SNL\*\*2)\*\*1.5,  
1 .5\*(SU-SI-SNU\*(1.0-SNU\*\*2)\*\*0.5+SNL\*(1.0-SNL\*\*2)\*\*0.5))  
GO TO 100  
40 FS=(1.0/R.0)\*(SU-SL)+.25\*(  
1 (SIN(SU)\*COS(SU)-SIN(SL)\*COS(SL))  
2 -(2.0/3.0)\*(COS(SU)\*(SIN(SU)\*\*3)-COS(SL)\*(SIN(SL)\*\*5)))  
100 CONTINUE  
RETURN  
END

```

CXLSQ      XLSQ
SUBROUTINE XLSQ
COMPLEX A,AA,ANM,CZERO,WASH,AIC
DIMENSION AIC(40,40),WASH(40)
COMMON/C1/A(84),AA(40,40),ANM(40,40),CZERO
COMMON/C2/HKFR(20),ZKER(20),FMACH(6),FREQ(10),NOM(5),IL(50),
1          HCOR(6),ZCOR(6),WXCMN(11),WBCN(11),WBIN(11),WT(90),
2          XF(2),YE(4),UX(10),UY(10),WXIMN(11),SIX(40,2),SCX(10,2),
3          ET(11)
COMMON/C3/Y(11),XAIC(10,10,2),YAIC(10,2),B(40,40),R(40,40),
1          C(40,40),T(40,40),TM(40,40),TR(40,40),TI(40,40)
COMMON/C4/CLFN,NOSKRN,NPY,SCOND,NMACH,NFRED,MAUG,NIONCX,RHO,
6          NMODES,LCOLL,LPRWSH,LPRCO,IIY,IIX,NSURF,ISLAT,FN,FC,
7          NCOLS,NOMIT,MACH,XCOLL,YCOLL,PI,U,OWCX,CXMN,IMOD,IRW,
8          EH,FK,B,NWIX,NCIX,CRON,NWCY,IFR,E1,E2,QWY,OWX,
9          SN,WAO,NIY,NWCX,NCCX,NWPX,NCPX,NXWING,NYWING,NXCS,NYCS
EQUIVALENCE (AA,AIC),(A,WASH)
II = 1
DO 135 I=1,NCOLS
RII = CABS(AA(II,1))
IF(RII.LE.E2) GO TO 135
IL(1) = II
II = II + 1
GO TO 136
135 IL(1) = -1
II2 = NCOLS - 1 - (I-1)
DO 135 II=II,II2
135 CALL CGREFD(AA(II+1,1),II,I+1)
136 CONTINUE
C      SOLVE FOR THE COEFFICIENTS BY BACK SUBSTITUTION
140 II = NCOLS
DO 150 I = 1,NCOLS
DO 150 L=1,NMODES
150 ANM(I,L) = CZERO
DO 160 J=1,NCOLS
IF(IL(II).LE.0) GO TO 210
JI = IL(II)
DO 160 I=1,NMODOES
ML = NCOLS + L
IF(II-NCOLS) 170,190,220
170 IK = II + 1
DO 180 K=IK,NCOLS
180 ANM(II,1) = ANM(II,1) - AA(JI,K)*ANM(K,L)
190 ANM(II,1) = (ANM(II,L) + AA(JI,ML))/AA(JI,II)
200 CONTINUE
210 II = II - 1
220 RETURN
END

```

```

CGEOM      GEOM
SUBROUTINE GEOM
COMPLEX A,AA,ANH,CZERO,WASH,AIC
DIMENSION AIC(40,30),WASH(40)
COMMON/C1/A(80),AA(40,80),ANH(40,40),CZERO
COMMON/C2/HKFR(20),ZKER(20),FMACH(6),FREQ(10),NOM(5),IL(50),
1      HCOR(6),ZCOR(6),WXCMN(11),WBCN(11),WBIN(11),WT(90),
2      XE(3),YE(3),UX(10),UY(10),WXIMN(11),SIX(40,2),SCX(10,2),
3      ETA(11)
COMMON/C3/Y(11),XAIC(10,10,2),YAIC(10,2),B(40,40),R(40,40),
1      C(40,40),T(40,40),TM(40,40),TR(40,40),TI(40,40)
COMMON/C4/CLFN,NGSKRN,NPY,SOUND,NMACH,NFREQ,MAUG,NIONCX,RHO,
6      NMDFS,LCOLL,LPRWSH,IPRCO,IIY,IIX,NSURF,ISOLAT,FM,FC,
7      NCOLS,NOMIT,MACH,XCOLL,YCOLL,P1,U,DWCX,CXMN,IMOD,IRW,
8      EM,FK,BZ,NWIX,NCIX,CRON,NWCY,IFR,E1,F2,QWY QWXX,
9      SN,WRO,NIY,NHCX,NCCX,NWPX,NCPX,NXWING,NYWING,NXCS,NYCS
EQUIVALENCE (AA,AIC),(A,WASH)
C      WBO = WING ROOT SEMI-CHORD
C      S = SEMI-SPAN
C      WTEN = WING TIP CHORD - NORMALIZED ON WBO
C      WTLN = WING TIP L.E. - NORMALIZED
C      SN = SEMI-SPAN - NORMALIZED
C      CBO = CONTROL SEMI-CHORD
C      FW = 2*NWIX+1
C      FC = 2*NCIX+1
C      WBO = XE(3)/2.0
C      CLFN = XE(4)/WBO
C      S = YE(3)
C      WTEN = (XE(3)-XE(2))/WBO
C      WTLN = XE(2)/WBO
C      SN = S/WBO
C      CBO = (XF(5)-XF(4))/2.0
C      F1=FW
C      F2 = F1*PI/2.
C      J = NWIX
C      COMPUTE CHORDWISE INTEGRATION AND COLLOCATION STATIONS
C      FIRST ON THE WING SURFACE
DO 6 I=1,NWIX
F2 = F2 - 2.*PI
SIX(J,1) = SIN(F2/F1)
T1 = FLOAT(I)/FLOAT(NIONCX) + 0.99
SCX(T1,1) = -SIX(J,1)
5   J=J-1
F1=FC
F2 = F1*PI/2.
J = NCIX
C      THEN ON THE CONTROL SURFACE
DO 6 I=1,NCIX
F2 = F2 - 2.*PI
SIX(J,2) = SIN(F2/F1)
T1 = FLOAT(I)/FLOAT(NIONCX) + 0.99
SCX(T1,2) = -SIX(J,2)
6   J=J-1
F1 = 4*NIY
F2 = 0.0
C      COMPUTE SPANWISE INTEGRATION AND COLLOCATION STATIONS
DO 8 I=1,NIY
Y(I) = SIN(F2/F1)
F2 = F2 + PI
ETA(I) = SIN(F2/F1)
8   F2 = F2 + PI

```

```
C COMPUTE WING SEMI-CHORDS AND MID-CHORD LOCATIONS AT THE
C SPANWISE COLLOCATION AND INTEGRATION STATIONS
PIR = YF(2)/YF(3)
POR = 1.0-PIR
CBON = (XE(5)-XE(1))/(2.0*WBO)
CXMN = CBON * XF(4)/WBO
DO 16 I=1,NIY
IF(FTA(I).LE.PI8) GO TO 12
F1 = WTLEN*(FTA(I)-PI8)/POR
IF(Y(I).LE.PIH) GO TO 13
F2 = WTLEN*(Y(I)-PIH)/POR
GO TO 14
12 F1 = 0.0
13 F2 = 0.0
14 WRIN(I) = 0.5*(2.0-F1)
WXIMN(I) = WRIN(I) + F1
WBCN(I) = 0.5*(2.0-F2)
16 WXCMN(I) = WRCN(I) + F2
56 RETURN
END
```

**CTRAMP**

SUBROUTINE TRAMP(NIY,NWCX,NCCX,NXWING,NYWING,NXCS,NYCS,NIF,WBO,SN)

C \*\*\* TRANSFORMATION MATRIX PROGRAM

C \*\*\* TRANSFORMS AIC COLLOCATION STATIONS TO UNSTEADY AERO STATIONS

COMMON/C3/Y(1),XAIC(10,10,2),YAIC(10,2),B(4,40),R(10,40).

1 C(40,40),T(10,40),TM(40,40),TR(40,40),TI(40,40)

C \*\*\* ZERO (TM) MATRIX FOR CHORDWISE TRANSFORMATION

KROWS=NXWING+NYWING+NXCS+NYCS

KCOLS=KROWS

DO 100 I=1,KROWS

DO 100 J=1,KCOLS

100 TM(I,J)=0.0

C \*\*\* CHORDWISE TRANSFORMATION (WING)

IF (NXWING .EQ. 0) GO TO 1999

DO 1000 I=1,NYWING

CALL BMAT(NXWING,NRSB,NCSB)

CALL THAT(NXWING,1,MSIZE,1,1,WBO,SN)

DO 1001 MR=1,MSIZE

DO 1001 MC=1,NCSR

TR(MR,MC)=0.0

DO 1001 MRC=1,MSIZE

1001 TR(MR,MC)=TR(MR,MC)+T(MR,MRC)\*R(MRC,MC)

CALL CMAT(NWCX,NIY,NXWING,NYWING,NIF,1,1,NRSC,NCSC,WBO,SN)

DO 1002 MR=1,NRSC

DO 1002 MC=1,NCSR

T(MR,MC)=0.0

DO 1002 MRC=1,NCSC

1002 T(MR,MC)=T(MR,MC)+C(MR,MRC)\*TR(MRC,MC)

KROW=(I-1)\*NXWING

DO 1003 LR=1,NXWING

LROW=KROW+LR

KCOL=(I-1)\*NYWING

DO 1003 LC=1,NYWING

LCOL=KCOL+LC

1003 TM(LROW,LCOL)=T(LR,LC)

1004 CONTINUE

1999 CONTINUE

C \*\*\* CHORDWISE TRANSFORMATION (CONTROL SURFACE)

IF (NXCS .EQ. 0) GO TO 2999

DO 2000 I=1,NYCS

CALL BMAT(NXCS,NRSB,NCSB)

CALL THAT(NXCS,1,MSIZE,2,1,WBO,SN)

DO 2001 MR=1,MSIZE

DO 2001 MC=1,NCSR

TR(MR,MC)=0.0

DO 2001 MRC=1,MSIZE

2001 TR(MR,MC)=TR(MR,MC)+T(MR,MRC)\*R(MRC,MC)

CALL CMAT(NCCX,NIY,NXCS,NYCS,NIF,2,1,NRSC,NCSC,WBO,SN)

DO 2002 MR=1,NRSC

DO 2002 MC=1,NCSR

T(MR,MC)=0.0

DO 2002 MRC=1,NCSC

2002 T(MR,MC)=T(MR,MC)+C(MR,MRC)\*TR(MRC,MC)

KROW=NXWING+NYWING+(I-1)\*NXCS

DO 2003 LR=1,NXCS

LROW=KROW+LR

KCOL=NXWING+NYWING+(I-1)\*NXCS

DO 2003 LC=1,NYCS

LCOL=KCOL+LC

2003 TM(LROW,LCOL)=T(LR,LC)

2004 CONTINUE

```

2970 CONTINUE
C *** REARRANGE ROWS AND COLUMNS FOR SPANWISE TRANSFORMATION
CALL RMAT(NXWING,NYWING,NXCS,NYCS,MSIZE)
DO 2050 MR=1,MSIZE
DO 2050 MC=1,MSIZE
TR(MR,MC)=0.0
DO 2050 MRC=1,MSIZE
  TI(MR,MC)=TI(MR,MC)+R(MR,MRC)*TM(MRC,MC)
2050 TI(MR,MC)=TI(MR,MC)+R(MR,MRC)*TM(MRC,MC)
C *** ZERO (TM) MATRIX FOR SPANWISE TRANSFORMATION
KROWS=NYY*(NXCX+NCX)
KCOLS=NWING*NWING+NXCS*NYCS
DO 3001 I=1,KROWS
DO 3001 J=1,KCOLUMNS
  TM(I,J)=0.0
3001 TM(I,J)=0.0
C *** SPANWISE TRANSFORMATION (WING)
IF (NYWING.EQ.0) GO TO 3999
DO 3002 I=1,NWCX
CALL RMAT(NYWING,NRSB,NCSB)
CALL TMAT(NYWING,/,MSIZE,1,1,WRO,SN)
DO 3001 MR=1,MSIZE
DO 3001 MC=1,NCSB
TR(MR,MC)=0.0
DO 3001 MRC=1,MSIZE
3001 TR(MR,MC)=TR(MR,MC)+T(MR,MRC)*R(MRC,MC)
CALL SMAT(NYY,NYWING,1,NRSS,NCSS,WRO,SN)
DO 3002 MR=1,NRSS
DO 3002 MC=1,NCSS
T(MR,MC)=0.0
DO 3002 MRC=1,NCSS
3002 T(MR,MC)=T(MR,MC)+C(MR,MRC)*TR(MRC,MC)
KROW=(I-1)*NYY
DO 3003 LR=1,NYY
LROW=KROW+LR
NITR=NWING-I
DO 3003 J=1,NITR
IF (WRO*X(1,1,I,J).LT.-5*(XAIC(J,1,1)+XAIC(J+1,1,1)))GO TO 3050
3050 CONTINUE
KCOL=NYWING*(NXWING-1)
GO TO 3090
3050 KCOL=NYWING*(J-1)
3070 DO 3080 IC=1,NYWING
  LCOL=KCOL+IC
3080 TM(LROW,LCOL)=T(LR,IC)
3080 CONTINUE
3090 CONTINUE
C *** SPANWISE TRANSFORMATION (CONTROL SURFACE)
IF (NYCS.EQ.0) GO TO 4999
DO 4000 I=1,NCX
CALL RMAT(NYCS,NRSB,NCSB)
CALL TMAT(NYCS,/,MSIZE,2,1,WRO,SN)
DO 4001 MR=1,MSIZE
DO 4001 MC=1,NCSB
TR(MR,MC)=0.0
DO 4001 MRC=1,MSIZE
4001 TR(MR,MC)=TR(MR,MC)+T(MR,MRC)*R(MRC,MC)
CALL SMAT(NYY,NYCS,/,NRSS,NCSS,WRO,SN)
DO 4002 MR=1,NRSS
DO 4002 MC=1,NCSS
T(MR,MC)=0.0
DO 4002 MRC=1,NCSS
4002 T(MR,MC)=T(MR,MC)+C(MR,MRC)*TR(MRC,MC)

```

```

KROW=(J-1)*NIY+NWCX*NIY
DO 4080 LR=1,NIY
LROW=KROW+LR
NITR=NXCS-1
DO 4070 J=1,NITR
IF (WBO*XS(1,J,I,1) .LT. .5*(XAIC(J,1,2)+XAIC(J+1,1,2)))GO TO 4051
4070 CONTINUE
KCOL=NYWING*NWING+NYCS*(NXCS-1)
GO TO 4090
4050 KCOL=NYWING*NWING+NYCS*(J-1)
4090 DO 4080 LC=1,NYCS
LCOL=KCOL+LC
4080 TM(IROW,LCOL)=T(IR,LC)
4070 CONTINUE
4990 CONTINUE
C *** REARRANGE ROWS AND COLUMNS SO STATIONS ARE STACKED ROWWISE
CALL RMAT(NIY,NWCX,NIY,NCCX,NSIZE)
DO 5001 MR=1,NSIZE
DO 5001 MC=1,KCOLS
TR(MR,MC)=0.0
DO 5001 MRC=1,NSIZE
5001 TR(MR,MC)=TR(MR,MC)+R(MR,MRC)*TM(MRC,MC)
DO 5002 MR=1,KROWS
DO 5002 MC=1,KCOLS
TM(MR,MC)=0.0
DO 5002 MRC=1,KROWS
5002 TM(MR,MC)=TM(MR,MC)+TR(MR,MRC)*TI(MRC,MC)
DO 5050 I=1,KROWS
DO 5050 J=1,KCOLS
TR(I,J)=TM(I,J)
5050 TI(I,J)=TM(I,J)
RETURN
END

```

```

CTMAT THAT
  SUBROUTINE THAT(NPTS,ND,MSIZE,NS,IY,WBO,SN)
  COMMON/C3/Y(1),XAIC(10,10,2),YAIC(10,2),B(40,40),R(40,40),
  1           C(40,40),T(40,40),TM(40,40),TR(40,40),TI(40,40)
C *** GENERATES (T)**(-1) MATRIX
C *** NPTS = NUMBER OF AIC POINTS ALONG STRIP IN ND DIRECTION
C *** MSIZE = ORDER OF T MATRIX
C *** NS = SURFACE (1=WING AND 2=CONTROL SURFACE)
C *** ND = INTERPOLATION DIRECTION (1=CHORDWISE AND 2=SPANWISE)
  IF (NPTS .LT. 4) MSIZE=NPTS
  IF (NPTS .GT. 3) MSIZE=3*NPTS-4
  DO 1 J=1,MSIZE
  DO 1 K=1,MSIZE
  1 T(J,K)=0.0
  IF (NPTS .GT. 4) GO TO 5000
  GO TO (2000,2100,3000,4000), NPTS
C *** NPTS=2 (TWO POINTS ALONG STRIP)
  2000 T(1,1)=1.0
  T(2,1)=1.0
  IF (ND .EQ. 1) T(1,2)=XAIC(1,IY,NS)
  IF (ND .EQ. 1) T(2,2)=XAIC(2,IY,NS)
  IF (ND .EQ. 2) T(1,2)=YAIC(1,NS)
  IF (ND .EQ. 2) T(2,2)=YAIC(2,NS)
  GO TO 6000
C *** NPTS=3 (THREE POINTS ALONG STRIP)
  3000 T(1,1)=1.0
  T(2,1)=1.0
  T(3,1)=1.0
  IF (ND .EQ. 2) GO TO 3010
C *** NPTS=3 CHORDWISE DIRECTION
  T(1,2)=XAIC(1,IY,NS)
  T(1,3)=T(1,2)**2
  T(2,2)=XAIC(2,IY,NS)
  T(2,3)=T(2,2)**2
  T(3,2)=XAIC(3,IY,NS)
  T(3,3)=T(3,2)**2
  GO TO 6000
C *** NPTS=3 SPANWISE DIRECTION
  3010 T(1,2)=YAIC(1,NS)
  T(1,3)=T(1,2)**2
  T(2,2)=YAIC(2,NS)
  T(2,3)=T(2,2)**2
  T(3,2)=YAIC(3,NS)
  T(3,3)=T(3,2)**2
  GO TO 6000
C *** NPTS=4 (FOUR POINTS ALONG STRIP)
  4000 T(1,1)=1.0
  T(2,1)=1.0
  T(3,1)=1.0
  T(4,2)=1.0
  T(5,4)=1.0
  T(6,4)=1.0
  T(3,4)=-1.0
  T(4,5)=-1.0
  IF (ND .EQ. 2) GO TO 4010
C *** NPTS=4 CHORDWISE DIRECTION
  T(1,2)=XAIC(1,IY,NS)
  T(1,3)=T(1,2)**2
  T(2,2)=XAIC(2,IY,NS)
  T(2,3)=T(2,2)**2
  T(3,2)=0.5*(XAIC(1,IY,NS)+XAIC(3,IY,NS))

```

```

T(3,3)=T(3,2)*e2
T(3,5)=-T(3,2)
T(3,6)=-T(3,3)
T(4,3)=2.0*T(3,2)
T(4,6)=-T(4,3)
T(5,5)=XAIC(3,1Y,NS)
T(5,6)=T(5,5)**2
T(6,5)=XAIC(4,1Y,NS)
T(6,6)=T(6,5)**2
GO TO 6000
C *** NPTS=4 SPANWISE DIRECTION
4010 T(1,2)=YAIC(1,NS)
T(1,3)=T(1,2)**2
T(2,2)=YAIC(1,NS)
T(2,3)=T(2,2)**2
T(3,2)=0.5*(YAIC(2,NS)+YAIC(3,NS))
T(3,3)=T(3,2)**2
T(3,5)=-T(3,2)
T(3,6)=-T(3,3)
T(4,3)=2.0*T(3,2)
T(4,6)=-T(4,3)
T(5,5)=YAIC(3,NS)
T(5,6)=T(5,5)**2
T(6,5)=YAIC(4,NS)
T(6,6)=T(6,5)**2
GO TO 6000
C *** NPTS .GT. 4
5000 IF (ND .EQ. 2) GO TO 5500
C *** NPTS .GT. 4 (CHORDWISE DIRECTION)
T(1,1)=1.0
T(1,2)=XAIC(1,1Y,NS)
T(1,3)=T(1,2)**2
T(2,1)=1.0
T(2,2)=XAIC(2,1Y,NS)
T(2,3)=T(2,2)**2
T(MSIZE,MSIZE-2)=1.0
T(MSIZE,MSIZE-1)=XAIC(NPTS,1Y,NS)
T(MSIZE,MSIZE)=T(MSIZE,MSIZE-1)**2
T(MSIZE-1,MSIZE-2)=1.0
T(MSIZE-1,MSIZE-1)=XAIC(NPTS-1,1Y,NS)
T(MSIZE-1,MSIZE)=T(MSIZE-1,MSIZE-1)**2
NT=NPTS-4
DO 5010 NR=1,NT
NR=NR+1
NC=1*NR+1
NP=NR+2
T(NR,NC)=1.0
T(NR,NC+1)=XAIC(NP,1Y,NS)
5010 T(NR,NC+2)=T(NR,NC+1)**2
NT=NPTS-3
DO 5020 NR=1,NT
NR=NR+1
NC=1*NR+1
T(NR,NC)=1.0
T(NR+1,NC+1)=1.0
T(NR,NC+3)=-1.0
T(NR+1,NC+4)=-1.0
T(NR,NC+1)=0.5*(XAIC(N+1,1Y,NS)+XAIC(N+2,1Y,NS))
T(NR,NC+2)=T(NR,NC+1)**2
T(NR,NC+4)=-T(NR,NC+1)
T(NR,NC+5)=-T(NR,NC+2)

```

```

      T(NR+1,NC+2)=/.0*T(NR,NC+1)
5410  T(NR+1,NC+5)=-T(NR+1,NC+2)
      GO TO 6000
C *** NPTS .GT. 4 (SPANWISE DIRECTION)
5500  T(1,1)=1.0
      T(1,2)=YAIC(1,NS)
      T(1,3)=T(1,2)**2
      T(2,1)=1.0
      T(2,2)=YAIC(2,NS)
      T(2,3)=T(2,2)**2
      T(MSIZE,MSIZE-2)=1.0
      T(MSIZE,MSIZE-1)=YAIC(NPTS,NS)
      T(MSIZE,MSIZE)=T(MSIZE,MSIZE-1)**2
      T(MSIZE-1,MSIZE-2)=1.0
      T(MSIZE-1,MSIZE-1)=YAIC(NPTS-1,NS)
      T(MSIZE-1,MSIZE)=T(MSIZE-1,MSIZE-1)**2
      NT=NPTS-4
      DO 510 N=1,NT
      NR=/* N
      NC=/* N+1
      NP=N+2
      T(NR,NC)=1.0
      T(NR,NC+1)=YAIC(NP,NS)
5510  T(NR,NC+2)=T(NR,NC+1)**2
      NT=NPTS-3
      DO 520 N=1,NT
      NR=/* N
      NC=/* N+2
      T(NR,NC)=1.0
      T(NR+1,NC+1)=/.0
      T(NR,NC+3)=-1.0
      T(NR+1,NC+4)=-1.0
      T(NR,NC+1)=/.0*(YAIC(N+1,NS)+YAIC(N+2,NS))
      T(NR,NC+2)=T(NR,NC+1)**2
      T(NR,NC+4)=-T(NR,NC+1)
      T(NR,NC+5)=-T(NR,NC+2)
      T(NR+1,NC+2)=/.0*T(NR,NC+1)
5520  T(NR+1,NC+5)=-T(NR+1,NC+2)
C *** INVERT T MATRIX
6000  CONTINUE
      CALL MINV (MSIZE,T,C)
      RETURN
      END

```

```

CCMAT 1 MAT
SUBROUTINE CCHAT(NPTS,NIY,NAICPX,NAICPY,NIF,NS,IY,NRS NCS,WRO,SN)
C *** FOR CHORDWISE TRANSFORMATIONS
C *** NPTS = NUMBER OF CHORDWISE UNSTEADY AERO COLLOCATION STATIONS
C *** NIY = NUMBER OF SPANWISE UNSTEADY AERO COLLOCATION STATIONS
C *** NAICPX = NUMBER OF CHORDWISE AIC COLLOCATION STATIONS
C *** NAICPY = NUMBER OF SPANWISE AIC COLLOCATION STATIONS
C *** IY = SPAN NUMBER OF AIC STRIP BEING TRANSFORMED
C *** NIF = CODE FOR DIFFERENTIATION (1=NO DERIVATIVE AND 2=D1 )/DX )
C *** MATRIX SIZE IS (NRS,NCS)
COMMON/C3/Y(1),XAIC(10,10,2),YAIC(10,2),R(40,40),R(10,40),
      1 C(10,40),T(40,40),TM(40,40),TR(40,40),T1(40,40)
      1 IF (NAICPX .GT. 3) GO TO 3
      1 NRS=NAICPX
      1 NCS=NAICPX
      1 DO 1 I=1,NRS
      1 DO 1 J=1,NCS
      1 C(I,J)=0.0
      1 GO TO 100
      1 NRS=NAICPX
      1 NCS=3*(NAICPX-2)
      1 DO 4 I=1,NRS
      1 DO 4 J=1,NCS
      4 C(I,J)=0.0
100 1 IF (NCS .GT. 6) GO TO 500
      1 IF (NCS .EQ. 0) GO TO 400
      1 GO TO (200,200,300),NCS
C *** TWO POINTS
200 200 DO 11 I=1,NAICPX
      200 C(1,1)=1.0
      200 C(1,2)=XINT(IY,1,NIY,NS,WRO,SN)
      200 IF (NIF .EQ. 1) C(1,1)=0.0
      200 IF (NIF .EQ. 2) C(1,2)=1.0
210 210 CONTINUE
      210 RETURN
C *** THREE POINTS
300 300 DO 19 I=1,NAICPX
      300 C(1,1)=1.0
      300 IF (NIF .EQ. 2) C(1,1)=0.0
      300 C(1,2)=XINT(IY,1,NIY,NS,WRO,SN)
      300 IF (NIF .EQ. 1) C(1,2)=1.0
      300 C(1,3)=C(1,2)*2
      300 IF (NIF .EQ. 1) C(1,3)=2.0*XINT(IY,1,NIY,NS,WRO,SN)
310 310 CONTINUE
      310 RETURN
C *** FOUR POINTS
400 400 DO 18 I=1,NAICPX
      400 NX=NPTS-1
      400 DO 16 J=1,NX
      400   16 (0.5*(XAIC(J,IY,NS)+XAIC(J+1,IY,NS)).G1.XINT(IY,1 NIY,NS,WRO,SN
      16) GO TO 400/
406 406 CONTINUE
      406 NX=NPTS
      406 GO TO 408
407 407 NX=J
408 408 KC=1
      408 IF (NX .GT. 2) KC=4
      408 C(I,KC)=1.0
      408 C(I,KC+1)=XINT(IY,1,NIY,NS,WRO,SN)
      408 C(I,KC+2)=C(I,KC+1)*2
      408 IF (NIF .EQ. 1) C(I,KC)=0.720

```

```

      IF (NIF .EQ. .) C(I,KC+1)=1.0
      IF (NIF .EQ. .) C(I,KC+2)=2.0*XINT(IY,I,NIY,NS,WBO,SN)
410 CONTINUE
      RETURN
C *** .GT. FOUR POINTS
500 DO 510 I=1,NAICPX
      NX=NPTS-1
      DO 506 J=1,NX
      IF (0.5*(XAIC(J,IY,NS)+XAIC(J+1,IY,NS)).GT.XINT(IY,I,NIY,NS,WBO,SN)
      ) GO TO 507
506 CONTINUE
      NX=NPTS
      GO TO 508
507 NX=J
508 IF (NX .LT. 3) GO TO 550
      IF (NX .GT. NAICPX-2) GO TO 580
      KC=(NX-2)*3+1
      C(I,KC)=1.0
      C(I,KC+1)=XINT(IY,I,NIY,NS,WBO,SN)
      C(I,KC+2)=C(I,KC+1)**2
      IF (NIF .EQ. .) C(I,KC+1)=1.0
      IF (NIF .EQ. .) C(I,KC)=0.0
      IF (NIF .EQ. .) C(I,KC+2)=2.0*XINT(IY,I,NIY,NS,WBO,SN)
      GO TO 510
510 C(I,1)=1.0
      C(I,2)=XINT(IY,I,NIY,NS,WBO,SN)
      C(I,3)=C(I,2)**2
      IF (NIF .EQ. .) C(I,1)=0.0
      IF (NIF .EQ. .) C(I,2)=1.0
      IF (NIF .EQ. .) C(I,3)=2.0*XINT(IY,I,NIY,NS,WBO,SN)
      GO TO 510
550 C(I,NCS-2)=1.0
      C(I,NCS-1)=XINT(IY,I,NIY,NS,WBO,SN)
      C(I,NCS)=C(I,NCS-1)**2
      IF (NIF .EQ. .) C(I,NCS-2)=0.0
      IF (NIF .EQ. .) C(I,NCS-1)=1.0
      IF (NIF .EQ. .) C(I,NCS)=2.0*XINT(IY,I,NIY,NS,WBO,SN)
550 CONTINUE
      RETURN
END

```

```

FORMAT SMAT
      SUBROUTINE SMAT(NIY,NAICPY,NS,NRS,NCS,WRO,SN)
C *** SPANWISE TRANSFORMATION
C *** NIY = NUMBER OF SPANWISE UNSTEADY AERO COLLOCATION STATIONS
C *** NAICPY = NUMBER OF SPANWISE AIR COLLOCATION STATIONS
C *** NS = SURFACE (1=WING AND 2=CONTROL SURFACE)
C *** MATRIX SIZE IS NRS BY NCS
      COMMON/C3/Y(1),XAIC(10,1),YAIC(10,2),B(40,40),R(10,1),
     1 C(10,40),T(40,40),TM(40,40),TR(40,40),TI(40,40)
      IF (NAICPY .GT. 3) GO TO 8
      NRS=NIY
      NCS=NAICPY
      DO 4 I=1,NRS
      DO 6 J=1,NCS
      C(I,J)=0.0
      GO TO 10
  4   NRS=NIY
      NCS=NAICPY-1
      DO 5 I=1,NRS
      DO 6 J=1,NCS
      C(I,J)=0.0
  5   IF (NCS .GT. 1) GO TO 500
      IF (NCS .EQ. 1) GO TO 400
      GO TO (200,210,220),NCS
C *** TWO POINTS
  200 DO 260 I=1,NIY
      C(I,1)=1.0
      C(I,2)=WRO*SN*Y(I)
  260 CONTINUE
      RETURN
C *** THREE POINTS
  300 DO 360 I=1,NIY
      C(I,1)=1.0
      C(I,2)=WRO*SN*Y(I)
      C(I,3)=C(I,1)**2
  360 CONTINUE
      RETURN
C *** FOUR POINTS
  400 DO 490 I=1,NIY
      IC=1
      IF (WRO*SN*Y(I) .LT. 0.5*(YAIC(2,NS)+YAIC(3,NS))) 1C=2
      C(I,1C)=1.0
      C(I,1C+1)=WRO*SN*Y(I)
      C(I,1C+2)=C(I,1C+1)**2
  490 CONTINUE
      RETURN
C *** .GT. FOUR POINTS
  500 DO 521 I=1,NIY
      NI=NAICPY-2
      DO 520 J=1,NI
      IF (0.5*(YAIC(I,NS)+YAIC(J+1,NS)) .GT. WRO*SN*Y(I)) GO TO 523
  520 CONTINUE
      IC=3*NAICPY-3
      GO TO 524
  523 IC=(J-2)*3+4
      IF (J .LT. 3) IC=3
  524 C(I,1C)=1.0
      C(I,1C+1)=WRO*SN*Y(I)
      C(I,1C+2)=C(I,1C+1)**2
  526 CONTINUE
      RETURN
      END

```

```

FORMAT      RMAT
SUBROUTINE RMAT (NXWING,NYWING,NXCS,NYCS,MSIZE)
C *** REARRANGES AIC STATIONS INTO PROPER SEQUENCE FOR SPANWISE
C *** INTERPOLATION
C *** MATRIX SIZE IS MSIZE=NXWING*NYWING+NXCS*NYCS (SQUARE)
COMMON/C3/Y(1,1),XAIC(10,10,2),YAIC(10,2),B(40,40),R(10,10),
1          C(40,40),T(40,40),TM(40,40),TR(40,40),TI(40,40)
C7ERO=0.0
MSIZE=NXWING*NYWING+NXCS*NYCS
DO 100 J=1,MSIZE
DO 100 J=1,MSIZE
100 R(I,J)=C7ERO
IF (NXWING .EQ. 0) GO TO 250
K=1
KK=
II=NYWING*NXWING
DO 110 I=1,II
R(I,K)=1.0
K=K+NXWING
IF (K .GT. II) KK=KK+1
IF (K .GT. II) K=KK
250 CONTINUE
250 CONTINUE
IF (NXCS .EQ. 0) GO TO 350
II=NXCS*NYCS
K=NYWING*NYWING+1
KK=NXWING*NYWING+1
DO 120 I=1,II
TK=I+NXWING*NYWING
R(TK,K)=1.0
K=K+NXCS
IF (K .GT. MSIZE) KK=KK+1
IF (K .GT. MSIZE) K=KK
350 CONTINUE
350 CONTINUE
RETURN
END

```

```

FORMAT BMAT
SUBROUTINE BMAT(NPTS, IRS, ICS)
COMMON/C3/Y(1), XATC(10,10,2), YATC(10,2), BR40,40), R(10,40),
      C(10,40), T(10,40), TM(40,40), TR(10,40), TI(40,40)
C *** R = B(IRs,ICS) MATRIX
C *** NPTS = NUMBER OF ATC STATION ALONG STRIP (EITHER CHORDWISE OR
C *** SPANWISE)
  ICS=NPTS
  IF (NPTS .GT. 1) GO TO 200
  IRS=NPTS
  DO 10 J=1,IRS
  DO 10 I=1,ICS
  B(I,J)=0.0
  IF (I .EQ. J) B(I,J)=1.0
  10 CONTINUE
  RETURN
200 IRS=6+(NPTS-1)*5
  DO 30 I=1,IRS
  DO 30 J=1,ICS
  30 B(I,J)=0.0
  B(1,1)=1.0
  B(2,2)=1.0
  B(IRs,ICS)=1
  B(IRs-1,ICS-1)=1.0
  IF (NPTS .EQ. 1) GO TO 400
  K=NPTS-4
  DO 40 I=1,K
  NR=2+I*1
  NC=1+1
  40 B(NR,NC)=1.0
  410 RETURN
  END

```

```

CMINV   MINV
SUBROUTINE MINV (NM,A,U)
DIMENSION A(40,40),U(40,40)
DO 1001 I=1,NM
DO 1001 J=1,NM
U(I,J)=0.0
IF (I.EQ.J) U(I,J)=1.0
1001 CONTINUE
EPS=0.00000001
DO 1015 I=1,NM
K=1
IF (I-NM) 9021,9017,9021
9021 IF (A(I,I)-EPS) 9005,9006,9007
9005 IF (-A(I,I)-EPS) 9006,9006,9007
9006 K=K+1
DO 1023 J=1,NM
U(I,J)=U(I,J)+U(K,J)
9023 A(I,J)=A(I,J)+A(K,J)
GO TO 9021
9017 DIV=A(I,I)
DO 1019 J=1,NM
U(I,J)=U(I,J)/DIV
9019 A(I,J)=A(I,J)/DIV
DO 1015 MM=i,NM
DELT=A(MM,I)
IF (ABS(DELT)-EPS) 9015,9015,9016
9016 IF (MM-I) 9014,9015,9010
9014 DO 1011 J=1,NM
U(MM,J)=U(MM,J)-U(I,J)*DELT
9011 A(MM,J)=A(MM,J)-A(I,J)*DELT
9015 CONTINUE
DO 1033 I=1,NM
DO 1033 J=1,NM
9033 A(I,J)=U(I,J)
RETURN
END

```

PART IV - SECTION B5.0

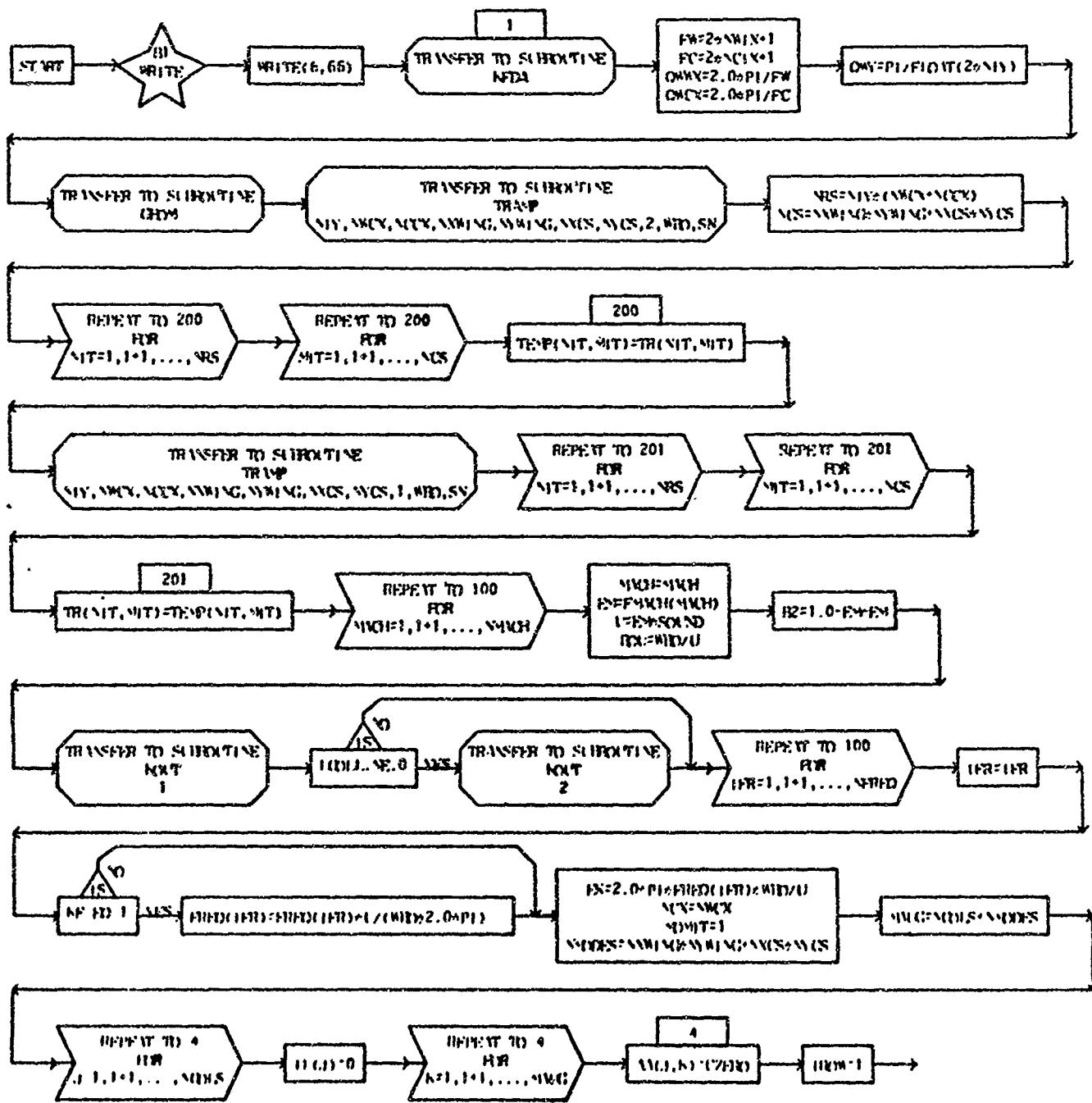
FLOW CHARTS FOR SUBSONIC  
AIC COMPUTER PROGRAM

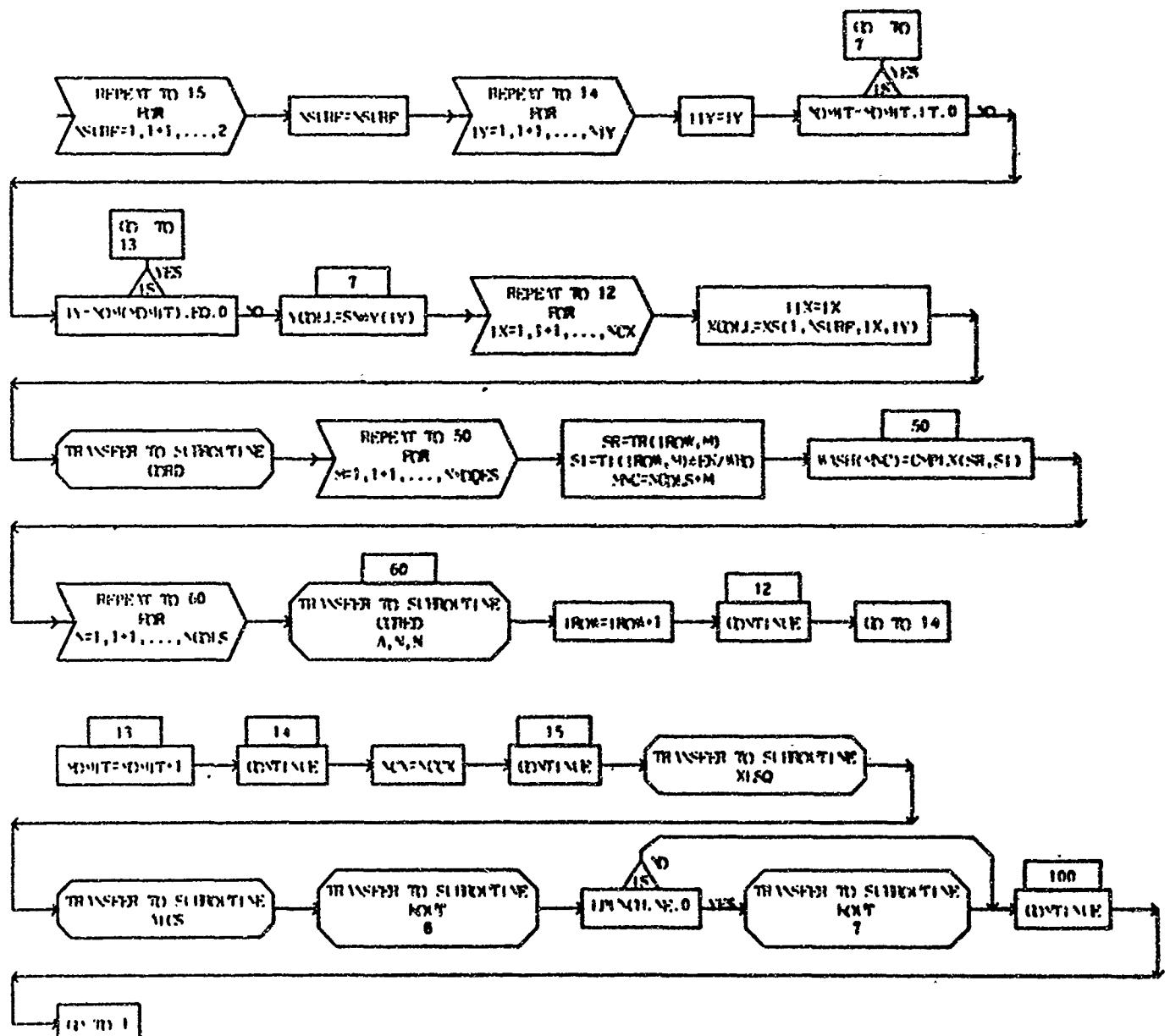
## DIMENSIONED VARIABLES

NAME	STORMS	SYMOL.	STORMS	SYMOL.	STORMS	SYMOL.	STORMS	SYMOL.	STORMS
TEMP	40,40	MC	40,40	WASH	40	F4	40,40		

COMPLEX A, 14, 194, C7R0, 924H, AIC

૨૫૨ - ૧





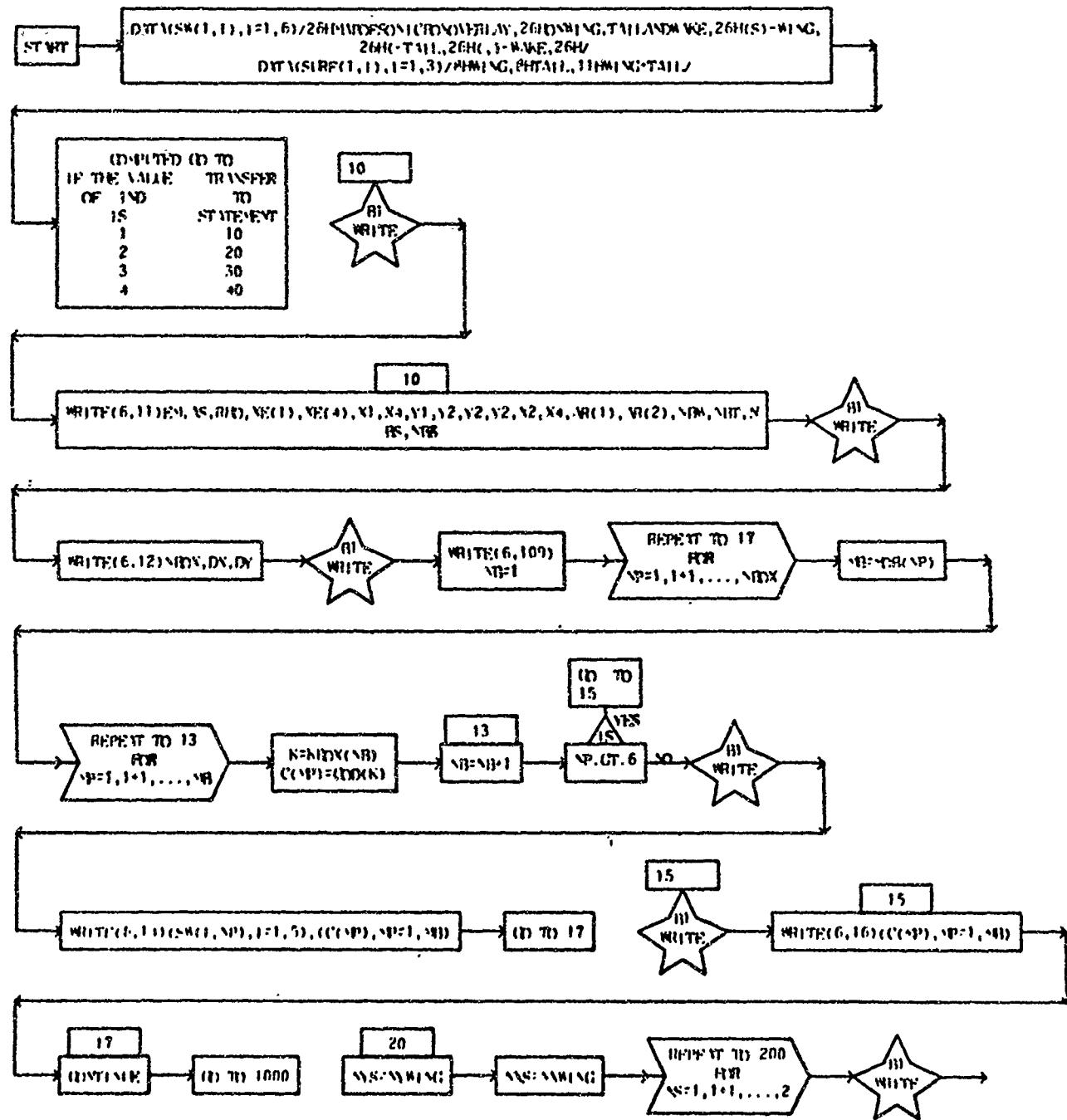
PORT      RXT

DIMENSIONED VARIABLES

SYMBOL	STORIES								
W	5.6	SURF	2.3	END	7	C	50		

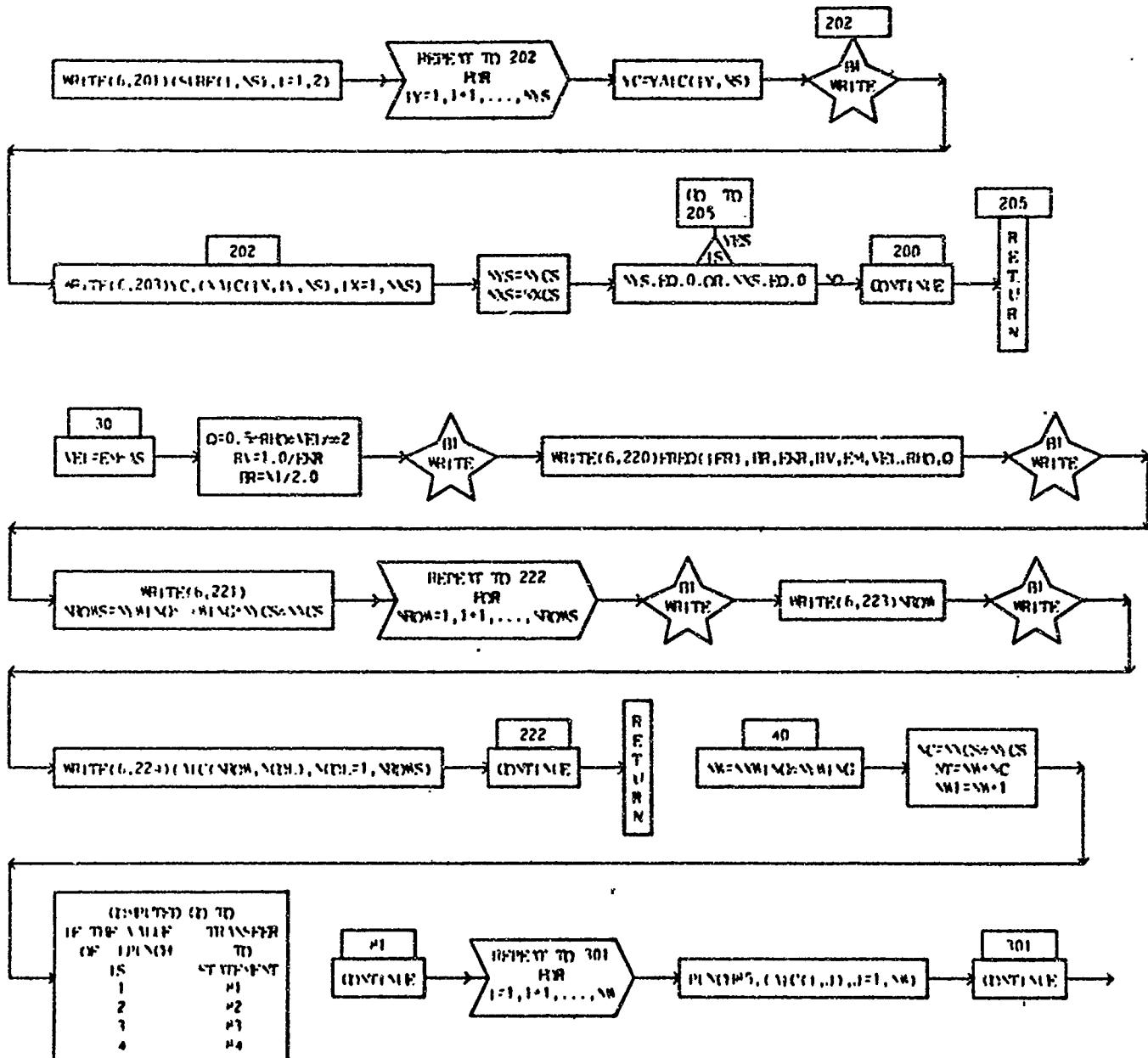
## SUBROUTINE ROUT (END)

PAGE 1

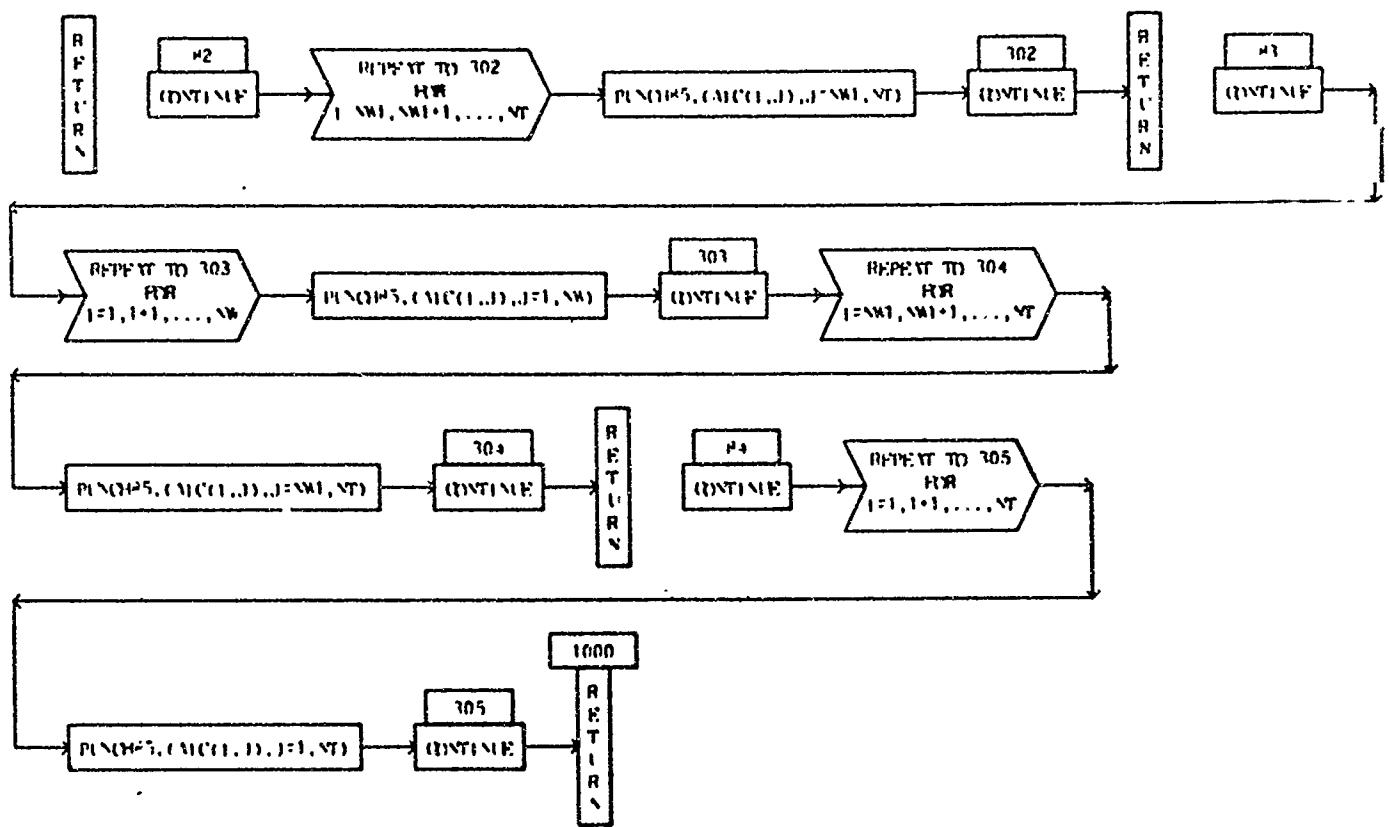


## SUBROUTINE POINT (IND)

PAGE 2

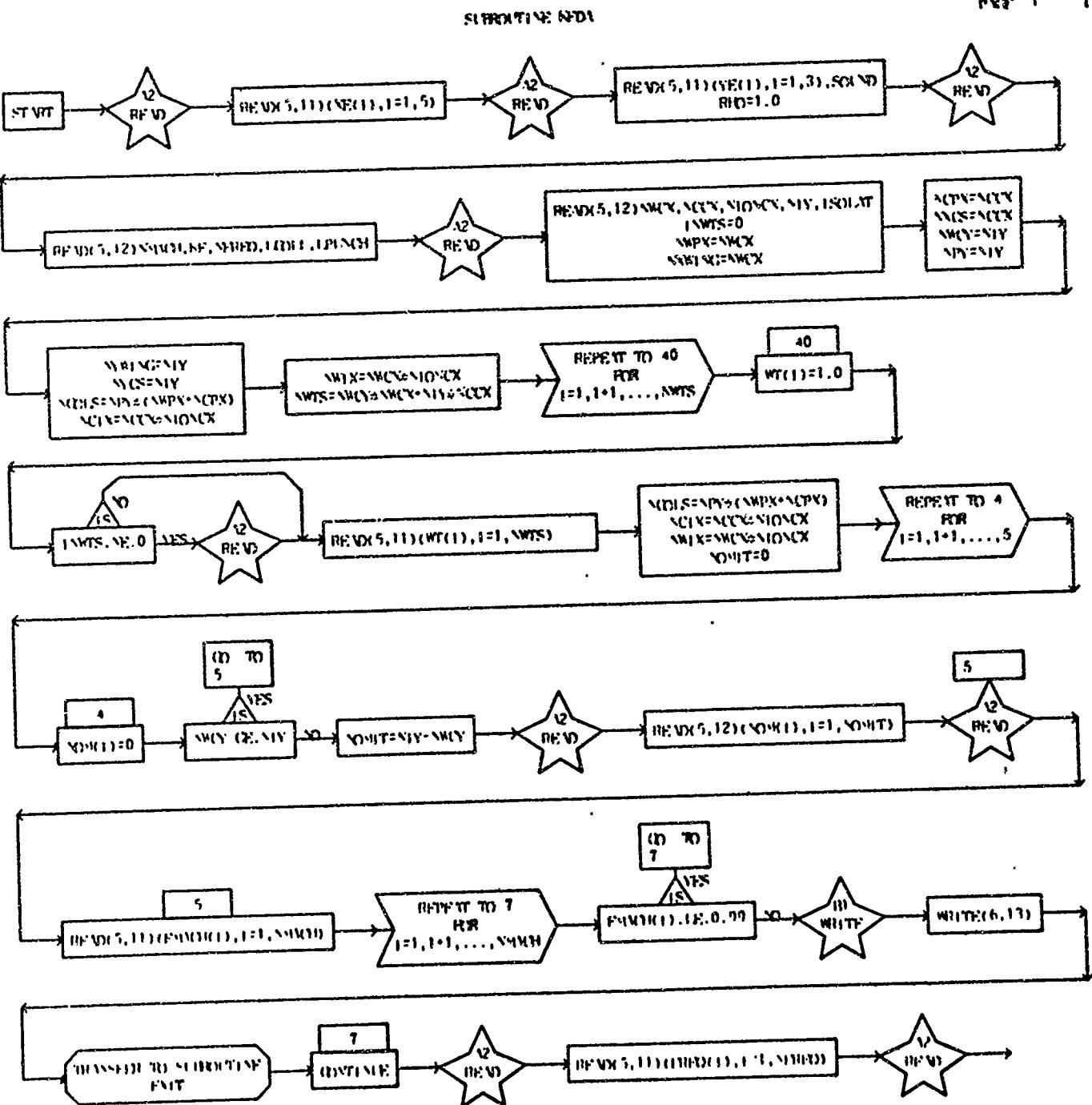


## SUBROUTINE RDT (IND)



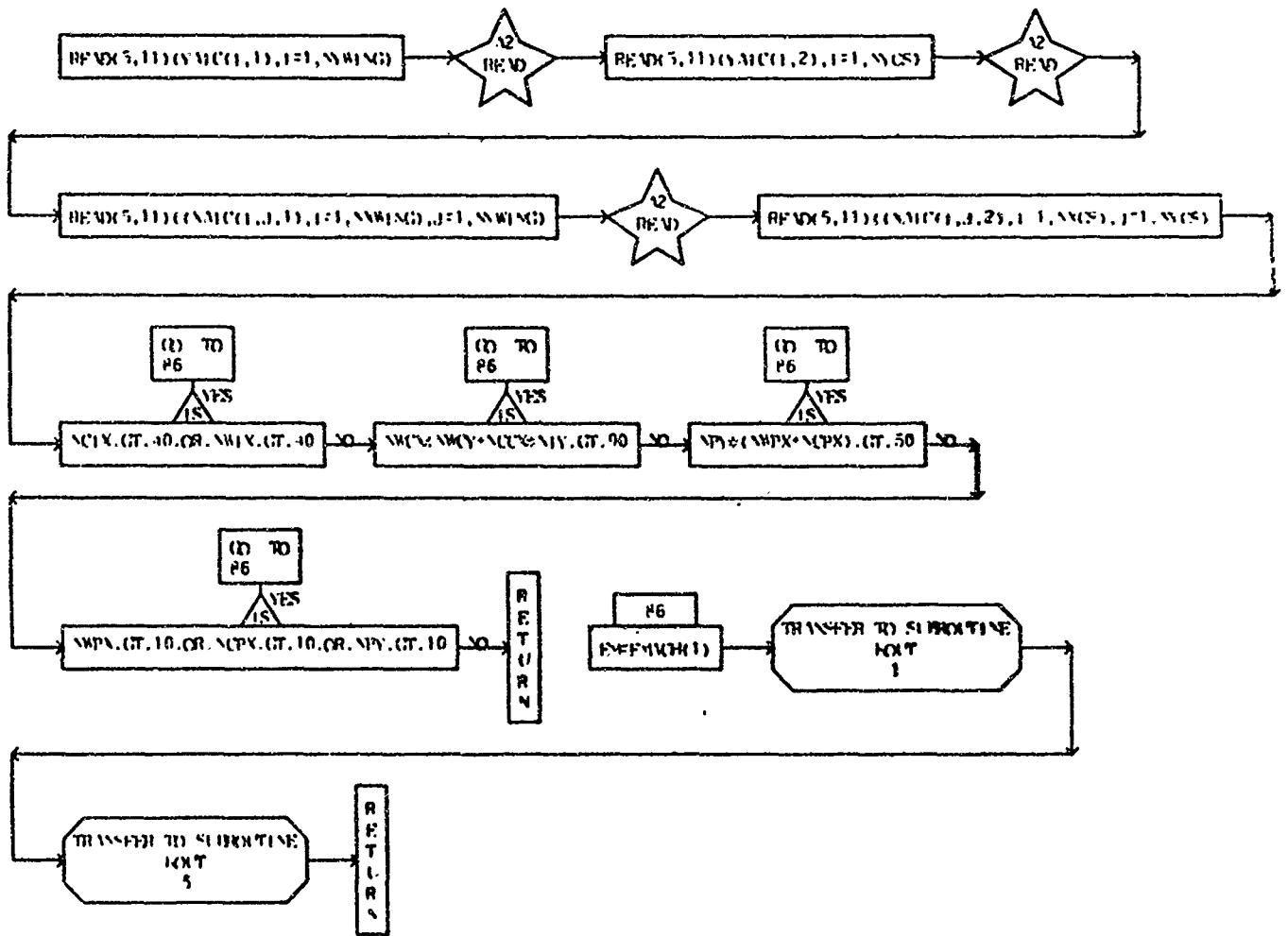
NTD1 NTD2

DIMENSIONED VARIABLES									
SYMBOL	STORAGE	SIMBL.	STORAGE	SIMBL.	STORAGE	SIMBL.	STORAGE	SIMBL.	STORAGE
MC	40,00		40						



## SUBROUTINE READ

PAGE 2



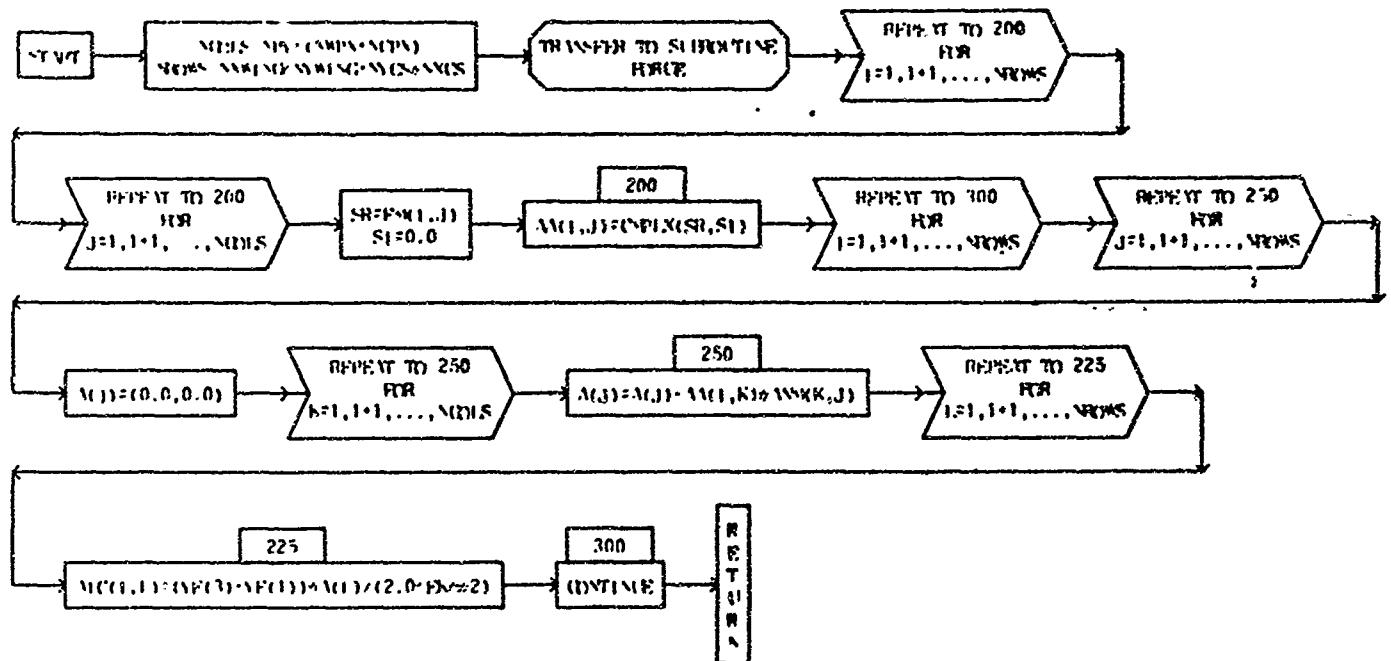
1165

DIMENSIONED VARIABLES

SYM#	STRTPTS								
10	10,20	100	20	100	10,10				

## STRUCTURE ALGS

FIG. 1



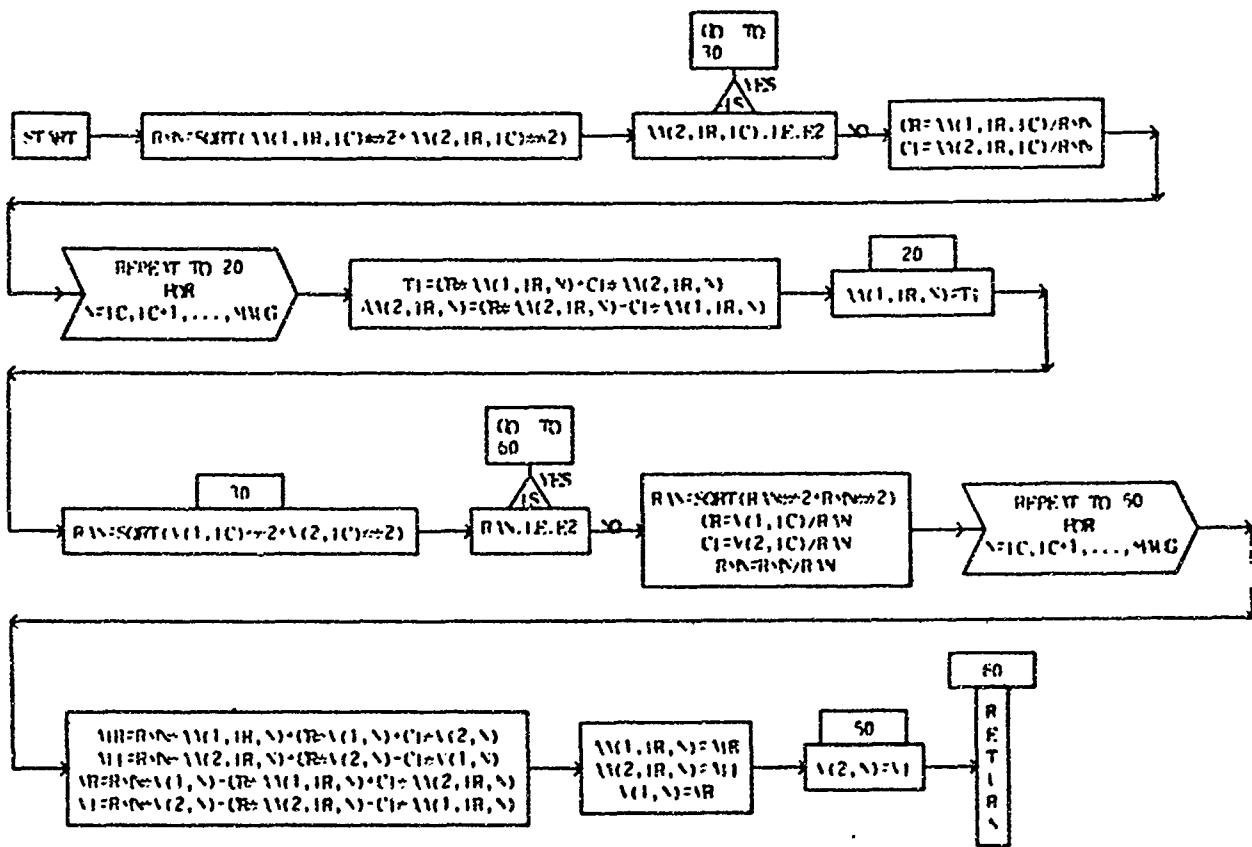
(178D) (189D)

DIMENSIONED VARIABLES

NAME	STORAGE	SYMPL.	STORAGE	SYMPL.	STORAGE	SYMPL.	STORAGE	SYMPL.	STORAGE
W10	10,00	W141	40	V	2,1				

SUBROUTINE (RFTDXV, IR, IC)

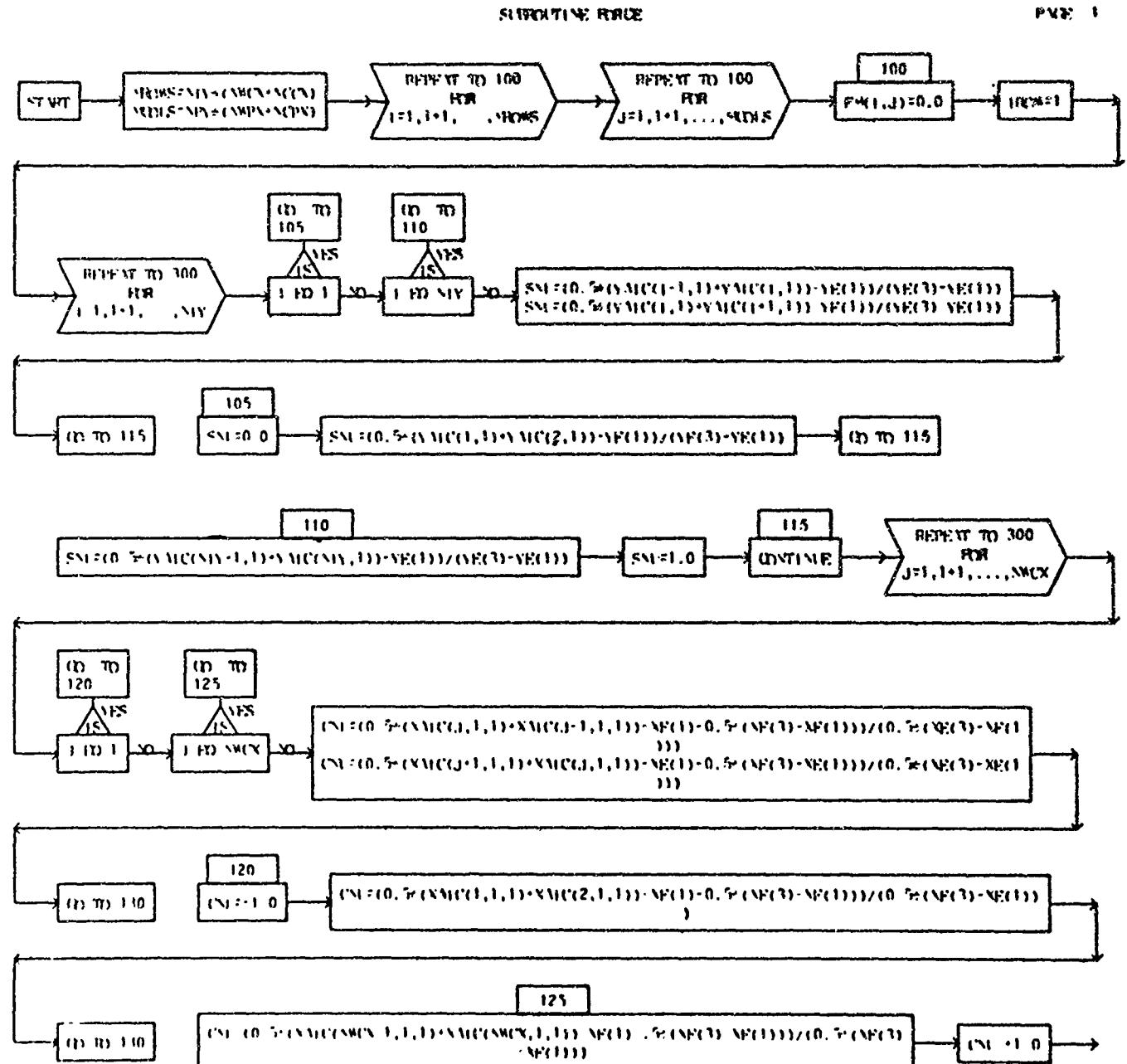
PAGE 1



HOLY

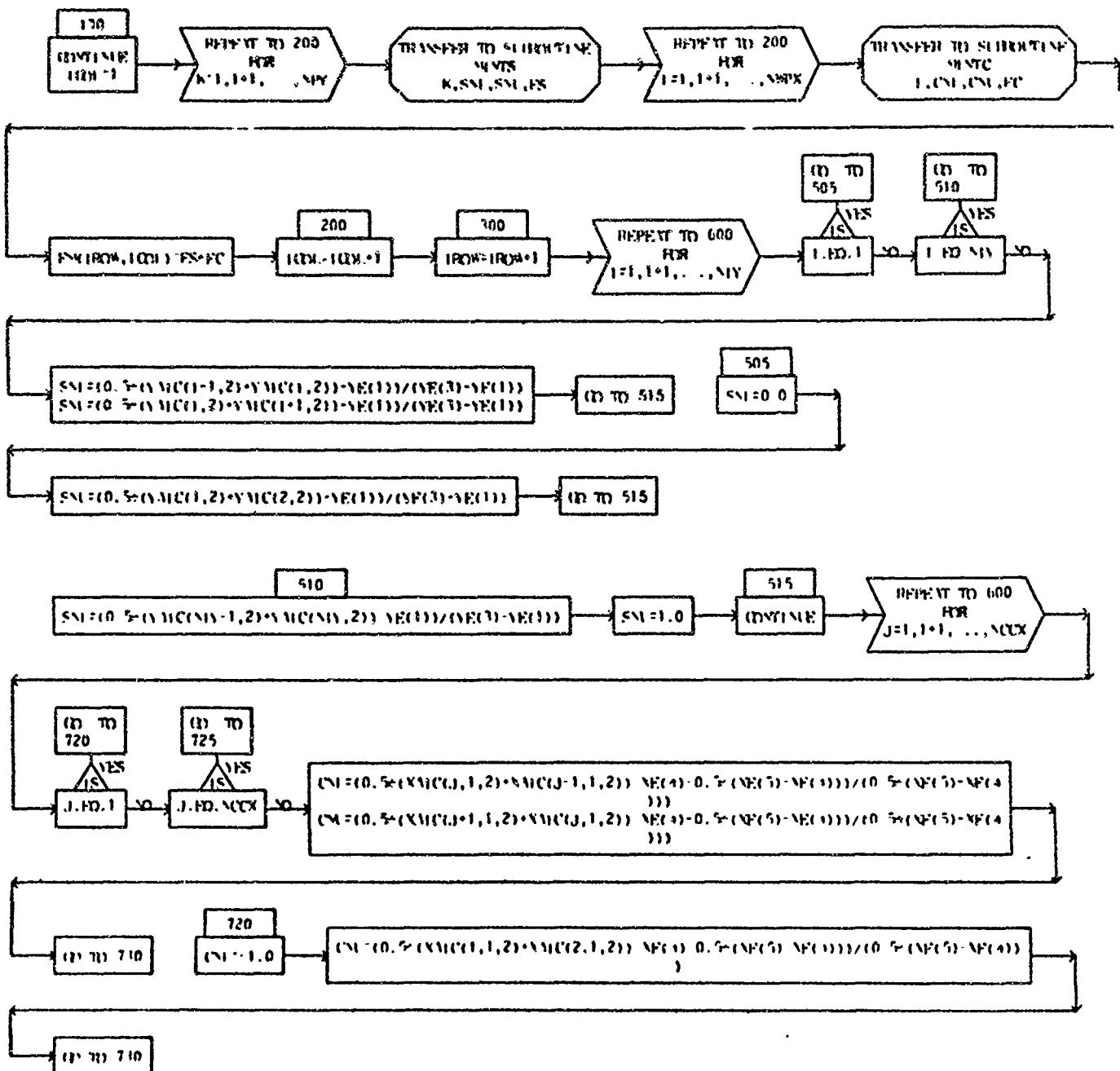
DIMENSIONED VARIABLES

SYM1	SYMBOLS	SYM2	SYMBOLS	SYM3	SYMBOLS	SYM4	SYMBOLS	SYM5	SYMBOLS
PS	10,10								



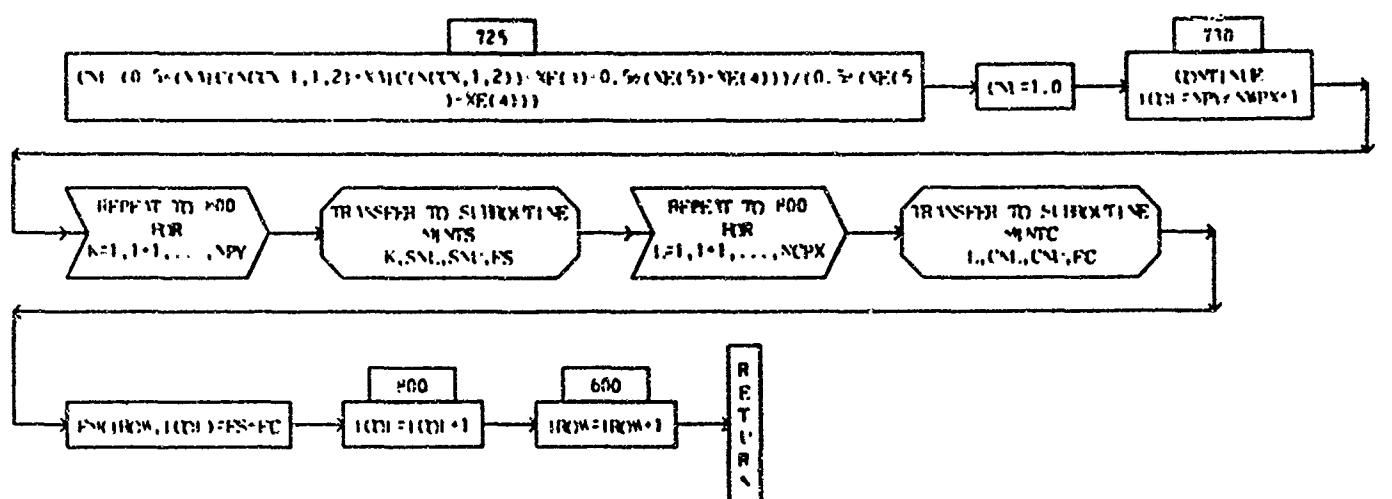
## SUBROUTINE R111

PAGE 2



## SUBROUTINE R30Z

PAGE 7



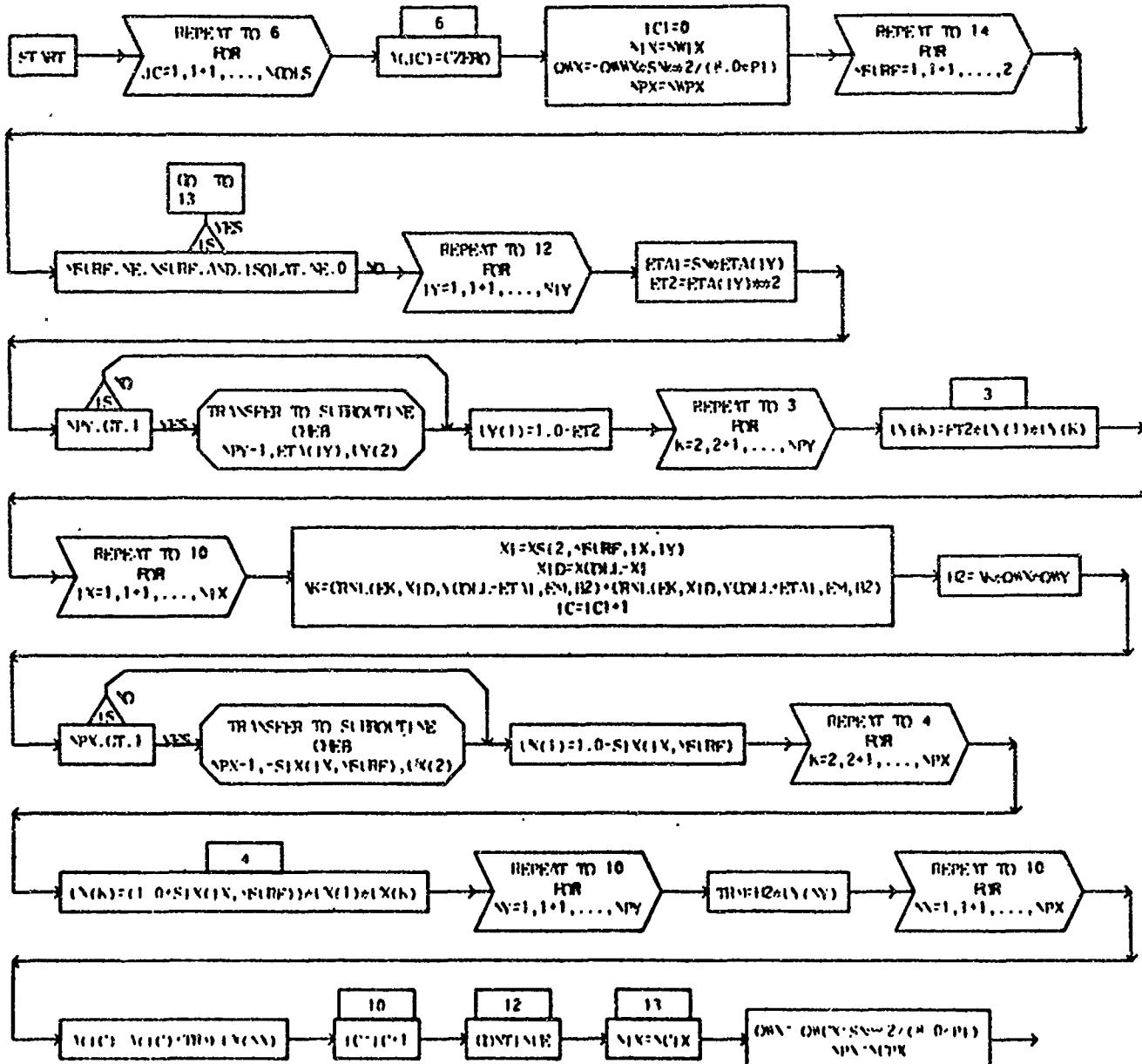
QRTZ QRTZ

DIMENSIONED VARIABLES

SYMBOL	STRAWS								
MC	40,40	MH	40						

## SUBROUTINE GRID

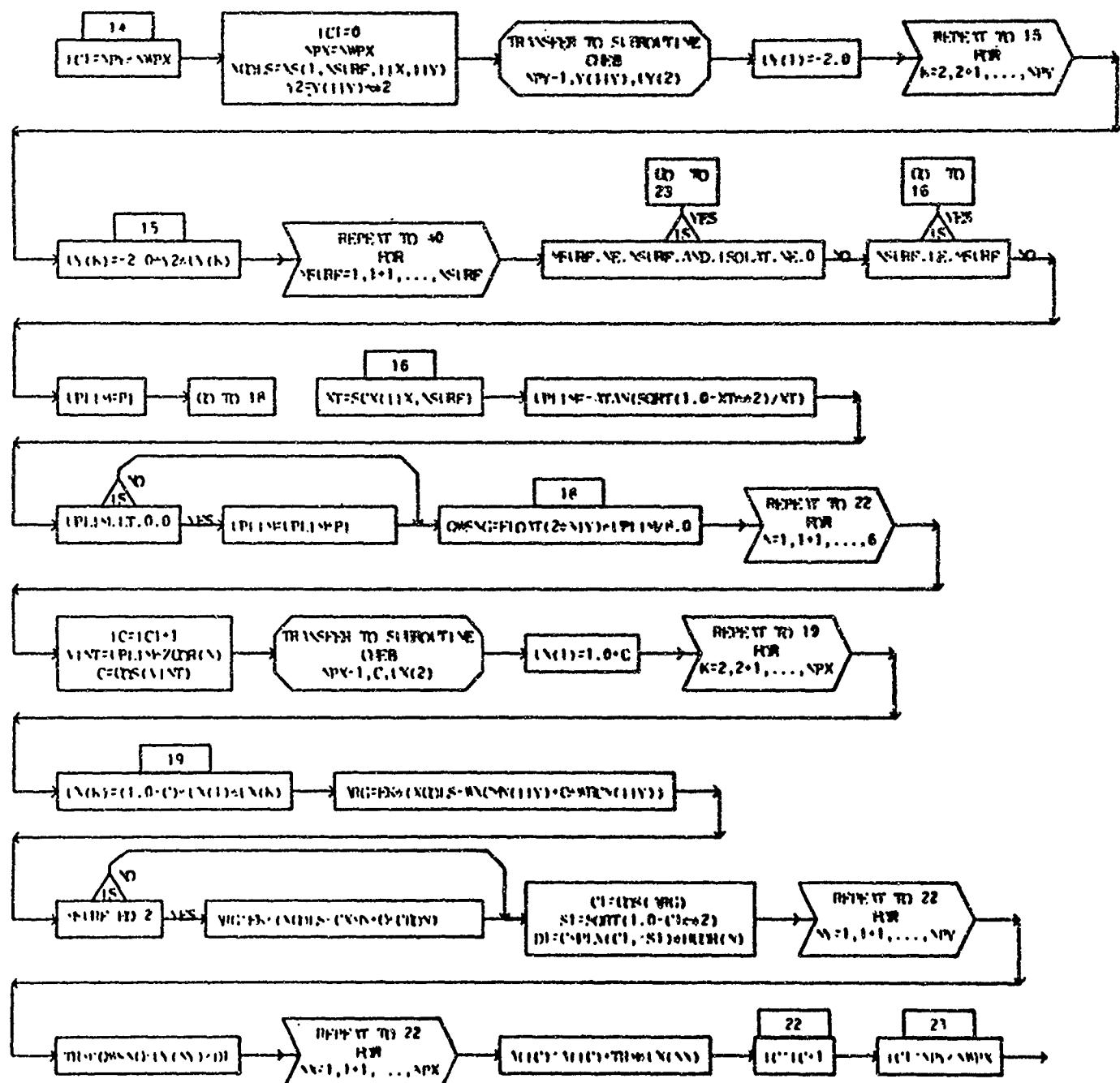
PAGE 1



*NOT REPRODUCIBLE*

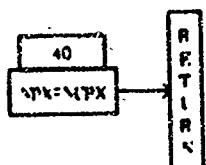
ROUTINE Q30

PAGE 2



STRUCTURE WORD

PAGE 1



CHS. CHS.

COMPLEX FUNCTION CRN1(X,V,C1,R2)

PAGE 1

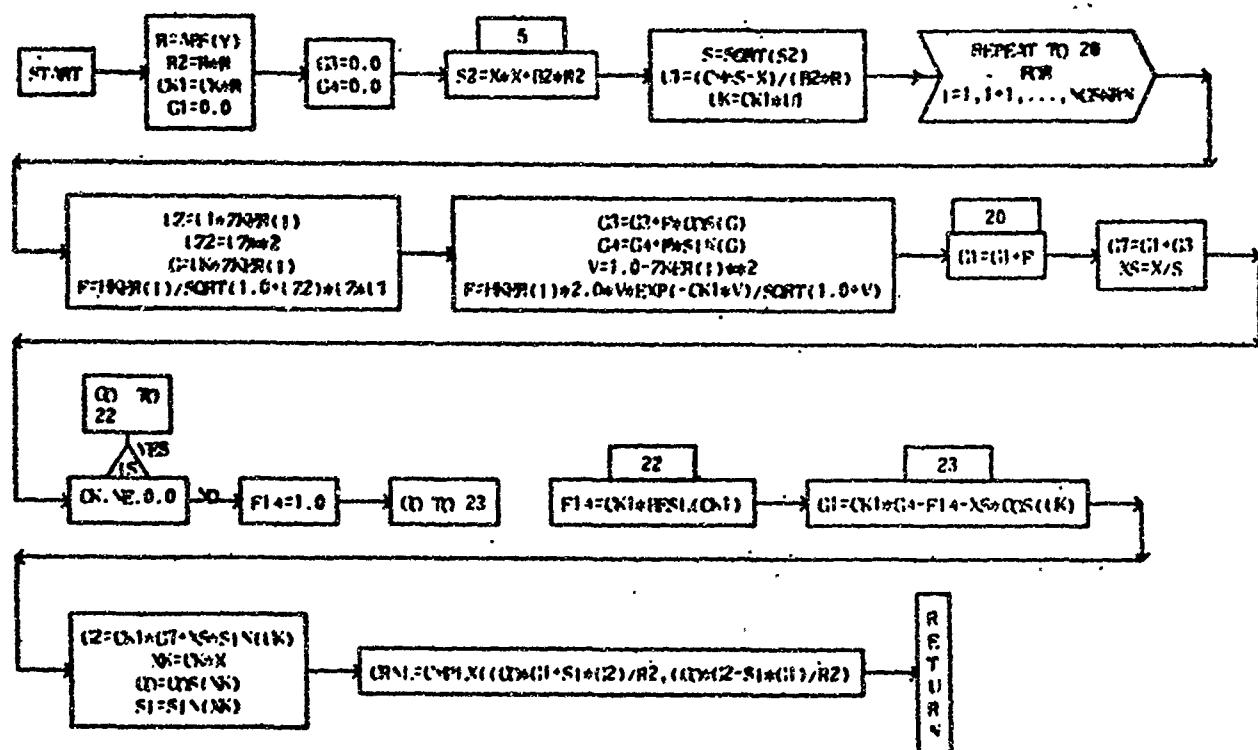
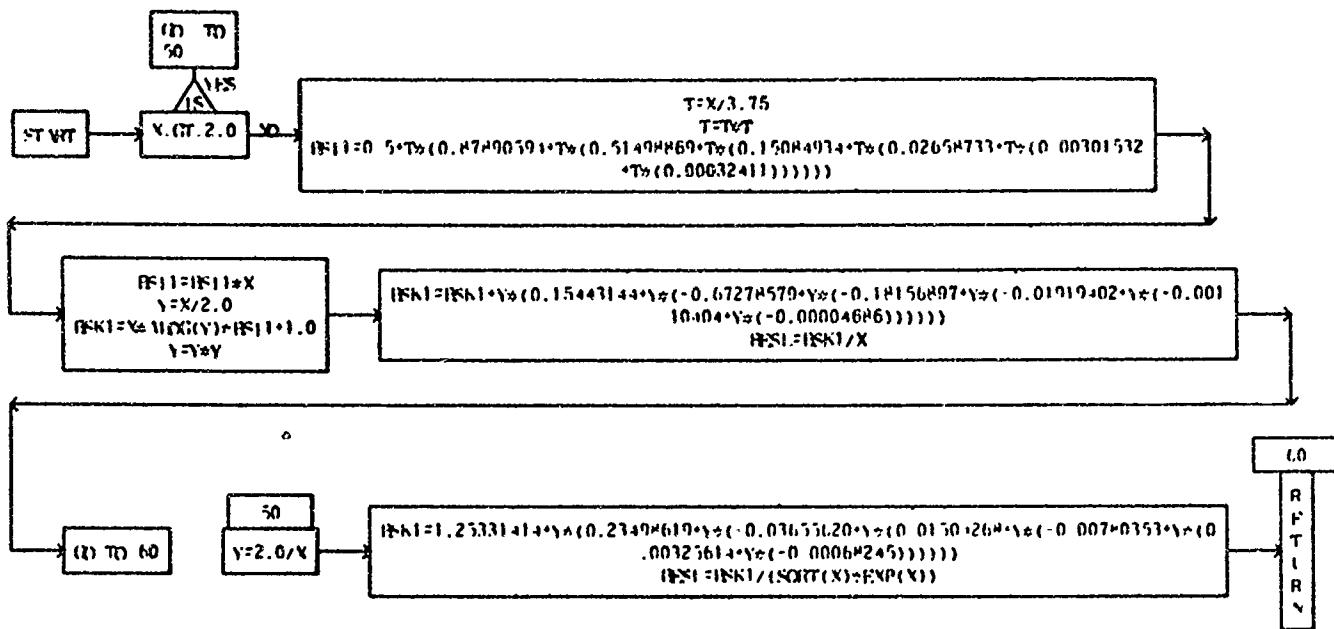




FIGURE 1(X)

ג'ז

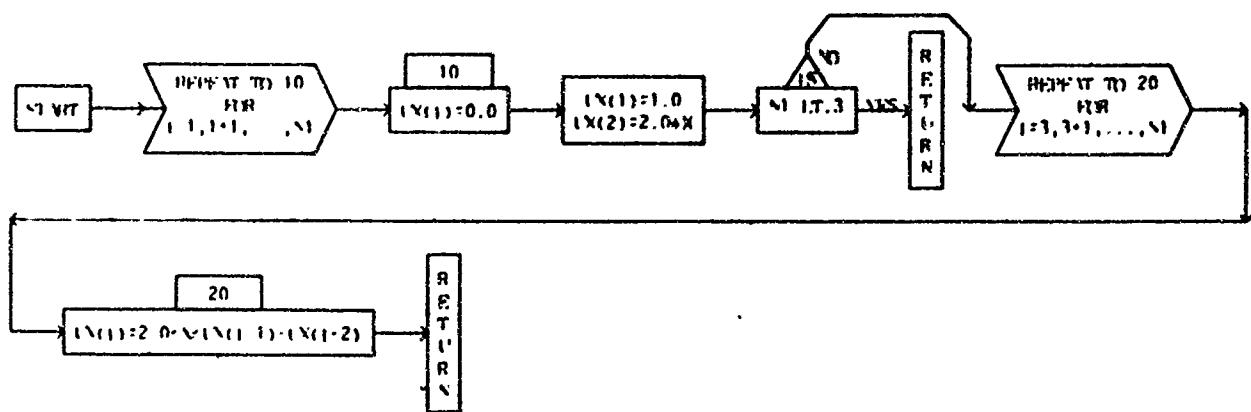


OFF OFF

DIMENSIONED VARIABLES

SYMBL	SYNTHESYS								
X	1								

## SUBROUTINE QERN1,X,1X1



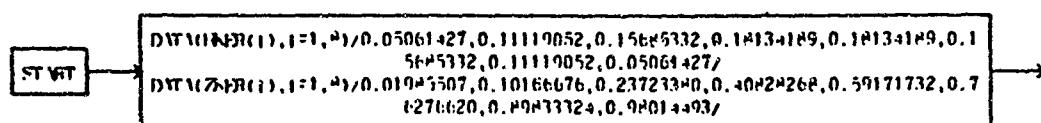
(b)(6) (b)(6)

DIMENSIONED VARIABLES

SYMOL.	STOR XES								
W10	40,40	W16H	40						

BLOCK DATA

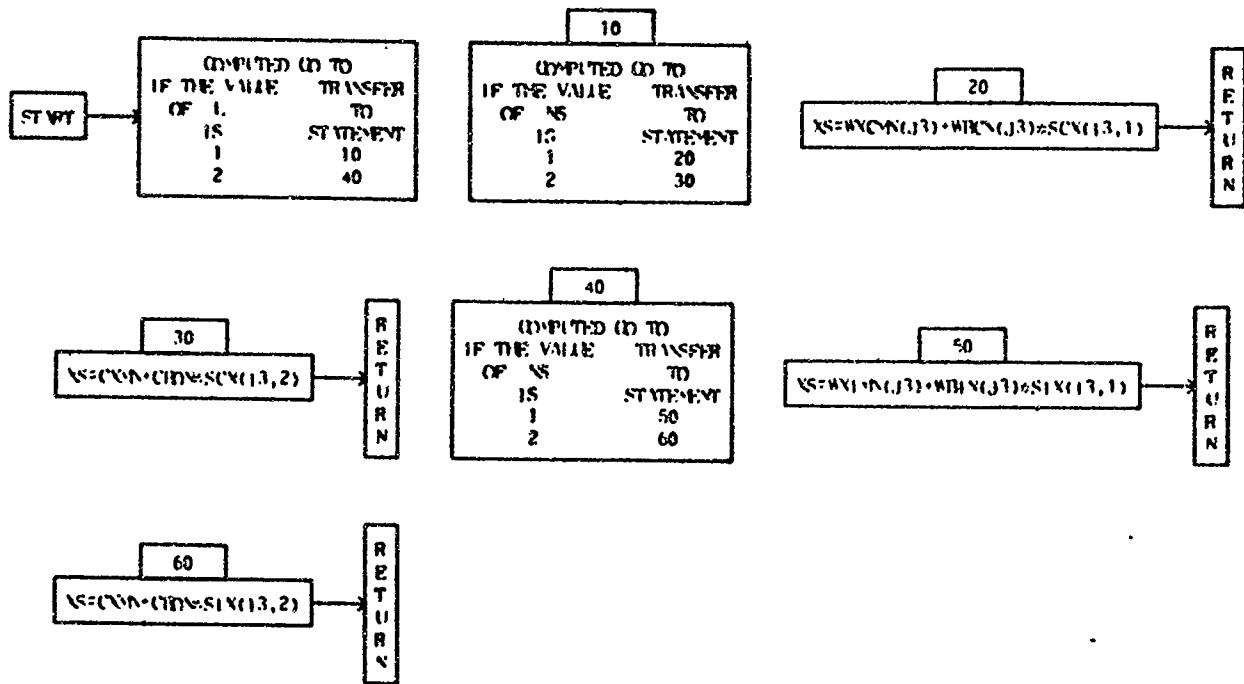
PAGE 1





FUNCTION XS(L,N,J3)

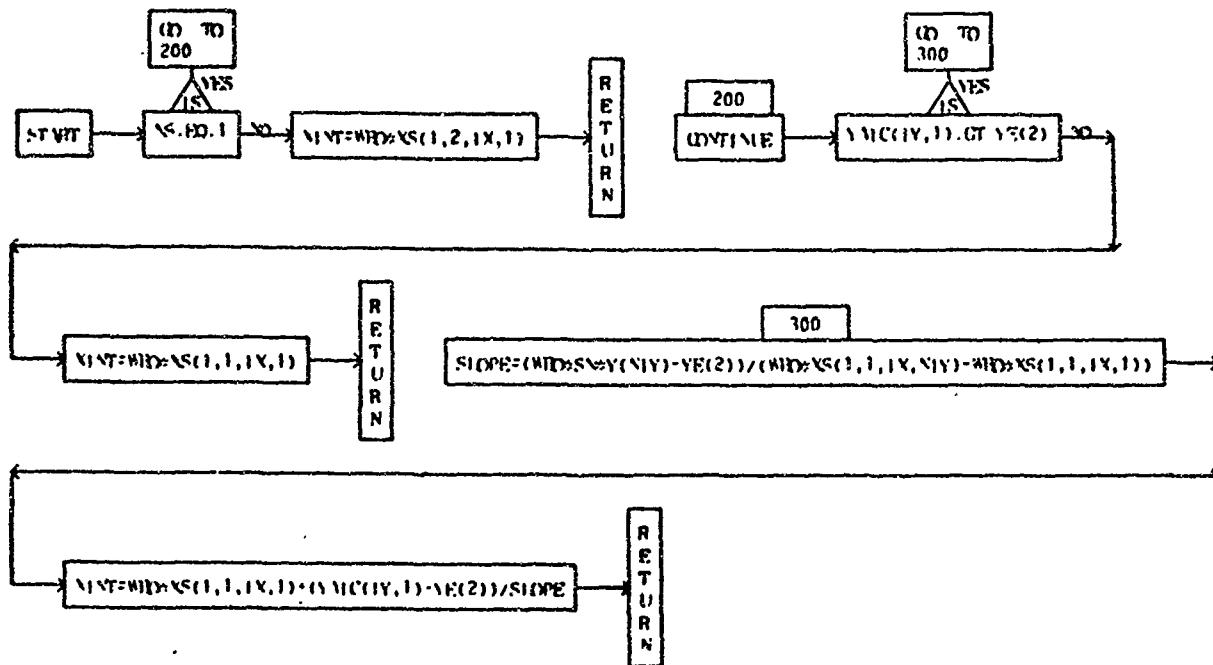
PAGE 1



1947

FUNCTION XINT (IY, IX, NY, NS, RD, SN)

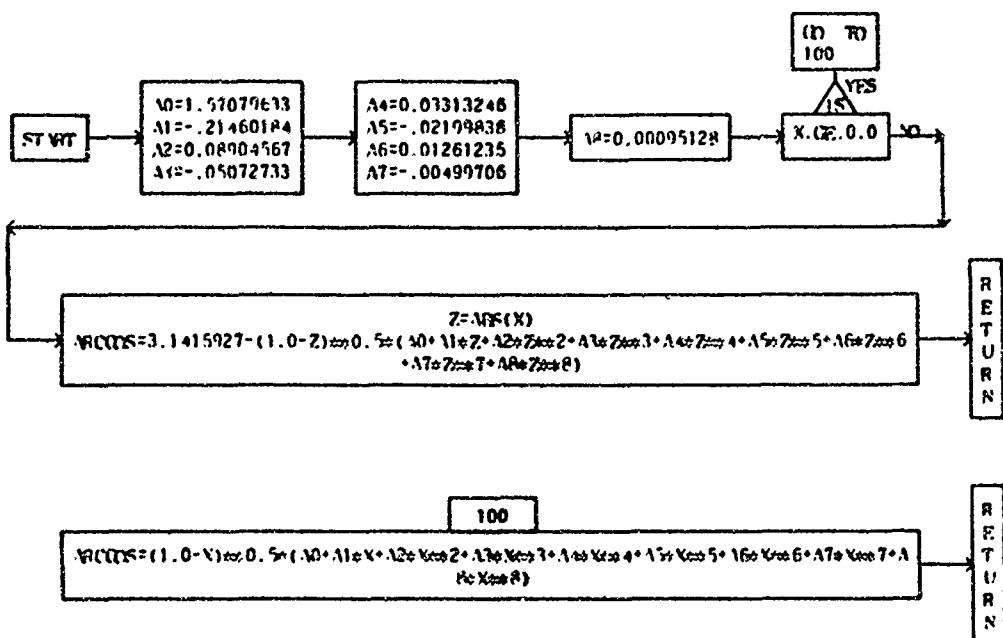
P(F-1)



WCUIS

## FUNCTION ARCCOS(X)

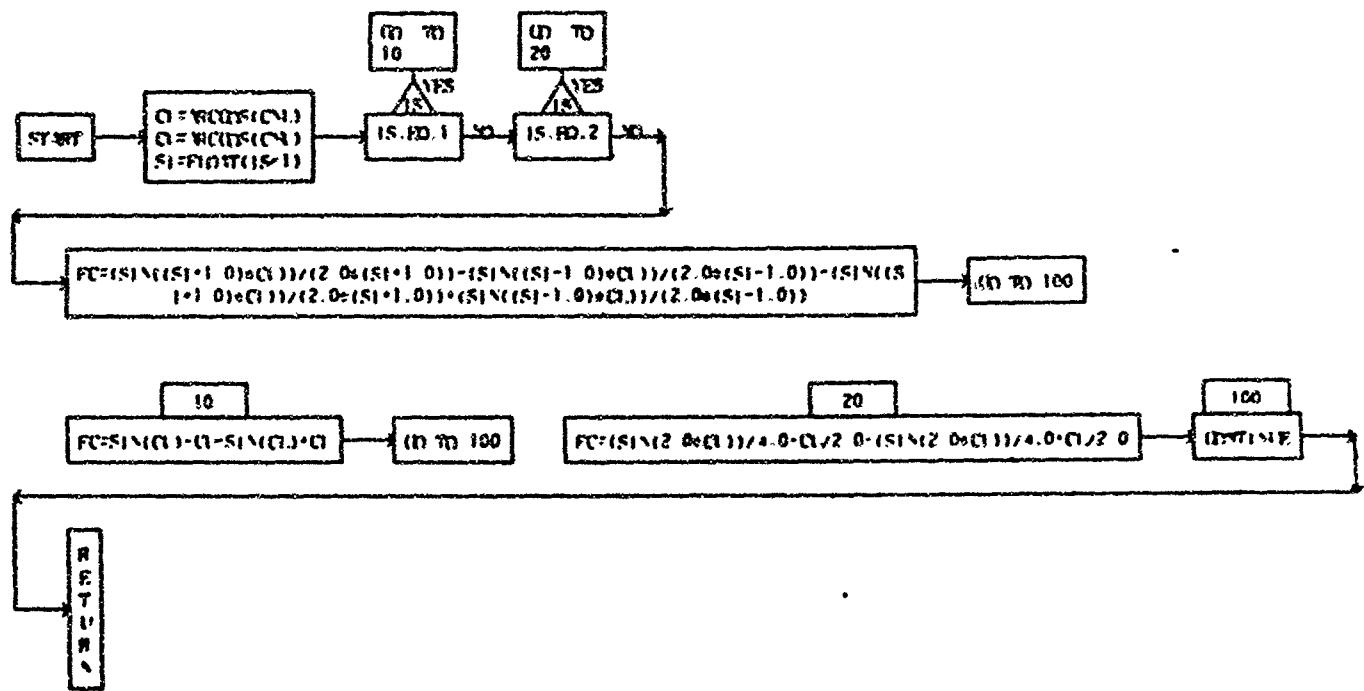
PAGE 1



447C

SIMPLIFIED MASTERS(SI,CV1,CV2,FC)

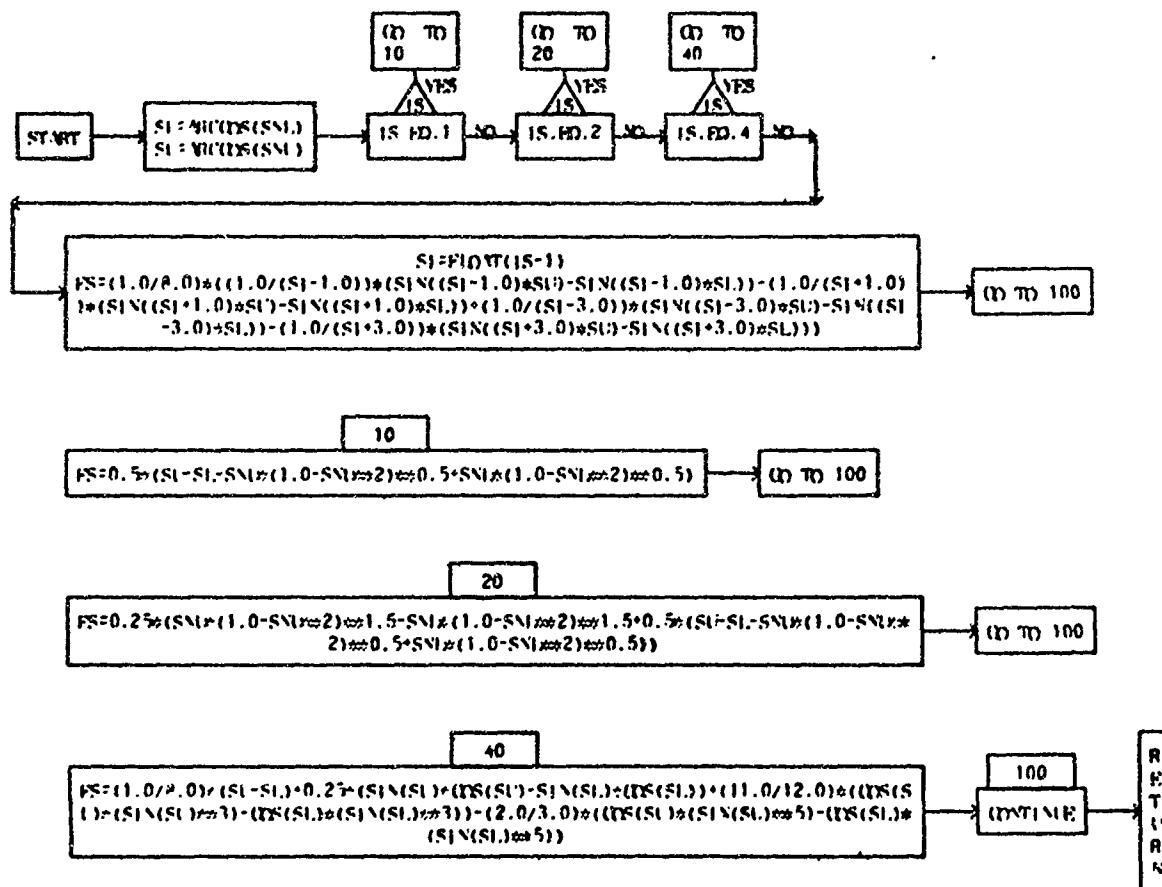
PAGE 1





ROUTINE MVSIS(SI,SNL,SNLFS)

PAGE 1



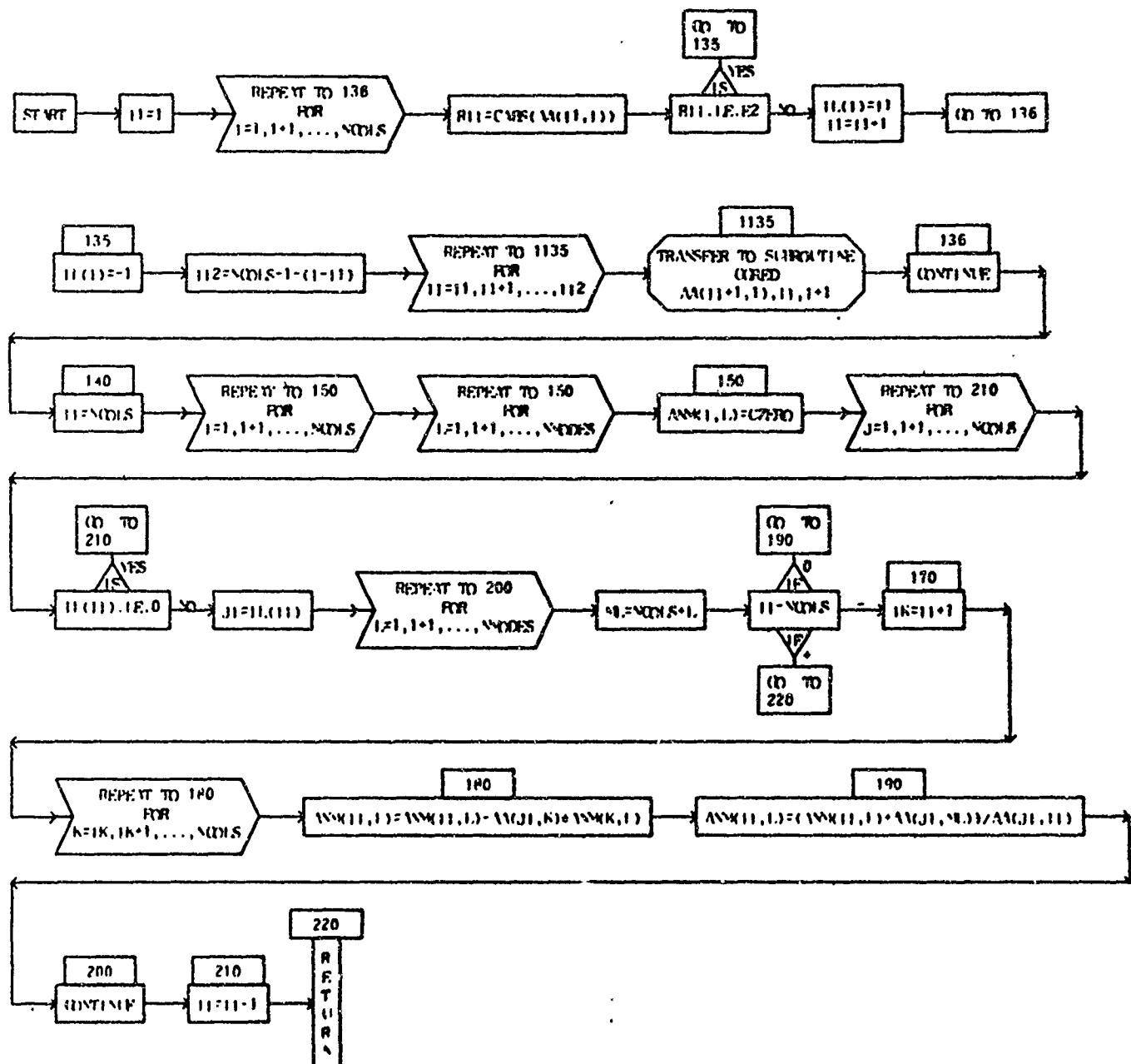
8180 8180

DIMENSIONED VARIABLES

SYMBOL	STORMES								
MC	10,20	WASH		40					

*NOT REPRODUCIBLE*

SUBROUTINE X10



A197310030001 L-18

ORW

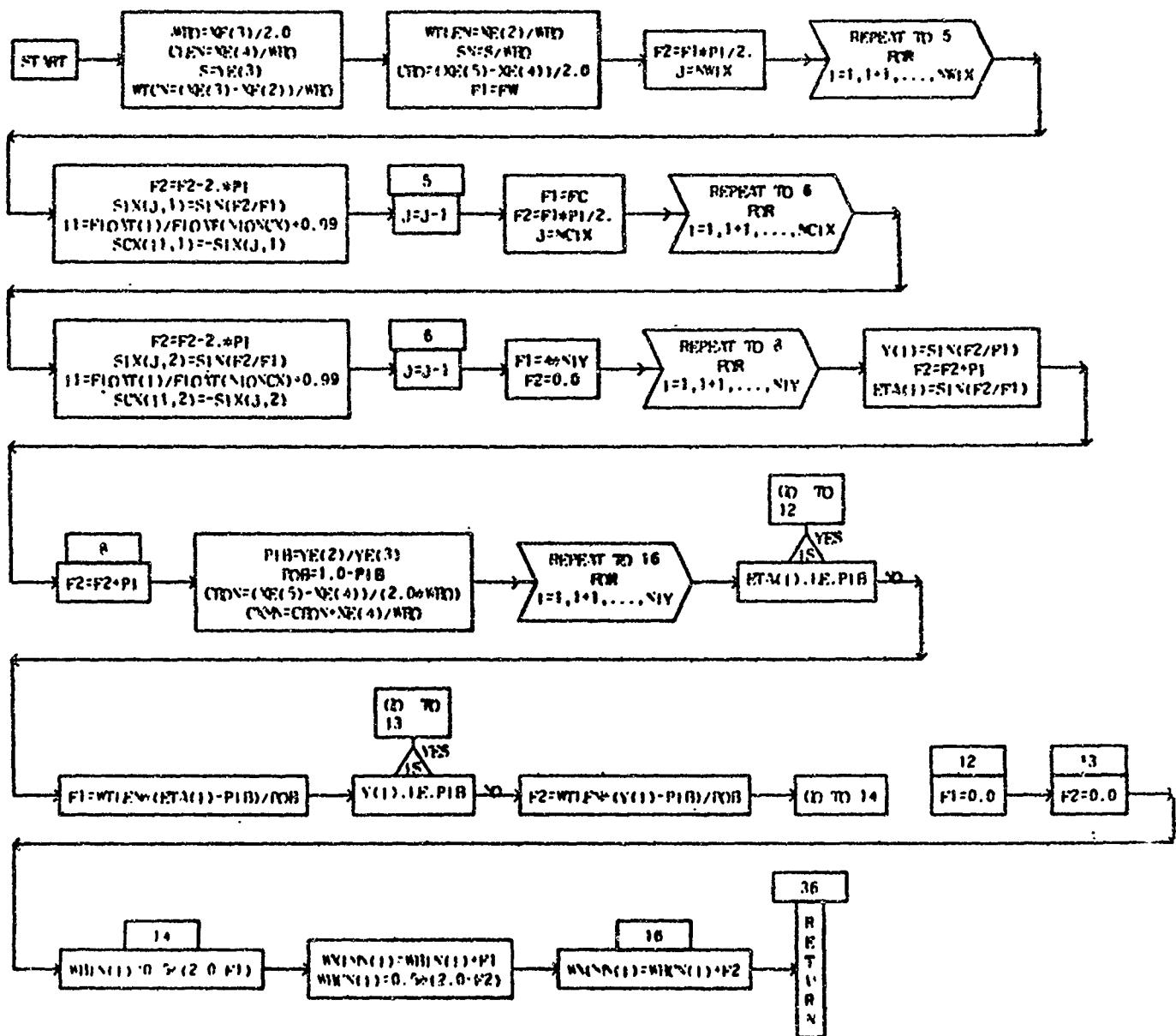
ORW

DIMENSIONED VARIABLES

SYMBOL	STORYES								
MC	40,40	WASH	40						

## SUBROUTINE Q374

PAGE 1

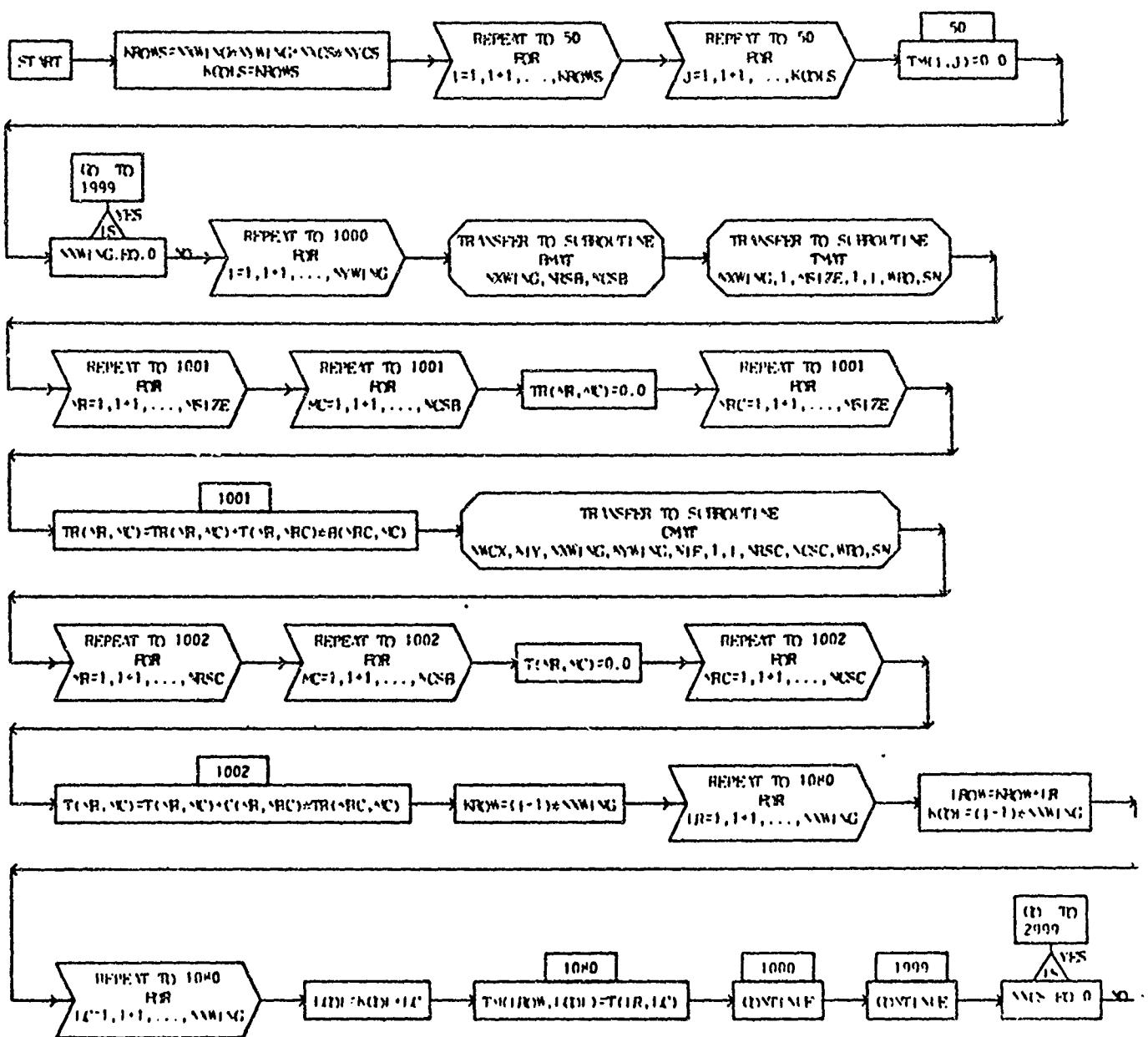


TR 14P

# NOT REPRODUCIBLE

SUBROUTINE TRAP(IVY, NROW, NCOL, NWING, NWING, NCSC, NCSC, NIF, MDO, SN)

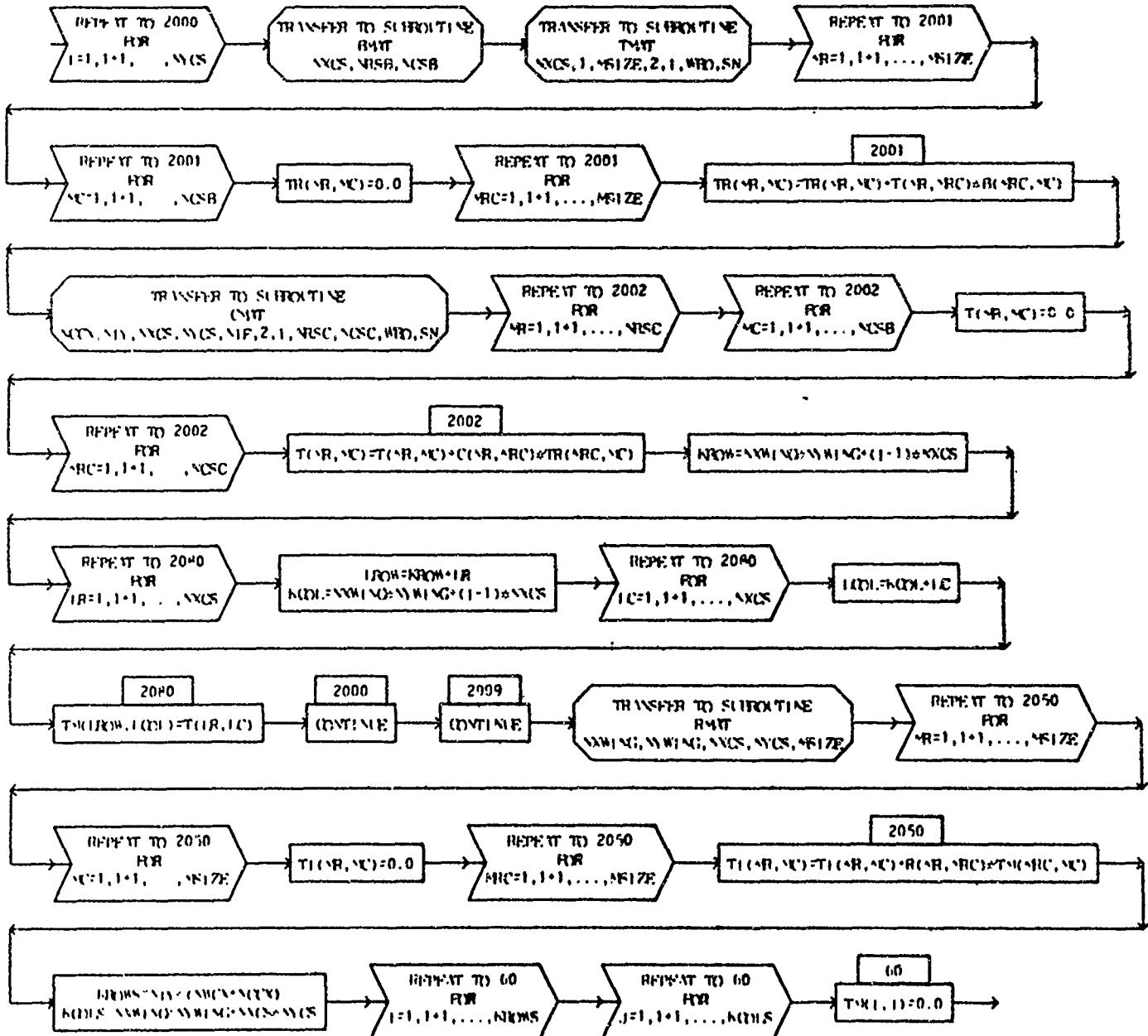
PAGE 1

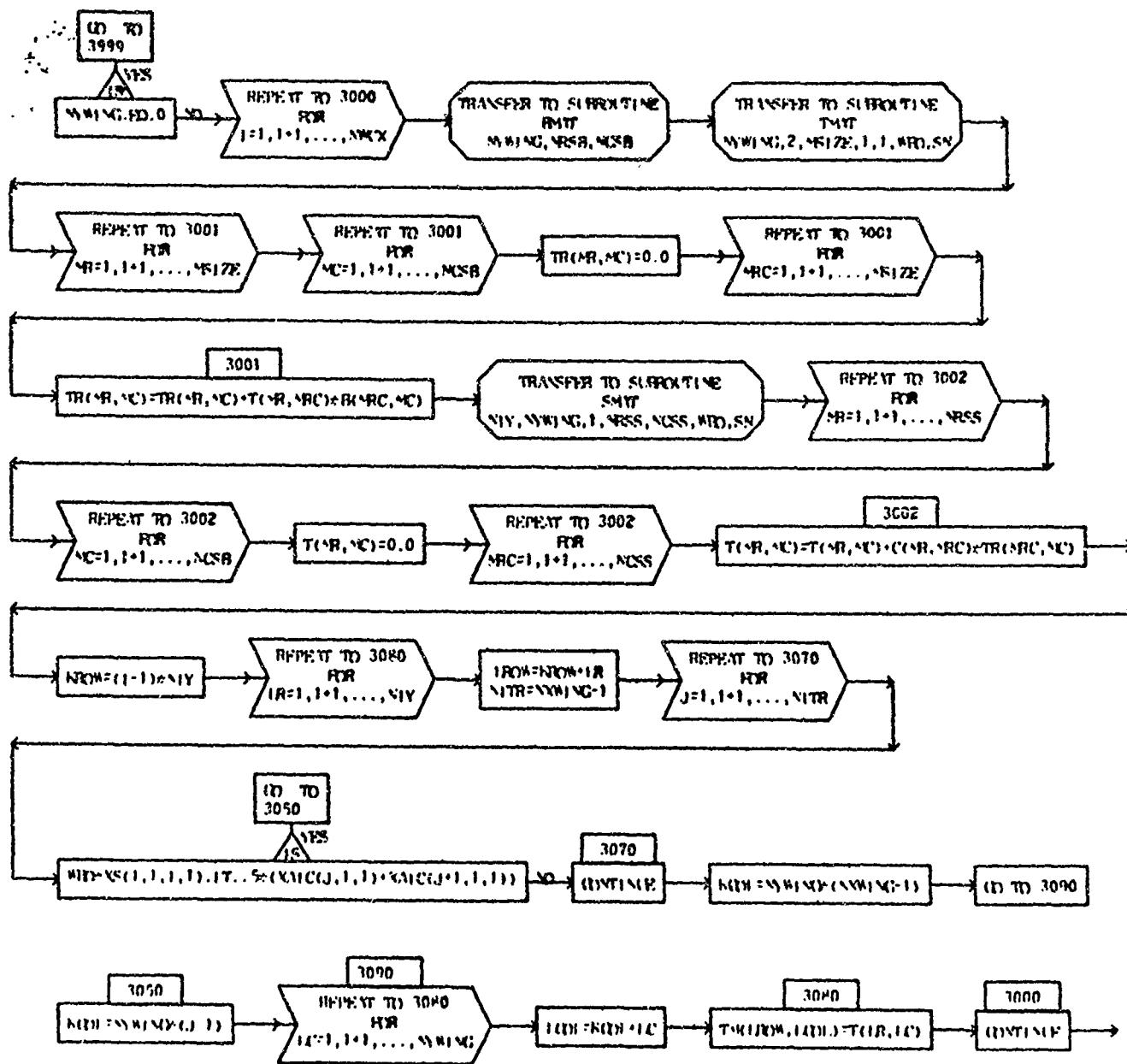


*NOT REPRODUCIBLE*

SUBROUTINE TRANSFER, NMC, NCX, NWING, NWING, NXCS, NCSC, NIF, WID, SN

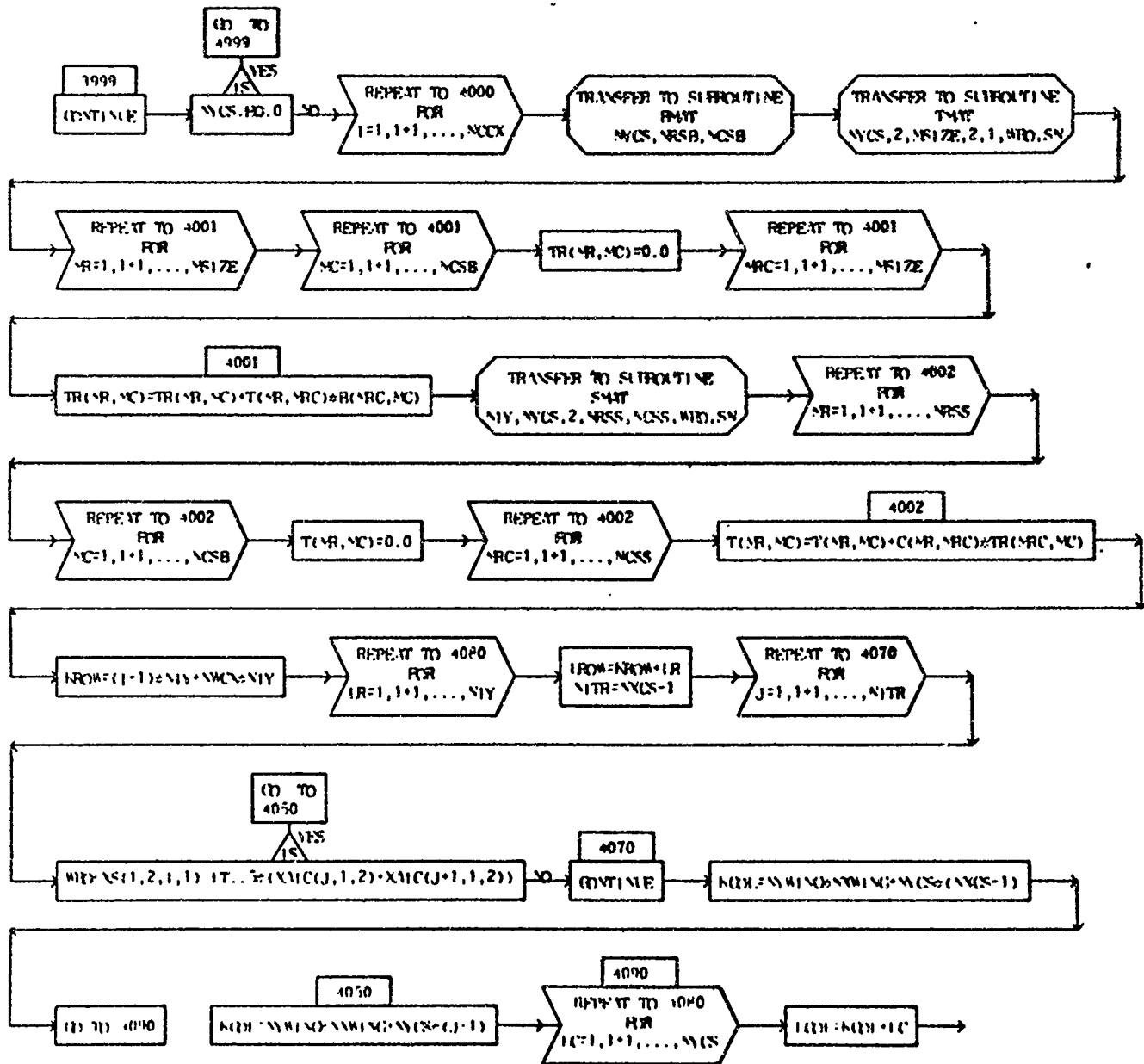
PART 2 1





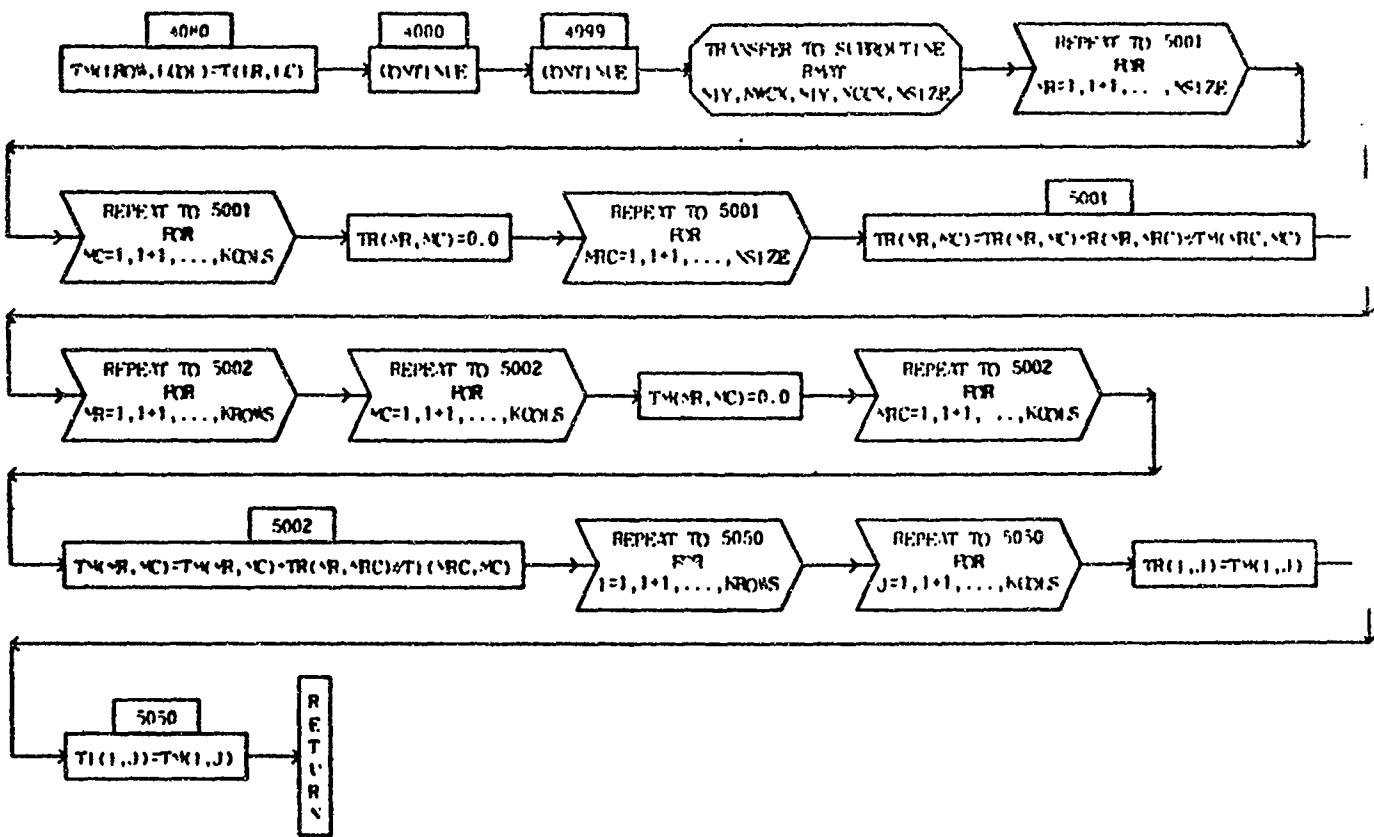
## SUBROUTINE TRAMPENY, NVCX, NCYC, NVCYC, NVCYC, NCS, NIP, NIO, SN

PAGE 4



SUBROUTINE TR(MY, MCX, MCY, MCZ, MCW, MCV, MCW, MCV, MCW, MCV)

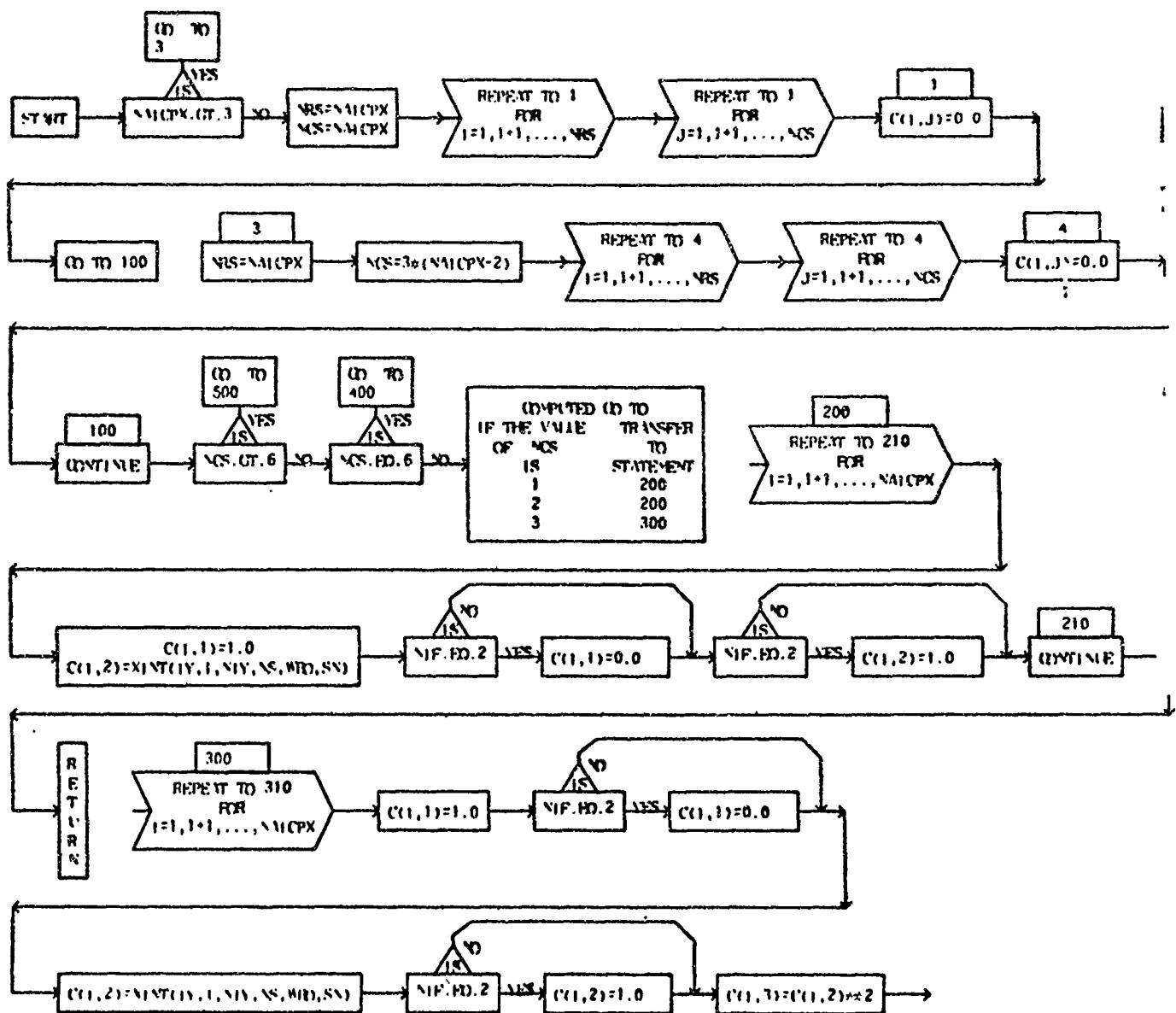
PAGE 3



CNT CNT

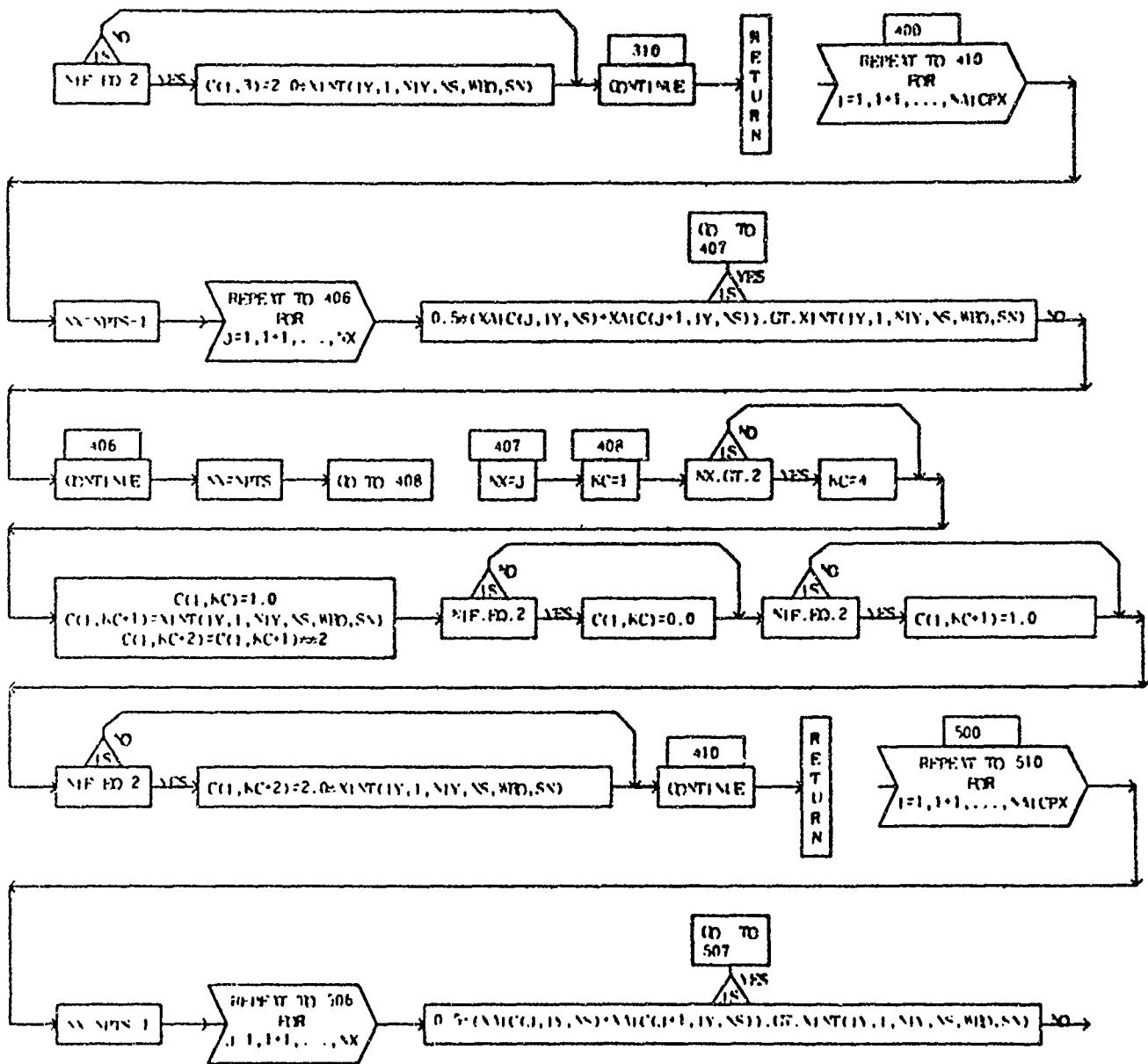
## SUBROUTINE CMTCPTS, NIV, NMCPX, NMCPY, NIF, NS, IV, VRS, NCS, WID, SN

PXF 1



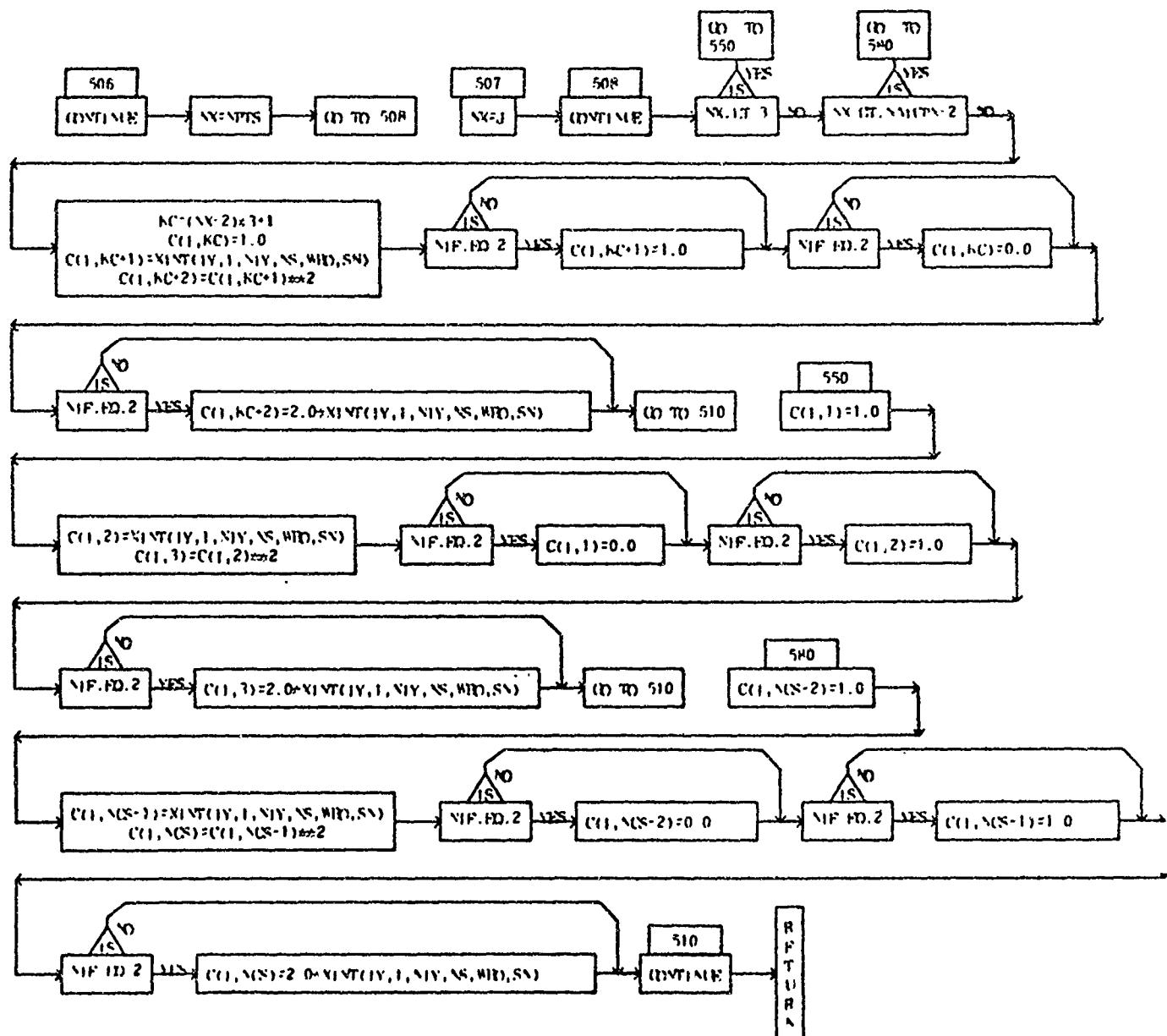
## SUBROUTINE CHITCPS(NY,NICPX,NACTPY,NIF,NS,IY,NRS,NCS,WID,SN)

PAGE 2



## SUBROUTINE CHAT(NPTS, NY, N1CPY, N2CPY, NF, NS, IY, NRS, NCS, WRD, SN)

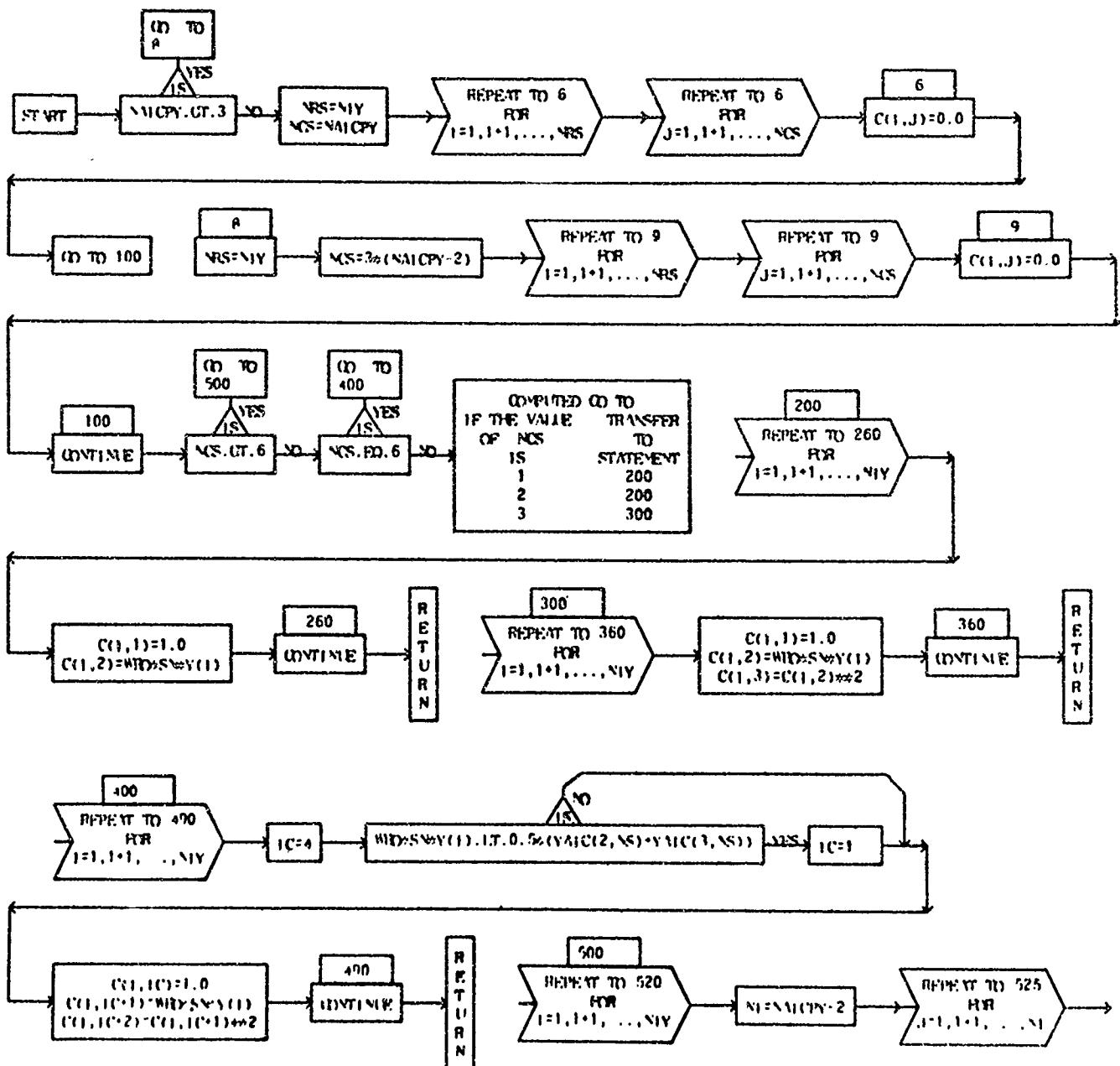
PAGE 3



SHT SHT

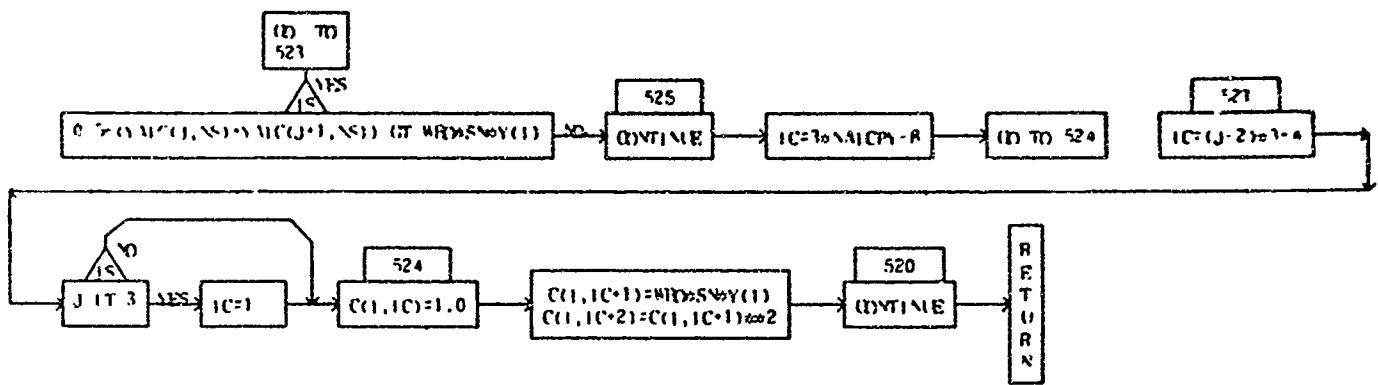
## SUBROUTINE SHIFT(V1,V2,COPY,NS,NVS,NCS,WID,SN)

PAGE 1



## SUBROUTINE SHITIN(Y,NSCTPY,N,NRS,NCS,MID,SY)

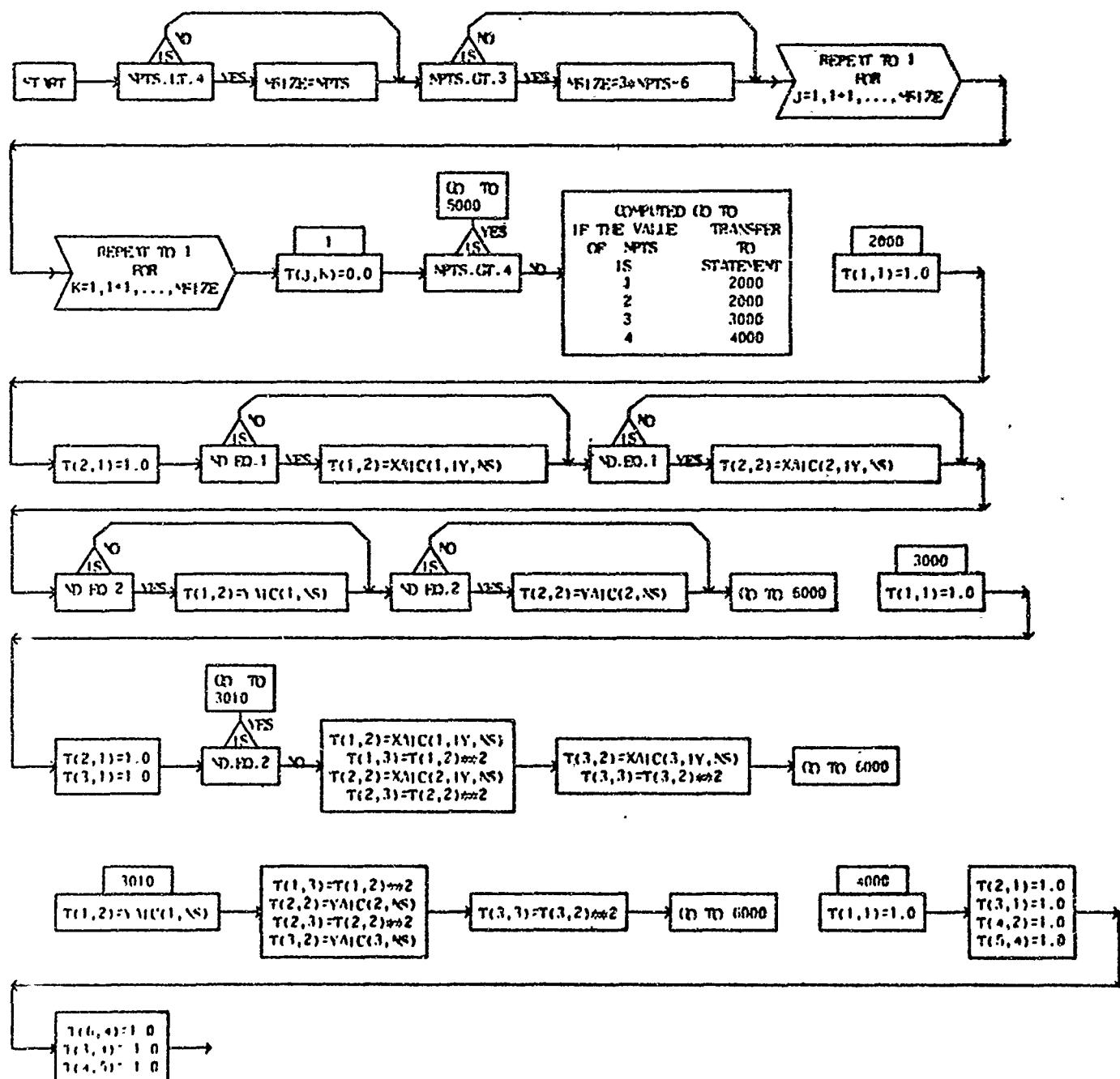
PAGE 2



THIR THIR

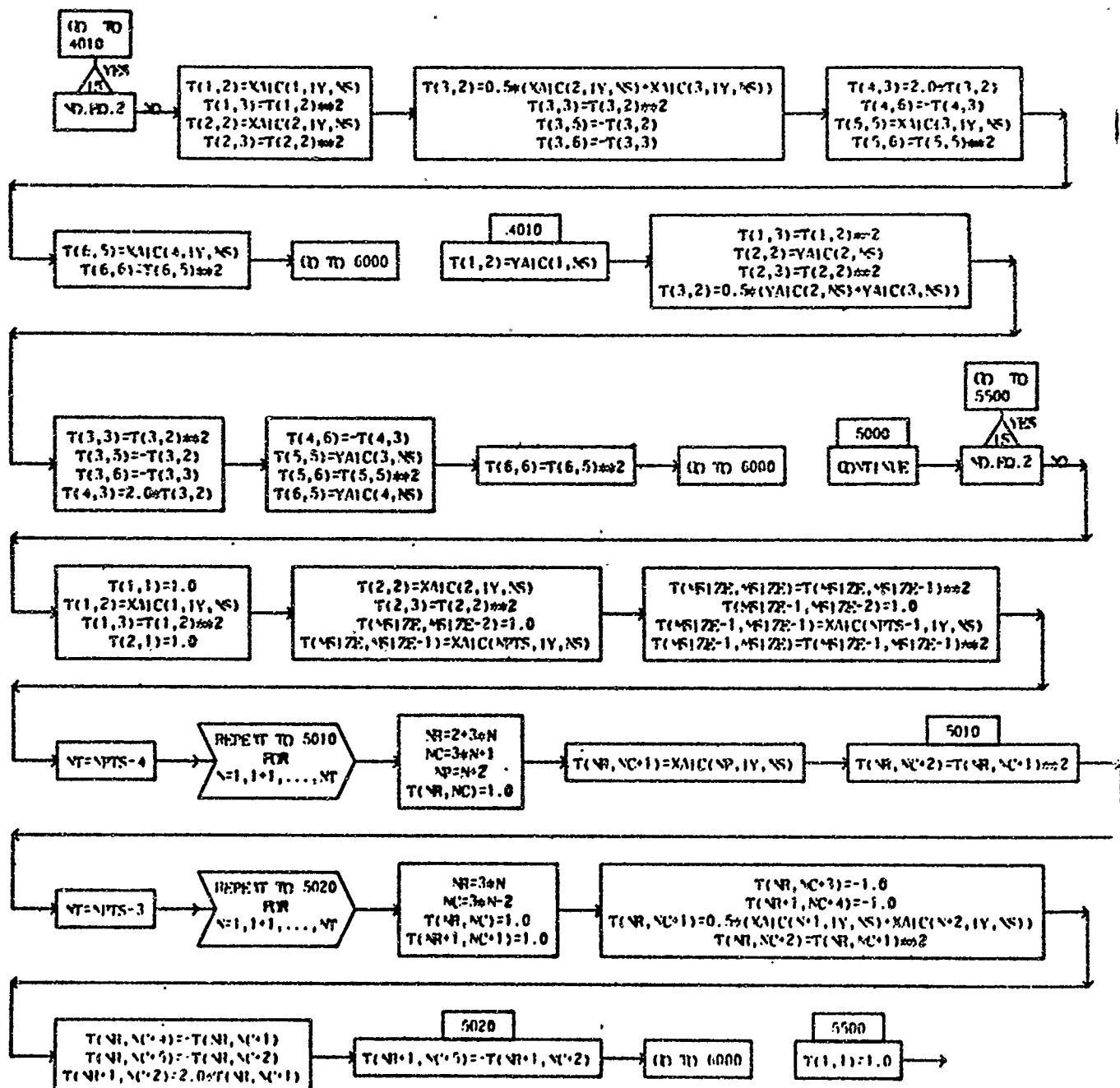
**STRUCTURE THAT (PTS, NO. MSIZE, NS, IV, WD, SN)**

३४६



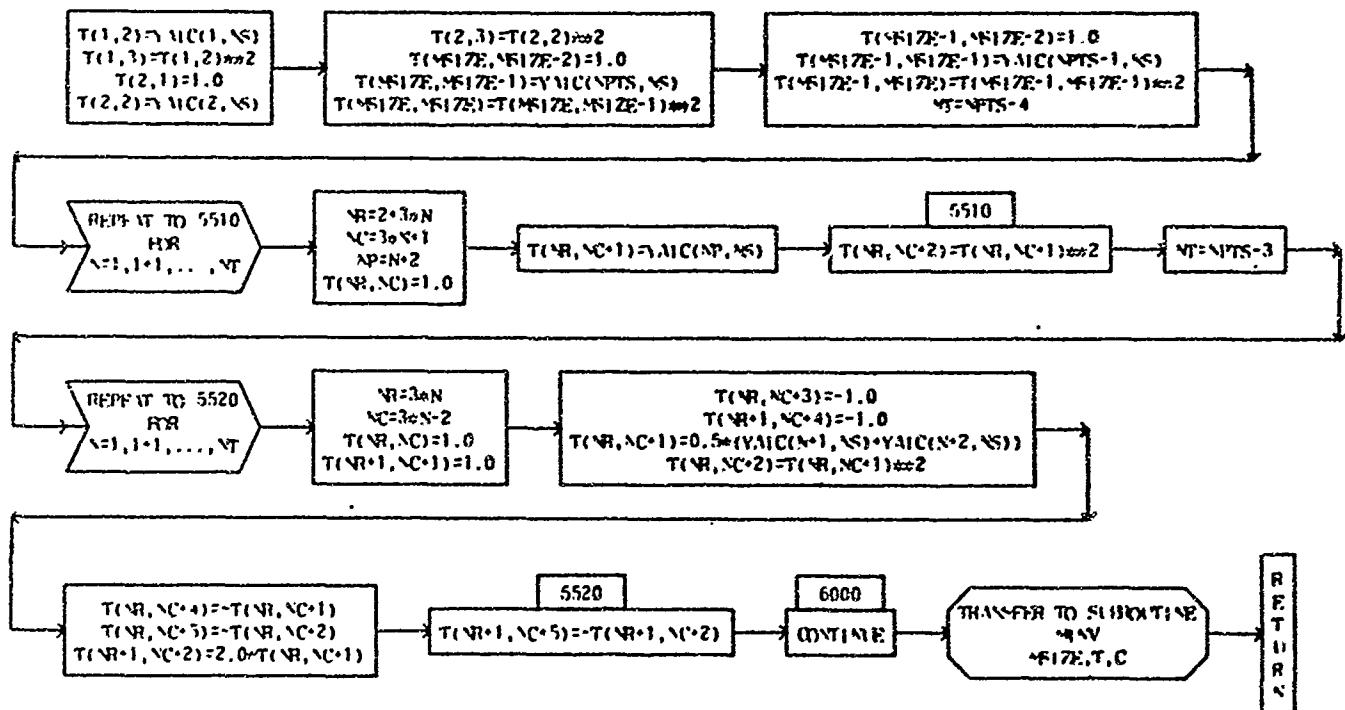
## SUBROUTINE TWT(NPTS, ND, NSIZE, NS, IY, WRD, SN)

EX 2



## SUBROUTINE TMT(NPTS, ND, NSIZE, NS, IV, WRD, SY)

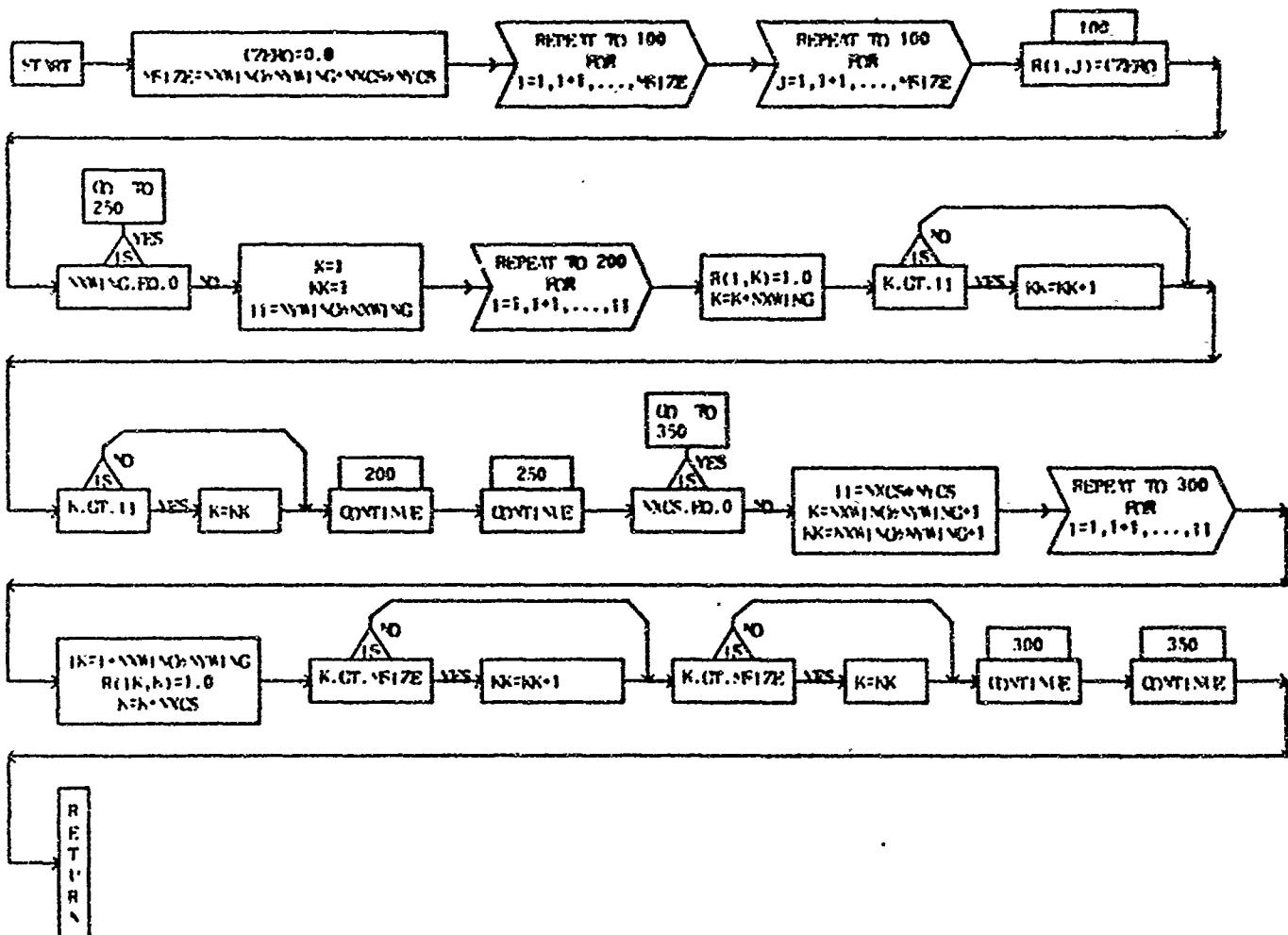
PAGE 3



R41T R41T

## SUBROUTINE RMT (N1NG, N2NG, N1CS, N2CS, NSIZE)

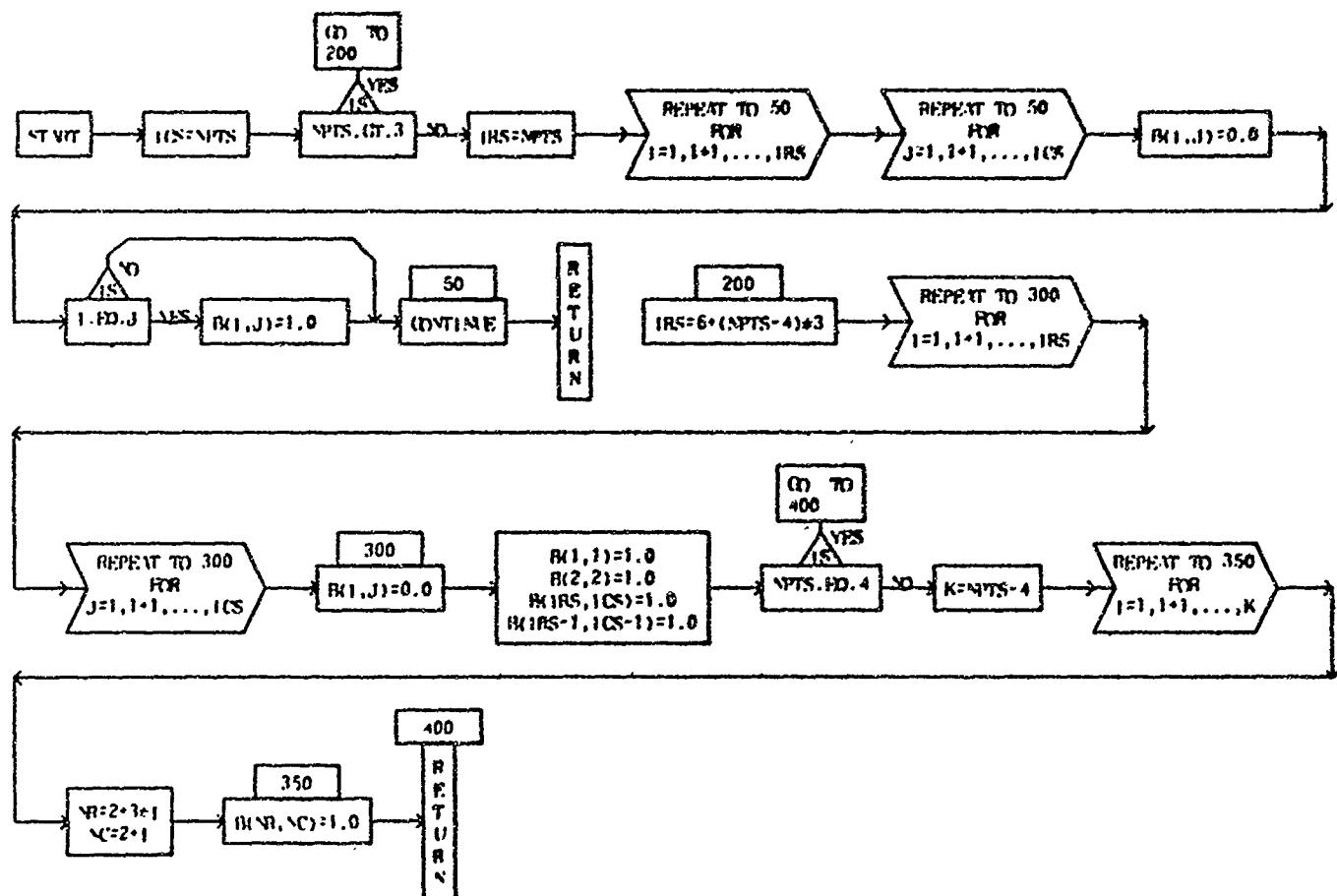
PAGE 1



HIT HIT

SUBROUTINE RMTINPTS, IRS, ICS

PAGE 1



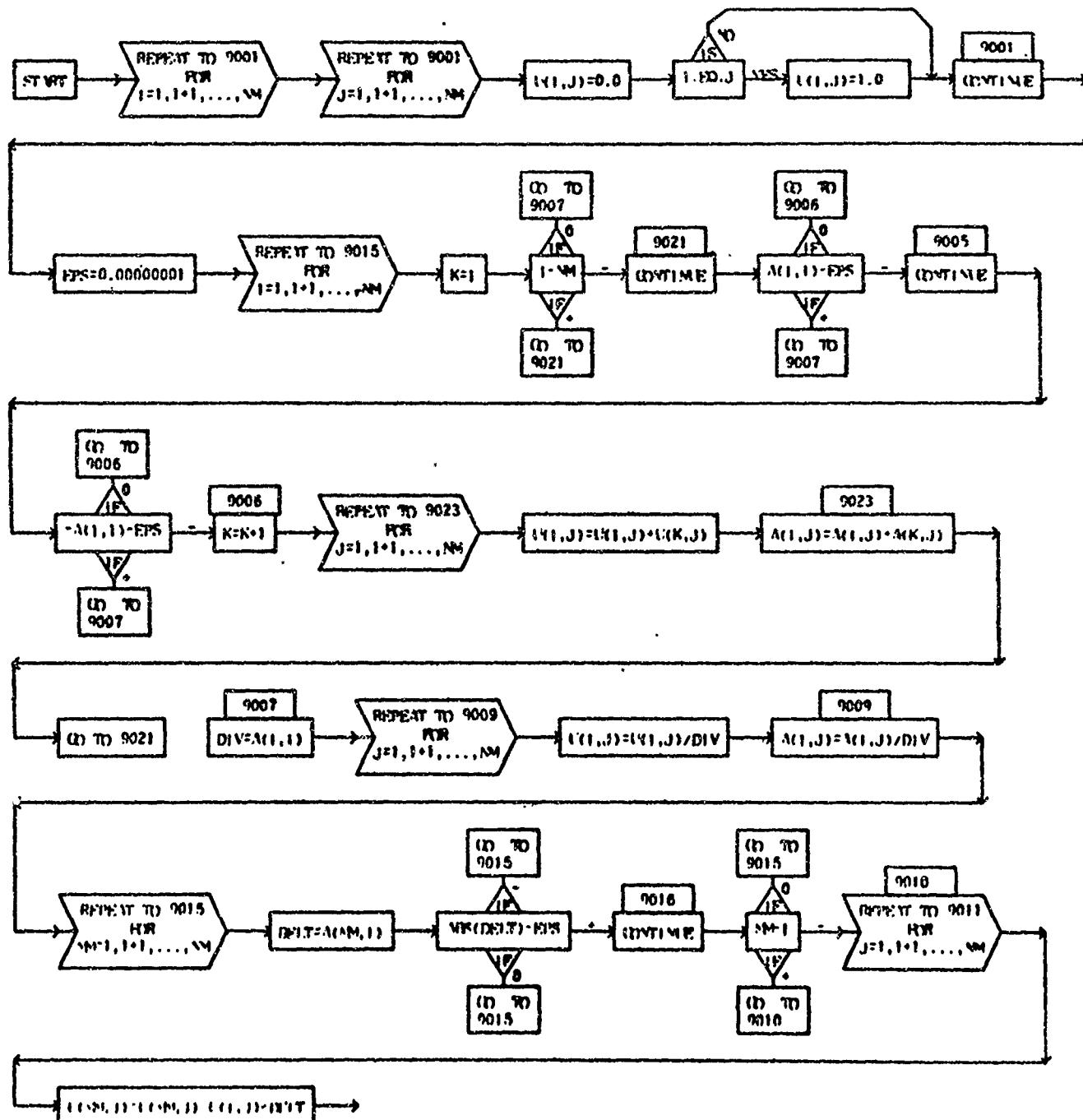
W W W

DIMENSIONED VARIABLES

SYMB.	STORAGES								
3	40,40	4	40,40						

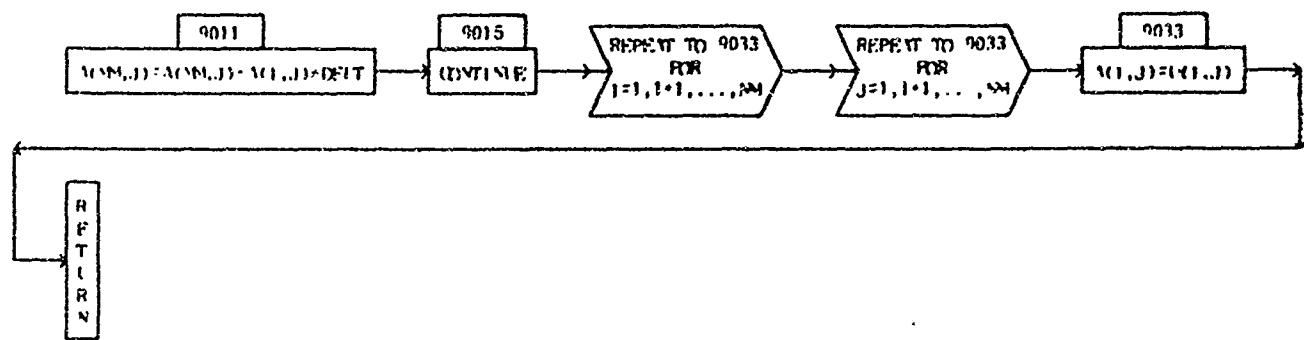
## SUBROUTINE MVN (NM,A,U)

PAGE 1



ROUTINE M45V (M,A,I)

PAGE 2



**UNCLASSIFIED**

Security Classification

**DOCUMENT CONTROL DATA - R & D**

(Security classification of title, body of abstract and indexing annotation must be entered when the overall report is classified)

1. ORIGINATING ACTIVITY (Corporate author) HUGHES AIRCRAFT COMPANY, MISSILE SYSTEMS DIVISION FALLBROOK AND ROSCOE BLVDS. CANOGA PARK, CALIFORNIA 91304	2a. REPORT SECURITY CLASSIFICATION <b>UNCLASSIFIED</b>
	2b. GROUP

**3. REPORT TITLE**

COLLOCATION FLUTTER ANALYSIS STUDY

**4. DESCRIPTIVE NOTES (Type of report and inclusive dates)**

FINAL REPORT (MARCH 1968 THROUGH MARCH 1969)

**5. AUTHOR(S) (First name, middle initial, last name)**

DYNAMICS AND ENVIRONMENT SECTION, DONALD R. ULRICH

6. REPORT DATE APRIL 4, 1969	7a. TOTAL NO OF PAGES	7b. NO OF REFS
---------------------------------	-----------------------	----------------

8a. CONTRACT OR GRANT NO N00019-68-C-0247	9a. ORIGINATOR'S REPORT NUMBER(S)
--	-----------------------------------

b. PROJECT NO	9b. OTHER REPORT NO(S) (Any other numbers that may be assigned to this report)
---------------	--

c.	
d.	

**10. DISTRIBUTION STATEMENT**  
~~IN ADDITION TO SECURITY REQUIREMENTS WHICH APPLY TO THIS DOCUMENT, AN ADDITIONAL SECURITY REQUIREMENT IS THAT EACH TRANSMISSION OF THIS DOCUMENT OUTSIDE THE AGENCIES OF THE U.S. GOVERNMENT MUST HAVE PRIOR APPROVAL OF THE COMMANDER NASC~~

11. SUPPLEMENTARY NOTES	12. SPONSORING MILITARY ACTIVITY NAVAL AIR SYSTEMS COMMAND DEPARTMENT OF THE NAVY WASHINGTON, D.C.
-------------------------	---

e. ABSTRACT	
-------------	--

THIS STUDY COVERS THE DEVELOPMENT OF A SET OF COMPUTER PROGRAM TO PERFORM FLUTTER ANALYSIS BY THE COLLOCATION METHOD. WHILE THIS METHOD HAS BEEN KNOWN FOR SOME TIME, ONLY RECENTLY HAVE ADVANCES IN COMPUTER TECHNOLOGY MADE THE METHOD TECHNICALLY AND FINANCIALLY FEASIBLE. THE INGREDIENTS OF A COLLOCATION FLUTTER ANALYSIS ARE: 1) A FLEXIBILITY MATRIX, 2) AERODYNAMIC INFLUENCE COEFFICIENT MATRIX, AND 3) AN EIGENVALUE SOLUTION. THIS STUDY IS PRESENTED IN FOUR VOLUMES. VOLUME I CONTAINS A GENERAL PROGRAM DISCUSSION. VOLUME II CONTAINS THE PROGRAM FLEX WHICH CALCULATES THE FLEXIBILITY MATRIX. VOLUME III CONTAINS A SET OF THREE PROGRAMS TO CALCULATE AERODYNAMIC INFLUENCE COEFFICIENTS FOR SUPERSONIC, TRANSonic, AND SUBSONIC FLIGHT REGIMES. VOLUME IV CONTAINS THE PROGRAM COFA WHICH SETS UP AND SOLVES THE FLUTTER EIGENVALUE MATRIX.

DD FORM 1473

**UNCLASSIFIED**

Security Classification

UNCLASSIFIED

Security Classification

14. KEY WORDS	LINK A		LINK B		LINK C	
	ROLE	WT	ROLE	WT	ROLE	WT
FLUTTER VIBRATION AERODYNAMIC INFLUENCE COEFFICIENTS						

UNCLASSIFIED

Security Classification